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A predictive model for planning emergency events rescue during COVID‑19 in Lombardy, Italy

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Abstract

Forecasting the volume of emergency events is important for resource utilization in emergency medical services (EMS). This became more evident during the COVID-19 outbreak when emergency event forecasts used by various EMS at that time tended to be inaccurate due to fuctuations in the number, type, and geographical distribution of these events. The motivation for this study was to develop a statistical model capable of predicting the volume of emergency events for Lombardy's regional EMS called AREU at diferent time horizons. To accomplish this goal, we propose a negative binomial additive autoregressive model with smoothing splines, which can predict over-dispersed counts of emergency events one, two, five, and seven days ahead. In the model development stage, a large set of covariates was considered, and the fnal model was selected using a cross-validation procedure that takes into account the observations' temporal dependence. Comparisons of the forecasting performance using the mean absolute percentage error showed that the proposed model outperformed the model used by AREU, as well as other widely used forecasting models. Consequently, AREU decided to adopt the new model for its forecasting purposes.

Keywords Decision support system · Emergency call data · Emergency departments data · Generalized nonlinear auto-regressive additive model · Predictive models

1 Introduction

Emergency medical services (EMS) represent the frst point of healthcare access for millions of patients worldwide in need of urgent treatments. Despite the heterogeneous organization of EMS agencies globally, they all share the primary goal of minimizing intervention time. To achieve this goal with limited resources, statistical models for forecasting the number of emergency calls and rescue missions play a crucial role in informing EMS agencies about future activity volumes, which are

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subject to signifcant daily and seasonal fuctuations. These fuctuations are infuenced by seasonal weather variations and extreme weather events (Alessandrini et al. [2011;](#page-22-0) Bassil et al. [2009;](#page-23-0) Lin et al. [2013](#page-23-1); Attia and Edward [1998](#page-22-1); Noble et al. [1971](#page-23-2)), such as heat waves or cyclones (Noji [2000](#page-23-3)), social and demographic factors (Schuman et al. [1977](#page-24-0); Kamenetzky et al. [1982\)](#page-23-4), and epidemiological phenomena (Al Amiry and Maguire [2021;](#page-22-2) Diaz et al. [2001](#page-23-5)), such as infuenza epidemics. Additionally, the day of the week and the time of the day impact the volume of EMS activity on diferent timescales (Cantwell et al. [2015](#page-23-6); Batal et al. [2001](#page-23-7)). In this complex framework, predictive models that account for all these factors can assist EMS organizations in optimal staf management and distributing ambulances and rescue equipment.

The importance of reliable predictive models became evident with the emergence of the COVID-19 pandemic. During that period, EMS organizations faced sudden and signifcant changes in the volume of emergency calls, and existing predictive models failed to capture this phenomenon. Thus, forecasting the number of calls and rescue missions in the near future is essential to optimize resource allocation and address the rapidly evolving needs of the served populations.

In this study, we describe the development of a predictive model to reliably forecast the number of emergency events in the Lombardy region of Italy. This research efort was driven by a request from AREU (*Agenzia Regionale Emergenza Urgenza*), the regional agency responsible for the organization and implementation of EMS, for a reliable predictive model to inform organizational decisions during and after the COVID-19 outbreak. Before the COVID-19 pandemic, AREU routinely used a predictive tool based on an unobserved component model for time series data (Harvey [1990\)](#page-23-8). However, this model was only developed to forecast events in the metropolitan area of Milan, the region's capital and most populous city in the Lombardy region, and it performed poorly when the COVID-19 pandemic began. Therefore, a new family of predictive models covering diferent areas of Lombardy and accounting for COVID-19-related factors was urgently needed.

The aim was to provide AREU with a predictive model that is (i) computationally efficient and time-effective, allowing for daily updates and new daily predictions, (ii) feasible in terms of accessible and up-to-date covariates, and (iii) fexible to accom-modate epidemiological and social changes (Kenett and Gotwalt [2022\)](#page-23-9).

To fulfll this purpose, we propose a generalized additive model (GAM, Hastie and Tibshirani [2017](#page-23-10)) with a negative binomial family, nonlinear autoregressive terms (Kedem and Fokianos [2002](#page-23-11)), and exogenous covariates, which can deal overdispersed count time series (Agresti [2015](#page-22-3)). The proposed model is fexible, allowing for nonlinear dependence between covariates and outcomes. Although the same family of models (i.e., GAM) has already been used to develop predictive models in a similar framework (e.g., Viglino et al. ([2017\)](#page-24-1)), our approach is the frst to simultaneously address nonlinearity, auto-regressive efects (Kedem and Fokianos [2002\)](#page-23-11), over-dispersion (Agresti [2015](#page-22-3)), time (Kedem and Fokianos [2002\)](#page-23-11), weather (Attia and Edward [1998;](#page-22-1) Noble et al. [1971](#page-23-2)) and epidemiological (Diaz et al. [2001\)](#page-23-5) factors. For a recent and exhaustive review of the literature on predictive models in the feld of EMS, see Al-Azzani et al. ([2021\)](#page-22-4); Huang et al. ([2021\)](#page-23-12) and the references therein. The developed model was compared, in terms of predictive performance, to

alternative forecasting methods, including the predictive tool used by AREU before the COVID-19 pandemic.

We focused our modeling efforts on predicting the volume of emergency events, defned as the dispatch of the most appropriate transport until the rescue is completed and/or the patient is referred to the most suitable hospital facilities. Planning emergency transportation dispatches is the most crucial organizational efort from a managerial and planning perspective. While most of the literature on forecasting models in EMS has focused on predicting emergency call volumes, trends in emergency call volumes do not always align with changes in actual emergency events, which are the ultimate organizational targets. In Lombardy, approximately half of the emergency calls are not forwarded to the second-level public safety access point because they are deemed non-urgent upon initial assessment (AREU [2022\)](#page-22-5). Various factors, such as media communications and social alerts, infuence the proportion of calls that do not require emergency services. For example, immediately after the frst COVID-19 case was confrmed in Italy, an unprecedented increase in emergency calls was observed in Lombardy. Many of these calls were requests for information and recommendations about the new disease (Marrazzo et al. [2020;](#page-23-13) Dattner et al. [2022](#page-23-14); Molenberghs [2023](#page-23-15)).

The fact that our study aims to predict the number of future emergency events is a strength. Specifcally, having a reliable model to forecast such events allows the central direction unit to activate additional ambulances and increase the number of emergency teams on shift. As reported by AREU, the organization in charge of EMS in Lombardy, implementing such actions requires at least 24 hours. This designated time frame allows sufficient flexibility to adjust the number of ambulances. It ensures efective planning and response to potential emergencies, maintaining an optimal balance of resources and providing timely medical assistance to those in need (Berchi et al. [2010](#page-23-16); Gilardi et al. [2021\)](#page-23-17). Therefore, we considered predicting events one day in advance as the shortest forecasting time frame. In addition, since that data is updated hourly, the proposed model allows for considering shorter prediction intervals if deemed necessary. The model presented in this paper has been implemented into user-friendly software. Following the initial testing phase reported here, the software has been successfully used by AREU for several months.

The paper is structured as follows. Subsec. [2.1](#page-2-0) describes the Lombardy EMS, which is the target of our research. The data sources utilized in the model development are outlined in Subsec. [2.2](#page-3-0). The model development process is described in Subsec. [2.3](#page-4-0), while Sect. [3](#page-11-0) presents the estimates and predictive performance of the model. In Sect. [4](#page-16-0), we discuss the strengths and limitations of our study.

2 Methods

2.1 EMS organization in Lombardy

Lombardy has a population of 10 million, the most populous region In Italy, accounting for approximately 17% of the Italian people. Before the COVID-19 pandemic, the regional EMS received around 1 million emergency calls annually,

Fig. 1 Description of the AREU organizational structures: **a** four SOREUs: AREU emergency management; **b** twelve ATTs: AREU management of territorial resources

corresponding to over 900,000 emergency events. AREU, the public agency responsible for coordinating, guiding, managing, and monitoring the out-of-hospital emergency network and emergency number service in Lombardy, oversees these operations. The agency is structured into peripheral units known as Territorial Business Units (AAT, *Articolazioni Aziendali Territoriali*) as well as Regional Emergency Operations Rooms (SOREU, *Sale Operative Regionali dell'Emergenza Urgenza*). The twelve AATs are distributed throughout the region, approximately following the provincial division, while the four SOREUs coordinate rescue operations in superprovincial competence areas (i.e., AAT aggregations). The geographical position and organization of the SOREUs and the distribution of the AATs are depicted in Fig. [1](#page-3-1).

2.2 Data

A comprehensive set of variables pertaining to emergency events in Lombardy from January 1st, 2015, until May 9th, 2021 were considered potential predictors for model development. We focused on predictors that are continuously available to AREU, enabling decision-makers to efectively utilize the predictive models for short-term forecasting (Kenett and Gotwalt [2022](#page-23-9)). A total of 134 variables were collected from various data sources: the AREU databases for emergency response data; the Regional Agency for Environmental Protection (ARPA) registry for weather data; the Department of Civil Protection repository for COVID-19 data; the Higher Institute of Health (ISS) estimates for other epidemiological information.

The AREU database contains information about all received calls: the SOREU receiving the call, the exact time of the call (i.e., date and hour/minutes), the call classifcation (e.g., frst aid), the AREU administrative area (i.e., province, zone, AAT), call initiation location (e.g., home, street) with geographic coordinates, the reason for the call, the severity code (i.e., triage), and whether the call triggered an aid response, resulting in an event. The data are aggregated at an hourly level.

Weather data from ARPA data are obtained through the Open Data project (ARPA - Regione Lombardia [2014](#page-22-6)), which collects temperature, rainfall, and snowfall data from sensors distributed across the Lombardy region. For each AAT, central sensors in the city center are selected, and the weighted average is computed at the SOREU level. The weights equal the proportion of calls (from January 1st, 2015 until May 9th, 2021) received from each province in the SOREU. The weather data are available at an hourly level but were aggregated at the daily level for our analyses, using indicators such as the daily average or the diference between the maximum and minimum temperature of the day.

COVID-19 data from the Department of Civil Protection are obtained from Dipartimento della Protezione Civile ([2020](#page-23-18)). The data cover the Lombardy region, except for the total number of positive cases reported at the province level. The data are available daily. In addition to the basic epidemiological information, we compute the efective reproduction number (Rodpothong and Auewarakul [2012](#page-24-2); Dabbaghian and Mago [2014](#page-23-19)) using the method employed by the ISS, available at Istituto Superiore di Sanità [\(2020\)](#page-23-20).

Finally, we consider the weekly fu incidence at the national level from 2015 to 2021 as communicated by ISS (Istituto Superiore di Sanità [2020\)](#page-23-20).

2.3 Model development

Let *Y* be a random vector of dimension $T \times 1$, with its components Y_t representing the counts of events at time $t \in \mathcal{T}, \mathcal{T} := \{1, \ldots, T\}$. In our study, the time index t is on the hourly scale, and the spatial aggregation unit was the SOREU. Therefore, we targeted the prediction of the number of emergency events for each hour of the day in each of the four SOREUs. Let $\mathbf{X} = (X_1, \dots, X_K)$ be a set of *T*-dimensional covariates associated with the response variable *Y*, indexed by $k \in \mathcal{K}, \mathcal{K} := \{1, ..., K\}$. Covariates can be year-, month- or day-specifc and can be lags of *Y*, such as the total number of events in the previous days.

Given the important territorial and urban diferences of the SOREUs, characterized by extremely diferent orographic characteristics and distributions of metropolitan and rural areas, we developed separate models for each area.

We opted for a GAM model to capture nonlinear relationships between *X* and *Y* with smoothing splines (Wood [2004](#page-24-3), [2011](#page-24-4), [2017\)](#page-24-5). Since the response was a count variable and preliminary exploratory data analyses showed evidence of over-dispersion (Agresti [2015](#page-22-3)), we assumed a negative binomial distribution (Casella and Berger [1990](#page-23-21)) for the response. Specifically, we assumed *Y_t* ∼ $\mathcal{NB}(r_t, \pi)$, where *t* ∈ \mathcal{T} , with $E(Y_t) = \mu_t = \frac{r_t \pi}{1 - \pi}$ and $V(Y_t) = \mu_t + \frac{\mu_t^2}{\pi}$. The expected value μ_t of Y_t is assumed to depend on the covariates as follows:

$$
\ln(\mu_t) = \alpha + \sum_{k=1}^K f_k(X_{tk}),
$$
 where $f_k(X_{tk}) = \sum_{d=1}^{D_k} \beta_{kd} b_{kd}(X_{tk}).$

Here, the coefficients β_{kd} are the unknown parameters to be estimated, while $b_{kd}(\cdot)$ are known basis functions, and D_k is the number of bases for the covariate X_{ik} .

Model	Covariates				
Model 1	Hour of the day when the event occurs at SOREU level. \star				
	Day of the week when the event occurs at SOREU level. \star				
	Interaction between the hour of the day and the day of the week. \star				
	Quarter of the year when the event occurs at SOREU level. \star				
	Daily average temperature lagged one day at the SOREU level				
	Number of events of the day before delayed 1/2/3 h at SOREU level				
	Number of events aggregated by day and delayed 1/2/7 days at SOREU level				
	Weekly flu incidence lagged one day at the national level				
	COVID-19 reproduction number based on the total amount of positive cases				
	lagged one day at Lombardy level				
Model 2	Hour of the day when the event occurs at the SOREU level				
	Day of the week when the event occurs at the SOREU level				
	Interaction between the hour of the day and the day of the week				
	Month of the year when the event occurs at the SOREU level. \star				
	Daily difference between the minimum and maximum temperature \star				
	lagged one day at the SOREU level				
	Number of events of the day before delayed 1/2/3/4 h at SOREU level				
	Number of events aggregated by day and delayed 1/7/14 days at SOREU level				
	Weekly flu incidence lagged one day at the national level				
	COVID-19 reproduction number based on the total amount of hospitalized patients				
	lagged one day at Lombardy level				
Model 3	Hour of the day when the event occurs at the SOREU level. \star				
	Variable indicating if the day when the event occurs at SOREU level				
	is during the weekend or a working day				
	Quarter of the year when the event occurs at the SOREU level. \star				
	Week of the year when the event occurs at the SOREU level. \star				
	Daily difference temperature with respect to 16° C lagged one day at the SOREU level				
	Number of events of the day before delayed 1/2/3 h at SOREU level				
	Number of events aggregated by day and delayed 1/2/7 days at SOREU level				
	Weekly flu incidence lagged one day at the national level				
	Number of hospitalized patients lagged one day at Lombardy level				
Model 4	Hour of the day when the event occurs at the SOREU level				
	Variable indicating if the day when the event occurs at SOREU level				
	is during the weekend or a working day				
	Interaction between the hour of the day and working days/weekend dummy variable				
	Month of the year when the event occurs at the SOREU level. \star				
	Daily average temperature lagged one day at the SOREU level. \star				
	Daily average precipitation lagged one day at the SOREU level. \star				
	Number of events of the day before delayed 1/2/3 h at SOREU level				
	Number of events aggregated by day and delayed 1/2/7/14 days at SOREU level				
	Weekly flu incidence lagged one day at the national level				
	Number of intensive care admissions lagged one day at Lombardy level				

Table 1 Description of the fve models considered in the cross-validation step

Model	Covariates			
Model 5	Hour of the day when the event occurs at the SOREU level. \star			
	Dummy variable describing the exceptional days, like 1st of January			
	when there are events that cause an increase in calls			
	Dummy variable describing the calendar school			
	Daily average temperature lagged one day at the SOREU level. \star			
	Daily average precipitation lagged one day at the SOREU level			
	Number of events of the day before delayed 1/2/5 h at SOREU level			
	Number of events aggregated by day and delayed 1/2/7/14 days at SOREU level			
	Weekly flu incidence lagged one day at the national level			
	Number of daily total positive cases at the province level lagged 5 days			
	The sum is computed to have the variables at the level of SOREU			

Table 1 (continued)

The *⋆* symbol expresses if the corresponding variable enters by a spline function

Table 2 MAPE from fve diferent models described in Table [1](#page-5-0) calculated across diferent time periods (30 days) considering respectively one, two, fve, and seven days ahead predictions for the *Plain* SOREU

We had to perform variable selection to fnd the optimal model to predict the number of events in each SOREU. The variable selection process was based on the data from the *Plain* SOREU, the second largest SOREU. We did not use the *Metropolitan* SOREU, which is the largest among the four, because AREU already had a predictive model for this area, and the development of a model for the remaining SOREU was their priority.

Given the large number of available explanatory variables (i.e., 134), we relied on assumptions a priori, based on the existing literature, about their efects on the count of events and their possible interactions. We assumed the presence of a time efect at the annual, weekly, and daily levels. In addition, we assumed an efect of weather (Attia and Edward [1998](#page-22-1); Noble et al. [1971\)](#page-23-2), epidemiological (Diaz et al. [2001\)](#page-23-5) and auto-regressive factors (Kedem and Fokianos [2002\)](#page-23-11). We constructed several sets of covariates to explain seasonal, weather, epidemiological, and auto-regressive efects with the available variables. For example, we explored whether the seasonal efect was better modeled at the month or quarter levels. In the frst case, the variable "month" was entered into the model, while in the second case, we entered the variable "quarter". Similarly, the meteorological impact was analyzed by considering the average daily temperature and the diference between the daily minimum and maximum temperature. Again, the impact of the COVID-19 spread was analyzed through the number of hospitalized patients with symptoms and the number of positive swabs. These are just a few examples of the combinations analyzed in this variable selection process.

Fig. 2 *Plain* model **results**: coefficients plots during the COVID-19 pandemic, **a** Effect of the hour of the day; **b** Efect of the day of the week, where 1 stands for Monday; **c** Efect of the quarters of the year, where 1 stands for the first quarter of the year; **d** Effect of the interaction between days and hours, where 1 stands for Monday. The black dotted lines represent two standard error bounds

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After that, we analyzed this set of covariates through exploratory analysis to understand the underlying relationships between the dependent variable (i.e., count of events) and covariates and among the covariates themselves. We fnally selected fve models with diferent sets of covariates **X** cross-validated across diferent time periods. Table [1](#page-5-0) briefy describes the set of variables inserted in these fve fnal models. Some of them are considered categorical variables in some models, and others as continuous variables inside a spline function. The *⋆* symbol in Table [1](#page-5-0) expresses if the ordinal variable is considered a continuous variable inside a spline function.

The observations in time–series data are temporally dependent, which means that traditional cross-validation procedures do not apply directly. To tackle this issue, a rolling cross-validation approach suitable for temporal data was preferred. Particularly, the candidate models were fitted to data Y_1, \ldots, Y_t , forecasts \hat{Y}_{t+1} were obtained, and the relative prediction errors $E_t = \frac{\hat{Y}_{t+1} - Y_{t+1}}{Y_{t+1}}$ $\frac{Y_{t+1}}{Y_{t+1}}$ were calculated for each model. This was repeated for $t = m, \ldots, m + N - 1$, where *m* corresponds to the minimum size of the dataset used to ft the models and *N* is the number of forecasts. The mean absolute percentage error (MAPE) for each model, computed across *N* forecasts, was used as a performance metric in the cross-validation step:

Fig. 3 *Plain* model **results**: coefficients plots using data before the COVID-19 pandemic, **a** Effect of the hour of the day; **b** Efect of the day of the week, where 1 stands for Monday; **c** Efect of the quarters of the year, where 1 indicates the frst quarter of the year; **d** Efect of the interaction between days and hours, where 1 stands for Monday. The black dotted lines represent two standard error bounds

$$
MAPE = \frac{\sum_{i=1}^{N} |E_i|}{N} 100,
$$
\n(1)

where $|\cdot|$ is the absolute value, and E_i is the relative prediction error from forecast *i*, $i = 1, \ldots, N$. The choice of the relative prediction error for assessing forecasting performance was based on matching the performance measure used by AREU. However, the user-friendly software where the fnal model is implemented also reports other performance metrics, such as the minimum absolute percentage error, the maximum absolute percentage error, and the median absolute percentage error.

Table [2](#page-6-0) shows the MAPE considering the fve diferent models described in Table [1](#page-5-0) cross-validated on a rolling basis across diferent time periods for the *Plain* SOREU. The MAPE is computed across 30 days considering one, two, fve, and seven days ahead predictions in 2016, 2018, and 2020. Therefore, for each year, 30 days were randomly selected. Then, in the frst step, the training set is composed of the period before the frst day of the 30 days randomly selected. The test set comprises the frst, second, ffth, and seventh days of the 30 days selected to have predictions one, two, fve, and seven days ahead. In the second step, the frst day of the 30 days randomly selected is added to the training set, the remaining 29 days are used as a test set, and so on. Model 1 has the lowest cross-validated MAPE overall compared to the other four models.

The predictive performance of the developed models was compared to that of other alternative approaches. The frst comparator was the model used by AREU for the *Metropolitan* SOREU, which was based on an unobserved component time series model (Harvey [1990](#page-23-8)). The model included several covariates such as a dichotomous variable for increased calls (e.g., snowfall), a dichotomous variable for decreased calls (e.g., midweek holiday), predicted average daily temperature, fu incidence value (estimated), and the square of the diference between the average daily temperature and a reference temperature (16◦ C). The model also considered stochastic seasonality at the weekly level. The developed model was also compared

Fig. 4 *Plain* **model results**: Quantiles at level 0.8 (black) and 0.99 (light green) considering the predicted events at hourly level one day ahead. The red dotted line shows the maximum quantile at level 0.8 (0.99) corresponding to 23 (29) events expected on March 29, 2021

Fig. 5 *Plain* **model results**: **a** Predictions one, two, fve, and seven days ahead across one year and relative true values; **b** Forecast errors one day ahead, the predictions inside the two red dotted horizontal lines have absolute errors below 5%. The black dotted line represents an absolute error equals 0

Fig. 6 *Metropolitan* **model results**: **a** Predictions one, two, fve, and seven days ahead across one year and relative true values; **b** Forecast errors one day ahead, the predictions inside the two red dotted horizontal lines have absolute errors below 5%. The black dotted line represents an absolute error equals 0

to other benchmarking models estimated on the same training data. These included a naive, deterministic model where predictions were simply set to the latest available observation, an ARIMA model based on the time series of previous events (Makridakis and Hibon [1997](#page-23-22)), and a generalized linear model (GLM) for count time series (Christou and Fokianos [2014\)](#page-23-23).

We use the open-source statistical software R (R Core Team [2015](#page-24-6)) for preprocessing and model ftting. Among the available R packages for ftting GAMs, we utilized the mgcv (Wood [2011\)](#page-24-4) package, which enables the fitting of GAMs on large datasets through the bam function. The ARIMA and GLM benchmarking models were fitted using the auto.arima R function and the $tsqlm$ function from tscount package (Liboschik et al. [2017](#page-23-24)), respectively. The full code used in this paper is available at https://github.com/angeella/Tsunami_project.

Fig. 7 *Lakes* **model results**: **a** Predictions one, two, fve, and seven days ahead across one year and relative true values; **b** Forecast errors one day ahead, the predictions inside the two black dotted horizontal lines have absolute errors below 5%. The black dotted line represents an absolute error equals 0

Fig. 8 *Alps* **model results**: **a** Predictions one, two, fve, and seven days ahead across one year and relative true values; **b** Forecast errors one day ahead, the predictions inside the two black dotted horizontal lines have absolute errors below 5%. The black dotted line represents an absolute error equals 0

3 Results

3.1 Model estimates

This section will focus on presenting the model developed specifcally for the *Plain* SOREU, which was used for variable selection. The covariates included in the optimal model are described in the frst model of Table [1](#page-5-0).

We employed cubic regression splines (Green and Silverman [2019](#page-23-25)) to capture the seasonal effects of hours and quarters. The cubic splines were chosen because they match up to the second derivative with their start, which is suitable for modeling cyclical efects. Specifcally, we used 24 basis functions for modeling the seasonal effects of hours and 4 basis functions for modeling the seasonal effects of quarters.

Fig. 9 *Metropolitan* **model results**: Predictions one day ahead across 145 days and relative true values

For the day variable, we opted for P-splines with 7 basis functions (Eilers and Marx [1996\)](#page-23-26) to capture the day's seasonal effects. Finally, the tensor product smooth (Ramsay et al. [1997\)](#page-24-7) (two-dimensional smooth, where the shape of one dimension varies smoothly over the other dimension) between day and hour covariates is applied to analyze the interaction between these two variables. Linear associations were assumed for the remaining covariates, which were included in the model without any smoothing terms. P-splines performed similarly to cubic regression splines but are numerically more stable and easier to ft. In addition, this permits a fast estimate of the smooth tensor product. The time complexity of the model ftting is essential in this case since AREU needs a computationally fast model to forecast the number of emergency events (Kenett and Gotwalt [2022](#page-23-9)).

For each covariate, we analyze the estimated association with the outcome. Figure [2](#page-7-0)a illustrates the estimated seasonal efects of hours within a day. We observe a positive efect during the late morning and afternoon when people are typically awake and active. In contrast, the efect becomes negative during the night and early morning when people are usually asleep. Figure [2](#page-7-0)b displays the effects of the day of the week. Mondays show the highest incidence of events compared to the other days of the week. Figure [2c](#page-7-0) presents the seasonal efects of quarters. The number of events is generally lower in the summer when the schools are closed, and people are on vacation. This observation may be associated with rising temperatures during that period. Finally, looking at the interaction between hours and days in Fig. [2d](#page-7-0), we can see a positive efect in the morning (9 a.m.–12 p.m.) of weekdays and a strong negative efect in the morning of the weekend. Furthermore, we can see a positive efect during the night on the weekend and a negative efect around 5 a.m. on Monday, Tuesday, and Wednesday.

We estimate the model considering data before the COVID-19 era to see if the temporal dynamics, particularly the seasonal efects, have also changed due to the pandemic. Figure 3 shows the same plots presented in Fig. [2](#page-7-0). We can see that the efect of the hour of the day (Fig. [3a](#page-8-0)) and of the quarter (Fig. [3](#page-8-0)d) do not change markedly, unlike the efect of the day of the week (Fig. [3b](#page-8-0)). One possible

Fig. 10 Screenshot of one of the many user-friendly interfaces that make the proposed model fully operational on a daily basis to support the decisions by AREU

interpretation could be that before the COVID-19 pandemic, many emergency events were concentrated during the weekend. Therefore, with the arrival of the COVID-19 pandemic, the emergencies referred to AREU have shifted by a few days. People become infected during the week and weekend and seek care on Monday. Before the COVID-19 pandemic, on the other hand, the primary demand, as we have said, was at weekends, when people went out to parties/hiking or when general practitioners were simply not available. Furthermore, Fig. [3d](#page-8-0) shows a positive efect on early mornings during all weeks and a night effect during the weekend. Again, before the COVID-19 pandemic, people most needed AREU interventions during weeknights and weekends.

Finally, we report the quantiles at levels 0.8 and 0.99 of the predictive distribution considering hourly predictions one day ahead. Figure [4](#page-9-0) shows these quantiles for each day from May, 9th, 2020 until May, 9th, 2021. Knowing the quantiles of predicted values can help AREU with resource planning and making informed emergency management decisions as a risk measure. For example, AREU knows that there is 80% probability that on March, 29th 2021, the hourly events will be at most 23 (and 29 at most with probability 99%), represented by the red dotted line in Fig. [4](#page-9-0). In other words, 23 (29) represents the cut-off point such that only 20% (1%) of the predicted emergency events exceed this value.

3.2 Model performance

We frst focus on the model's performance developed for the *Plain* SOREU. For each date from May, 9th, 2020 until May, 9th, 2021, the model described in the previous section was ftted on one year of retrospective data. The resulting model was used to forecast the number of events one, two, fve, and seven days ahead. Figure [5a](#page-10-0) compares the predictions one, two, fve, and seven days ahead with the true number of emergency events, while Fig. [5b](#page-10-0) shows the forecast errors for the one day ahead

Fig. 11 *Metropolitan* model results: coefficients plots during the COVID-19 pandemic, a Effect of the hour of the day; **b** Efect of the day of the week, where 1 stands for Monday; **c** Efect of the quarters of the year, where 1 stands for the frst quarter of the year; **d** Efect of the interaction between days and hours, where 1 stands for Monday. The black dotted lines represent two standard error bounds

prediction. The periods where the error appears to be slightly larger are during the second pandemic wave (November-February 2021) and around the holiday season. In general, the mean absolute percentage error over the whole year was 4.53%. This is a good result, considering that AREU required the mean absolute percentage error to be at most 5% for the predictions to be helpful in efficiently planning future activities. Appendix [2](#page-21-0) shows the MAPE values grouped by month and year to have a better view of Fig. [5.](#page-10-0)

The model selected for the *Plain* SOREU data was then applied to the data of the other three SOREUs. The one day ahead mean absolute percentage error was still acceptable for the *Alps* (6.241%), *Lakes* (5.815%), and *Metropolitan* (4.309%) SOREUs. Figure [6a](#page-10-1) shows the predictions one, two, fve, and seven days ahead for the *Metropolitan* SOREU, while Fig. [6](#page-10-1)b describes the prediction errors for the one day ahead forecast. Similarly, Fig. [7a](#page-11-1) and b illustrate the results for the *Lakes* SOREU, and Fig. [8a](#page-11-2) and b for the *Alps* SOREU. As the *Plain* case, Appendix [2](#page-21-0) reports the MAPE values considering all SOREUs grouped by month and year. The

Fig. 12 *Metropolitan* model results: coefficients plots before the COVID-19 pandemic, a Effect of the hour of the day; **b** Efect of the day of the week, where 1 stands for Monday; **c** Efect of the quarters of the year, where 1 stands for the frst quarter of the year; **d** Efect of the interaction between days and hours, where 1 stands for Monday. The black dotted lines represent two standard error bounds

changes in the efects after ftting the model to pre and post-COVID data for the *Metropolitan*, *Lakes* and *Alps* SOREUs are reported in Appendix [1.](#page-20-0)

Figure [9](#page-12-0) compares the one day ahead predictions obtained with the proposed model to the predictions of the model currently used by AREU on the *Metropolitan* SOREU, which was the only SOREU for which the AREU model was calibrated. The predictions are compared across 145 days (i.e., from 2020–10-14 until 2021–03- 07). We observed a signifcant improvement: our model achieved a MAPE of 4.44% whereas the AREU model achieved a MAPE of 5.11%. Therefore, the developed GAM showed a signifcantly lower error than the unobserved component time series model used by AREU.

Regarding the other benchmarking models, when looking at the one day ahead predictions over one year, the naive deterministic, ARIMA and model and tsglm models achieved a MAPE of 7.359%, 11.177% and 10.461% respectively. Thus, the proposed model outperformed all of the considered benchmark models.

To test the fexibility of the proposed model, we trained it using data from the pre-COVID-19 period only, spanning from December 31, 2017, to December 31, 2018. Considering the *Plain* SOREU, we obtained MAPE values (calculated from

Fig. 13 Lakes model results: coefficients plots during the COVID-19 pandemic, a Effect of the hour of the day; **b** Efect of the day of the week, where 1 stands for Monday; **c** Efect of the quarters of the year, where 1 stands for the first quarter of the year; **d** Effect of the interaction between days and hours, where 1 stands for Monday. The black dotted lines represent two standard error bounds

December 31, 2017, to December 31, 2018): 4.093 for one day ahead, 4.341 for two days ahead, 4.391 for five days ahead and 4.465 for seven days ahead. The results for the other SOREUs are provided in Appendix [2.](#page-21-0) The proposed model demonstrates its ability to capture the dynamic changes in epidemiological and societal circumstances thanks to the incorporation of selected covariates such as the efective reproduction number (Rodpothong and Auewarakul [2012;](#page-24-2) Dabbaghian and Mago [2014](#page-23-19))), as well as the adaptability of the splines in handling variations in the number of emergency events across diferent periods.

4 Discussion

We have described the development of a statistical model developed with state-ofthe-art techniques to predict emergency events in the most populous Italian region. Because the forecasting errors were compatible with the organizational needs of AREU, the model is a valuable tool for efficiently planning emergency activities.

Fig. 14 *Lakes* model results: coefficients plots before the COVID-19 pandemic, a Effect of the hour of the day; **b** Efect of the day of the week, where 1 stands for Monday; **c** Efect of the quarters of the year, where 1 stands for the first quarter of the year; **d** Effect of the interaction between days and hours, where 1 stands for Monday. The black dotted lines represent two standard error bounds

A user-friendly dashboard providing the model estimates was implemented to make this model available to decision-makers in AREU, enabling the use of the model in everyday EMS coordination. Such an application is represented in Fig. [10.](#page-13-0)

Due to the diferent organization schemes of EMS around the globe, generalizing models predicting emergency events or calls to other contexts is often complex and, in some cases, impossible. However, the general methodology applied in this study and the overall model development process can also be used in other settings. Additionally, we found that our model performed very well on all of the SOREUs in Lombardy, even though the variables were selected based on the *Plain* SOREU data only. This suggests that the form of the model may generalize to slightly diferent contexts, such as other Italian regions or other European countries. This possibility is already under consideration by AREU decision-makers.

Our study focused on the GAM methodology for model development. Further research should evaluate the application of generalized additive mixed models (GAMMs), i.e., extensions of GAM incorporating random efects. GAMMs are better suited to deal with autocorrelation structures at a price, however, of higher

Fig. 15 *Alps* model results: coefficients plots during the COVID-19 pandemic, a Effect of the hour of the day; **b** Efect of the day of the week, where 1 stands for Monday; **c** Efect of the quarters of the year, where 1 stands for the first quarter of the year; **d** Effect of the interaction between days and hours, where 1 stands for Monday. The black dotted lines represent two standard error bounds

computational costs (Lin and Zhang [1999](#page-23-27)). In addition, further analyses should explore the possible addition of interaction terms. Bayesian extensions could also be explored. Such models could be used to model trend and seasonal components with appropriate Markov random feld priors with diferent forms and degrees of smoothness (Fahrmeir and Lang [2001](#page-23-28)). Finally, considering additional epidemiological variables, especially those related to COVID-19 or other emerging health crises, could be valuable and appropriate.

The proposed model was able to capture the dramatic daily and seasonal variations that emerged during the COVID-19 pandemic, attaining good performances both during one of the peaks of the COVID-19 epidemic in Lombardy and in moments when the volume of cases was limited. Nonetheless, we emphasize how predictive models like the one we presented need periodic, rigorous, quality evaluations and, eventually, substantial updates. This is particularly true in the COVID-19 era, when the rapidly increasing proportion of vaccinated individuals and the sudden spread of new viral variants may change the efect of

Fig. 16 *Alps* model results: coefficients plots before the COVID-19 pandemic, a Effect of the hour of the day; **b** Efect of the day of the week, where 1 stands for Monday; **c** Efect of the quarters of the year, where 1 stands for the first quarter of the year; **d** Effect of the interaction between days and hours, where 1 stands for Monday. The black dotted lines represent two standard error bounds

COVID-19-related predictors in the model. Even beyond COVID-19 factors, structural and organizational modifcations in the EMS apparatus may heavily impact the role of the predictors in the model. For these reasons, strict, continuous collaboration between public health stakeholders and data analysts is deemed essential.

Month	Year	MAPE				
		One day ahead	Two days ahead	Five days ahead	Seven days ahead	
5	2021	3.428	3.388	3.903	2.942	
$\overline{4}$	2021	3.851	4.088	4.409	4.834	
3	2021	4.690	4.450	5.265	5.709	
$\overline{2}$	2021	5.958	6.214	6.882	6.201	
$\mathbf{1}$	2021	4.292	5.275	4.258	5.540	
12	2020	6.078	7.037	6.095	5.581	
11	2020	4.861	5.056	5.626	6.023	
10	2020	4.373	4.161	4.263	4.250	
9	2020	3.431	3.347	4.026	3.870	
8	2020	6.882	7.311	6.836	6.546	
7	2020	4.853	5.049	5.640	9.994	
6	2020	4.897	5.821	6.475	5.943	
5	2020	5.007	7.422	5.859	5.483	

Table 4 *Plain* **model results**: One, two, fve, and seven days ahead MAPE for the *Plan* SOREU grouped by month and year

Table 5 *Metropolitan* **model results**: One, two, fve, and seven days ahead MAPE for the *Metropolitan* SOREU grouped by month and year

Month	Year	MAPE				
		One day ahead	Two days ahead	Five days ahead	Seven days ahead	
5	2021	3.782	5.121	6.613	6.181	
$\overline{4}$	2021	4.033	4.326	5.915	6.492	
3	2021	3.630	4.085	4.344	4.701	
$\overline{2}$	2021	3.408	4.330	4.186	4.624	
1	2021	5.490	5.838	6.346	7.173	
12	2020	5.773	5.523	6.015	5.510	
11	2020	4.533	5.360	7.753	9.697	
10	2020	3.857	4.381	4.972	6.356	
9	2020	4.403	9.118	6.980	7.959	
8	2020	4.559	6.223	7.297	14.282	
7	2020	5.181	6.362	4.173	4.484	
6	2020	4.664	5.484	5.230	4.909	
5	2020	4.786	4.374	6.453	6.586	

Appendix 1: Model estimates

We show here the plots of the component smooth functions for *Metropolitan* (Figs. [11](#page-14-0) and [12\)](#page-15-0), *Lakes* (Figs. [13](#page-16-1) and [14](#page-17-0)) and *Alps* (Figs. [15](#page-18-0) and [16](#page-19-0)) SOREUs using the entire dataset and data pre-COVID pandemic era.

Month	Year	MAPE				
		One day ahead	Two days ahead	Five days ahead	Seven days ahead	
5	2021	5.167	5.356	4.167	5.019	
$\overline{4}$	2021	7.385	7.547	7.499	7.919	
3	2021	5.941	6.275	6.993	6.701	
$\overline{2}$	2021	4.677	5.397	5.870	6.423	
$\mathbf{1}$	2021	5.801	5.648	5.835	5.881	
12	2020	6.254	5.786	5.992	6.157	
11	2020	7.585	7.379	7.031	7.300	
10	2020	6.154	6.084	5.968	6.095	
9	2020	5.184	5.978	6.983	7.325	
8	2020	8.265	10.084	13.004	14.502	
7	2020	4.686	4.787	5.013	5.061	
6	2020	5.754	6.267	5.647	5.788	
5	2020	8.134	8.489	10.961	11.182	

Table 6 *Alps* **model results**: One, two, fve, and seven days ahead MAPE for the *Alps* SOREU grouped by month and year

Table 7 *Lakes* **model results**: One, two, fve, and seven days ahead MAPE for the *Lakes* SOREU grouped by month and year

Month	Year	MAPE				
		One day ahead	Two days ahead	Five days ahead	Seven days ahead	
5	2021	3.333	4.570	6.064	4.471	
$\overline{4}$	2021	5.808	6.17	6.020	6.311	
3	2021	5.447	6.175	5.697	6.091	
$\mathfrak{2}$	2021	6.044	5.727	5.704	7.038	
1	2021	6.368	6.735	6.198	7.259	
12	2020	6.769	6.877	7.771	9.065	
11	2020	6.189	7.067	11.571	14.247	
10	2020	4.798	6.851	6.869	6.855	
9	2020	4.883	5.116	6.515	6.405	
8	2020	6.313	5.237	6.811	7.773	
7	2020	5.391	7.310	5.162	5.470	
6	2020	6.511	5.749	6.817	7.493	
5	2020	5.401	6.701	7.522	7.553	

Appendix 2: Model performance

Table [3](#page-19-1) shows the MAPE computed during the pre-COVID-19 period (i.e., from 2017–12-31 to 2018–12-31) concerning one, two, fve, and seven days ahead predictions of events volume for the SOREUs *Metropolitan*, *Alps* and *Lakes*.

Tables [4](#page-20-1), [5,](#page-20-2) [6](#page-21-1) and [7](#page-21-2) show the one, two, fve, and seven days ahead MAPE values for the *Plain*, *Metropolitan*, *Lakes* and *Alps* SOREUs respectively grouped by month and year. The time period considered is the one represented in Figs. [5,](#page-10-0) [6,](#page-10-1) [7](#page-11-1) and [8](#page-11-2).

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Declarations

Confict of interest The authors declare no competing interests.

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