

<sup>1</sup> **Multi–decadal dynamics of alternate bars in the**  
<sup>2</sup> **Alpine Rhine River**

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3 **Abstract.** We report on a multi-decadal analysis of alternate bar dynam-  
4 ics in a 41.7 km reach of the Alpine Rhine River, which represents an almost  
5 unique example of a regulated river with fixed levees, straight reaches and  
6 regular bends in which alternate gravel bars spontaneously formed and mi-  
7 grated for more than a century. The analysis is based on freely available Land-  
8 sat imagery, which provided an accurate and frequent survey of the dynam-  
9 ics of the alternate bar configuration since 1984. Bars were characterized in  
10 terms of wavelength, migration, and height. Longitudinal and temporal pat-  
11 terns are investigated as a function of flood occurrence and magnitude and  
12 in relation to the presence of local planform discontinuities (bends and ramps)  
13 that may affect their dynamics. Bars in the upper part of the reach are mostly  
14 steady and relatively long (about 13 channel widths); bars in the lower part  
15 of the reach are migrating and shorter (about 9 channel widths). Bar height  
16 is rather uniform along the reach, ranging between 3 to 4 m. The temporally  
17 long hydrological dataset allowed the investigation of bar migration during  
18 flood events, showing that bars migrate faster for intermediate floods. The  
19 observed relationship between bar migration and wavelength was consistent  
20 with linear theories for free migrating and steady forced bars in straight chan-  
21 nels. The comparison of theories with observations highlights the key role  
22 of theories to support interpretation of observations, for a better understand-  
23 ing of the morphodynamic processes controlling bar formation and dynam-  
24 ics.

## 1. Introduction

25 Alternate bars have been documented in channelized river reaches for nearly 3 centuries  
26 (e.g. *Engels* [1914], *Werth* [2014]). They emerged as a morphological response of river beds  
27 to levee construction and channel straightening. Their widespread occurrence in wide,  
28 morphologically regulated streams attracted the attention of hydraulic engineers because  
29 of their undesired effects on bridges, embankments, intake structures and river navigation  
30 (*Jäggi* [1984]). Moreover, regular periodic oscillations that alternate bars impose to the  
31 flow in a straight channel initially provided an intriguing (though lately questioned) pos-  
32 sible explanation for the origin of river meandering, (*Lewin* [1976], *Parker* [1976]), thus  
33 stimulating the interest of fluvial geomorphologists.

34 In the 1960s, a consistent research effort to understand causes and controls on bar forma-  
35 tion, their geometrical properties (length, magnitude of scours and deposits), and migra-  
36 tion was undertaken, through complementary approaches, mainly including mathematical  
37 and physical scale modeling. A remarkable bias towards modeling approaches is evident in  
38 the alternate bars literature, with limited availability of field observations until recently.  
39 This was mainly because of the relatively long temporal and spatial scales needed to  
40 properly describe their dynamics (e.g., *Eekhout et al.* [2013]). Such bias limits our present  
41 understanding and ability to predict the morpho-dynamic response of regulated rivers to  
42 hydromorphological pressures, for instance those related to changes in the flow and sedi-  
43 ment supply regime, in levee alignment, and with other river management or restoration  
44 measures.

45 A consistent theoretical framework on alternate bar dynamics, strongly supported by  
46 laboratory observations, has been developed in the past four to five decades (e.g., *Engelund*  
47 *and Hansen* [1967], *Struiksmā et al.* [1985], *Colombini et al.* [1987], *Tubino et al.* [1999],  
48 *Lanzoni* [2000a], *Lanzoni* [2000b], *Crosato et al.* [2011]). However, most of its outcomes  
49 were derived and verified using assumptions such as constant flow discharge, channel  
50 width, and slope; homogeneous sediment size; and indefinitely or semi-indefinitely long  
51 straight channels. The relevance of other neglected factors has not been thoroughly inves-  
52 tigated so far, given the scarcity of observations documenting the morphological properties  
53 of alternate bars in complex (though regulated) rivers. More robust field observations are  
54 therefore of fundamental importance, to assess the possibility of using mathematical theo-  
55 ries as predictors (e.g., *Parker* [1976], *Fredsøe* [1978], *Crosato and Mosselman* [2009])  
56 as well as tools to interpret (e.g., *Rodrigues et al.* [2015]) the expected or observed bar  
57 morphodynamics. Some indications of the potential of bar theories to predict observed  
58 behaviors emerged from recent works (*Eekhout et al.* [2013], *Rodrigues et al.* [2015], *Ja-*  
59 *ballah et al.* [2015]), though these same studies stress the need for continued research that  
60 integrates modeling and field approaches.

61 The observation gap has been increasingly addressed only very recently, thanks to the  
62 development of in-situ monitoring technologies (e.g., flow and bathymetric survey), (*Ro-*  
63 *drigues et al.* [2015]), as well as through remote sensing and the use of satellite imagery  
64 (*Henshaw et al.* [2013]). Table 1 summarizes the main existing field studies with a focus on  
65 alternate bar dynamics. Three studies out of eight (*Welford* [1994]; *Eekhout et al.* [2013];  
66 *Jaballah et al.* [2015]) focused on a reach length of nearly 100 channel widths or more,  
67 allowing the observation of a considerable number of alternate bar units. However, only

68 one of these three (*Jaballah et al.* [2015]) covers a multi-decadal time scale, with the other  
69 two multi-decadal studies referring to reaches with a more limited number of bars (*Church*  
70 *and Rice* [2009], *Ferguson et al.* [2011]). Furthermore, the three multi-decadal analyses  
71 have a relatively poor temporal resolution of surveys, with an average of 1 available survey  
72 every 3 to 5 years.

73 The present paper focuses on a quantitative understanding of long-term dynamics of  
74 alternate bars in the Alpine Rhine River. This is a renowned example of a channelized  
75 stream where an impressively long and regular sequence of alternate bars has been ob-  
76 served for decades (*Jäggi* [1984]). Moreover, it is believed to be one of the few examples  
77 of rivers where migrating alternate bars can be observed (*Crosato and Mosselman* [2009]).

78 The goals of this study were: i) to quantify the morphodynamics of alternate bars in  
79 the Alpine Rhine River, with a particular emphasis on bar migration; ii) to assess to what  
80 extent the predictions of analytical bar theories are consistent with field observations; and  
81 iii) to further explore how theories may help interpret observed alternate bar dynamics.  
82 These goals are achieved by developing and analyzing a dataset of freely available mul-  
83 titemporal Landsat imagery, which combine unprecedented temporal length (3 decades);  
84 spatial length ( $> 400$  channel widths); and temporal resolution ( $\sim 2$  images per year).

## 2. Study site and methods

### 2.1. The Alpine Rhine River

85 The Rhine river is one of the largest rivers in Europe, with a basin of  $1.85 \times 10^6$  km<sup>2</sup> and  
86 a length of 1326 km. The upper part of the basin, between the confluence of Vorderrhein  
87 and Hinterrhein and the lake of Constance, is called Alpine Rhine. This sub-basin is  
88 located in the eastern part of Switzerland, western Austria (the tributary Ill) and the

89 whole territory of Liechtenstein (Figure 1). The Alpine Rhine is 93 km long and its  
90 catchment area is 6123 km<sup>2</sup>.

91 We focused the analysis on a reach that is 41.7 km long and is located between the  
92 Landquart's confluence (km 23.3 of the Alpine Rhine, Landquart's drainage area: 618 km<sup>2</sup>)  
93 and the confluence with the Ill river (km 65.0, Ill's drainage area: 1281 km<sup>2</sup>). No other  
94 relevant tributaries are present along the study reach. The whole reach was heavily  
95 channelized in the 19<sup>th</sup> and 20<sup>th</sup> centuries, with the last levees built in the 1930s and 1940s.  
96 These engineering works aimed at increased flood protection and drastically simplified the  
97 originally dynamic multi-channel morphology. Nowadays, the reach is characterized by a  
98 continuous sequence of alternate bars, which makes the Alpine Rhine the perfect site to  
99 study this morphological pattern.

100 The hydrological regime is pluvio-nival, characterized by snow-melt in spring and sum-  
101 mer and by larger floods most probable in autumn. The river is strongly affected by  
102 hydro-power production, with water release fluctuations superimposed throughout the  
103 year. Hydropeaking increases discharge on average by 70-80 m<sup>3</sup>s<sup>-1</sup>, exhibiting a regular  
104 daily (and weekly) pattern. After 2010, the pattern became more irregular, due to new  
105 rules of the energy production management.

106 There are several available hydrometric stations in this reach. We used the daily data  
107 of the Austrian gauging stations in Bangs, Feldrik, and Lustenau for the period 1951 -  
108 2010, and of the Swiss station in Diepoldsau for the period 1919 - 2012. For this last  
109 station, 10-min data were also available for the period 1984-2013. The average discharge  
110 upstream of the Ill's confluence was 150 m<sup>3</sup>s<sup>-1</sup> (dataset 1996-2010). Minimum flow was  
111 40.3 m<sup>3</sup>s<sup>-1</sup> and maximum recorded flood peak (1988) was 2650 m<sup>3</sup>s<sup>-1</sup> (Figure 2).

112 The cross-section of the channelized reach was designed with a classical trapezoidal  
113 shape, with a base width ( $W$ ) that increases from 85 m in the upstream part up to  
114 106 m downstream. No floodplain is present and the levees (with a transverse slope of  
115 approximately  $35^\circ$ ) are composed of boulders that prevent any planform changes. Bed  
116 material is primarily composed by gravel, with a median grain size ranging between 60 mm  
117 upstream and 20 mm downstream [Hunziker *et al.*, 2001], with local variability caused by  
118 the alternate bars grain sorting. Longitudinal bed slope decreases along the reach, from  
119 2.9 ‰ upstream, to 1.3 ‰ downstream. Though there are no sharp discontinuities in the  
120 streamwise variability of slope and grain size, it is possible to identify three sub-reaches,  
121 each having rather homogeneous values of width, slope and median grain size (Table 2).  
122 Furthermore, we identified the presence of planform and bed elevation discontinuities, in  
123 the form of bends and two unstructured ramps, these latter formed by boulders with a  
124 diameter much larger than the representative diameter of the bed. These ramps artificially  
125 impose a local increase of the longitudinal slope, respectively imposing a change in the  
126 bed elevation of 2.60 m ( $r_1$ ) and 1.40 m ( $r_2$ ). Their location was marked in the vector map  
127 (Figure 1 and Figure 3d), in order to assess their potential impact on bar morphodynamics.

## 2.2. Image database

128 For this study, we used the images acquired by Landsat 4-5 TM (30 m resolution),  
129 Landsat 7 ETM+ and Landsat 8 OLI (15 m resolution of the panchromatic band). The  
130 dataset covers a period of around 30 years, starting from 1984, with a partial interruption  
131 of acquisition between 1991 and 1998. A total number of 58 images out of 78 available  
132 were downloaded and used for this study. Cloud cover and high discharge are the two  
133 main causes of removal of images from the study.

134 Figure 2 shows the temporal sequence of the available images, superimposed to the  
135 discharge record. Emerged gravel bars are visible on the Landsat images only for discharge  
136 values lower than  $350 \text{ m}^3\text{s}^{-1}$ . The full dataset of 78 images covers a discharge range from  
137  $64 \text{ m}^3\text{s}^{-1}$  to  $540 \text{ m}^3\text{s}^{-1}$ . Figure 3a)-c) shows three examples of Landsat images, taken at  
138 different discharges. The mirror alignment problem that affected the Landsat 7 ETM+  
139 sensor after 2003 (and produced the black strips visible in Figure 3b) did not affect our  
140 analysis in a significant way, as it was generally possible to locate the front and tail of  
141 most of the bar units. Furthermore, a more detailed aerial image (Google Maps ©) was  
142 used to accurately define the embankment line and the low flow channel width ( $W$ ).

### 2.3. Bed topography database

143 We used a complete cross-section dataset of the Alpine Rhine surveyed in 2005 by  
144 the International Rhine Regulation (IRR) to determine hydraulic variables of the study  
145 reach. The survey includes more than 200 cross sections with a longitudinal spacing of  
146 approximately 200 m. Mean hydraulic conditions were determined for each of the three  
147 sub-reaches (Table 2).

148 Uniform flow conditions were computed in each cross section, using a log-like formula  
149 for roughness, corresponding to the average sediment size in every sub-reach and the  
150 sub-reach averaged longitudinal slope. The analysis identified: i) the value of discharge  
151 that submerged all the bar deposits (fully wet discharge,  $Q_{FW}$ , equal to an average of  
152  $300 \text{ m}^3\text{s}^{-1}$ ); and ii) the discharge at which the full cross section was expected to actively  
153 transport bed material as bed load (fully transport discharge,  $Q_{FT}$ , equal to an average  
154 of  $650 \text{ m}^3\text{s}^{-1}$ ). Transport conditions were evaluated considering a threshold on the dimen-  
155 sionless bed shear stress equal to 0.03 [*Parker et al.*, 2007]. This choice is independent

156 from the computations of the thresholds values of the bar theory described in the following  
157 paragraphs.

#### 2.4. Monitoring of bar properties

158 The 41.7 km long reach included a series of approximately 40 bar units. Here we define  
159 a bar unit as extending between two consecutive fronts (or tails) on the same side of the  
160 river. Satellite images were imported into Quantum GIS software (*QGIS Development*  
161 *Team* [2009]) and the location of bar fronts and tails was measured in each of the 58  
162 available images, as the most downstream and upstream point of the emerged deposits.  
163 Figure 3d) reports an example of the resulting vector map of the alternate bars. From  
164 this dataset of geographical coordinates, bar wavelength ( $L$ ) and bar migration were  
165 computed. Bar wavelength is defined as the distance between two consecutive fronts (or  
166 tails) on the left (or right) bank (length of the bar unit). Bar migration is the temporal  
167 difference between the location of the front (or tail) of the same bar unit. The high  
168 temporal resolution of the Landsat imagery ensured an easy recognition of the same bars  
169 on the images. A parameter called bar elongation was also computed as the wavelength  
170 difference of the same bar unit between two different Landsat images. Reference Landsat  
171 data for the difference in time are October 22, 1999 ( $Q=149\text{ m}^3\text{s}^{-1}$ ) and July 16, 2010  
172 ( $Q=154\text{ m}^3\text{s}^{-1}$ ).

173 In the case of images acquired with largely different discharge conditions, location of  
174 bar fronts and tails are affected by changes in the exposed area. This implies that the  
175 front (or tail) of the bar may appear to move upstream (or downstream) only because of  
176 a different water level. In order to minimize this effect, we performed a spatial average,  
177 combining fronts and tails results.

178 Free bar theory provides an estimation of the bar amplitude, which is defined for each  
179 bar unit as the difference between the highest and the lowest bed elevation values over  
180 the entire unit. The relatively coarse longitudinal spacing between consecutive cross-  
181 sections in the available topographic survey (200 m) didn't allow an exact computation  
182 of bar amplitude. For this reason, a parameter called "bar height" was computed in the  
183 cross-section dataset as the difference between the lowest and the highest values of bed  
184 elevation in each cross-section. This probably underestimates the actual bar amplitude,  
185 as the highest and lowest bed elevation values over one entire bar unit may not occur at  
186 the same cross-section.

## 2.5. Overview of bar theories

187 Since the late 1960s, several mathematical theories have been proposed to investigate  
188 and predict morphodynamics of alternate bars in straight river reaches [*Callander*, 1969]  
189 (an accessible introduction to the topic can be found in *Nelson* [1990]). These are mostly  
190 analytical theories, i.e. mathematical models based on analytical (or semi-analytical)  
191 solutions of the governing physical system, typically the two dimensional Saint Venant -  
192 Exner shallow water model [*Tubino et al.*, 1999]. The mathematical model is kept at the  
193 lowest meaningful level of complexity through a series of simplifying assumptions such  
194 as considering small bar amplitude, hence small deviations from the plane bed solution.  
195 This ensures the possibility to obtain mathematical solutions in close analytical form.

196 It is useful here to briefly recall the main features and outcomes of analytical bar  
197 theories that will be compared with the field observations on the Alpine Rhine River.  
198 The planform of the study reach can be viewed as a sequence of 16 straight longitudinal  
199 sections, connected by 14 short bends of constant curvature, and two ramps (left panel

of Figure 1). The most relevant bar theories for this case are therefore those for straight  
river reaches, which account for 83% of the whole reach length. As with many other  
analytical models for river bars and meandering, most of these theories predict properties  
of alternate bars for given constant values of flow discharge, channel width, reach slope,  
and sediment grain size. Quantitative results depend also on the choice of the roughness  
formula and of the bedload predictor. In the calculations we used a log-like formula  
for the former and the Meyer-Peter and Müller one for the latter. Moreover, the model  
assumes flow conditions where the entire cross section is actively transporting sediments.  
This means that the channel width corresponds to the active width (*Ashmore et al.* [2011];  
*Zolezzi et al.* [2012]).

According to analytical theories, alternate bars in straight, equiwidth reaches can de-  
velop because of a free instability mechanism of the riverbed ("free bars": *Colombini*  
*et al.* [1987]; *Schielen et al.* [1993]). Alternate bars in straight channels can also be forced  
by local persistent perturbations of the straight channel planform, as for example by the  
abrupt transitions from bends to straight reaches or by localized narrowing ("forced bars":  
*Struiksmas et al.* [1985], *Johannesson and Parker* [2013], *Struiksmas and Crosato* [2013]).

Linear theories consider bars as small-amplitude perturbations of the bed topography,  
i.e., much smaller compared to the reach-averaged flow depth. They allow computation  
of how deformation of an initially planar bed affects near-bed flow direction and strength,  
and the direction and rate of bedload. Thus, they predict formation, wavelength, and  
migration of bars. Non-linear theories (*Colombini et al.* [1987]; *Schielen et al.* [1993])  
are needed to predict the amplitude of bars. In straight channels, linear theories predict  
free alternate bars to be downstream migrating and forced alternate bars to be non-

223 migrating. In the same setting, forced steady bars are predicted to be about twice as long  
224 ( $L/W \sim 15 - 20$ ) as free migrating bars ( $L/W \sim 6 - 10$ ). Comparable length scales are  
225 predicted by non-linear theories, while migration speed is largely overestimated by linear  
226 theories, in comparison with data and non-linear theories [*Colombini et al.*, 1987].

227 In addition to the above simplifying assumptions, free bar theories assume an indefinitely  
228 long straight river reach, while theories for forced bars refer to a reach of finite length. The  
229 above assumptions strongly simplify the actual heterogeneity that characterizes natural  
230 rivers, where discharge is unsteady, grain size is heterogeneous, and channel width and  
231 slope may vary in the streamwise direction. *Tubino* [1991] proposed an analytical non-  
232 linear theory to investigate the role of discharge unsteadiness on alternate bar formation,  
233 amplitude, and wavelength. This mathematical analysis provides a suitable framework  
234 to evaluate the ratio between the temporal scales of floods and that of bar development,  
235 defined as  $U$  by *Tubino* [1991]. When  $U \gg 1$  floods do not last long enough to ensure  
236 bars reach a morphological equilibrium, whereas when  $U \ll 1$  it is possible to have  
237 instantaneous equilibrium of bar morphology with the flow conditions (see also *Eekhout*  
238 *et al.* [2013] for a recent application). Moreover, the assumption of constant grain size  
239 has been removed by *Lanzoni and Tubino* [1999] who developed a linear theory for free  
240 bars with bimodal sediments.

### 3. Results

241 Results of the Landsat imagery analysis are presented here in terms of bar wavelength,  
242 migration, and amplitude with focus on the longitudinal and temporal variations. The  
243 observed bar properties are then compared and interpreted by the available bar theories.

### 3.1. Bar wavelength

244 Bar wavelengths along the whole 41.7 km reach of the Alpine Rhine river are shown in  
245 Figure 4 for the period 1984-2013. Here, each point represents the wavelength of a single  
246 bar unit, as measured on one of the Landsat images. A total of 39 bar units are included.

247 Overall bar wavelengths range in the interval 750 - 1700 m, which corresponds roughly  
248 to 7 - 17 average channel widths. Based on bar wavelength values, the study reach can  
249 be divided into two main sectors. In the upstream sector, which extends down to km 16  
250 (bend 4), bars tend to be longer, with wavelengths in the interval 1200 - 1700 m ( $L/W =$   
251 14 - 20). Large fluctuations of the locally averaged wavelength are present along this  
252 first sector, with minimum values occurring close to the localized persistent planform  
253 discontinuities, such as bend  $b_1$  and  $b_2$ , and the first ramp  $r_1$ .

254 A sudden shortening is visible starting from bend 4, and shorter bars occur throughout  
255 the sector, with wavelengths generally in the interval 700 - 1200 m ( $L/W = 7 - 12$ ). The  
256 local bar wavelength shows a more uniform spatial trend on average, but with a higher  
257 number of outliers, with bars as short as 500 m and longer than 1700 m. Overall, the  
258 mean behavior of the data cloud in Figure 4 appears to vary rather smoothly within  
259 the straight reaches, while the presence of ramps, individual sharp bends, or sequences  
260 of nearly consecutive bends, is often associated with discontinuities in the spatial trend,  
261 inducing local elongation/shortening of bars. Wavelength values in the three sub-reaches  
262 were compared through a Kruskal-Wallis test. The outcome confirmed that the upstream  
263 sub-reaches is characterized by longer values ( $p < 0.05$ ). Bar wavelength shows a much  
264 higher local variability in the three longer straight reaches located in the upstream sector  
265 compared both to the shorter reaches located in the same upstream sector and to the

266 three longer reaches located in the downstream sector. The opposite behavior occurs in  
267 the downstream sector, where the highest variability in local bar wavelength is observed  
268 in the short straight reaches located in between bends. Local wavelength variability in  
269 straight reaches 2, 9, and 15 is the largest, with wavelengths that may differ by up to  
270 500 m.

271 Cumulative values of bar elongation are reported in Figure 5, where the change from  
272 1999 to 2010 is shown. We chose to limit the analysis to this period, to avoid the long  
273 gap between 1990 and 1999, which hinders an accurate reconstruction of bar dynamics.  
274 During this time interval, maximum elongation as well as maximum shortening range  
275 around 200 - 250 m (approximately 2.5 - 3 times the river width). Upstream of bend 4,  
276 bar wavelengths tend to remain fairly constant in time, with total variations shorter than  
277 one river width. The larger variations are observed in the reach between bend 4 and bend  
278 7, with bars experiencing an elongation of more than 200 m just downstream of bend 4,  
279 followed by an almost linear transition to a shortening of more than 200 m before bend 7.  
280 Close to bend 8, bars suddenly shifted to elongation (up to 150 m). Downstream of this,  
281 in the long straight sub-reach between bend 10 and 11, bars showed little variations, with  
282 a tendency to shorten towards the end of the reach. Also the longitudinal mean trend of  
283 bar elongation shows abrupt shifts near some bends, as it has been observed in Figure 4  
284 for bar wavelength.

### 3.2. Bar migration

285 The second parameter considered in the characterization of bar dynamics is their migra-  
286 tion. In Figure 6, the spatial trend of the cumulative bar migration over the period 1999-  
287 2010 is presented. Maximum downstream migration was approximately 1000 m (about 9

288 - 10 river widths or one average bar wavelength in the case of the downstream part of the  
289 reach). Many bars, mainly located in the upstream sub-reach and near planform obstacles,  
290 showed very low values of migration, with only 3 bars from a total of 77 denoting a slight  
291 upstream migration (negative values). In analogy with bar wavelength (Section 3.1), two  
292 rather different bar migration patterns characterize the same upstream and downstream  
293 sectors of the study reach, with the Kruskal-Wallis test resulting in a statistically differ-  
294 ent behaviour for the upstream sub-reach (lower migration) compared to the central and  
295 downstream sub-reaches ( $p < 0.05$ ). Upstream of bend 4 bars are generally non-migrating  
296 (or "steady"), with total migration values lower than one river width in both straight  
297 and curved reaches. A few km downstream of bend 4 migration reaches its maximum,  
298 with values around 1000 m. Along this second sector, bars tend to migrate downstream  
299 consistently, with several bar units moving downstream by 700 - 1000 m in most of the  
300 long straight subreaches 7, 8 and 13. The slowing effect of bends and ramps on alternate  
301 bars in the downstream sector is clearly visible. Close to bends 7, 8, 9 and 12, 13, 14, bars  
302 migrated less than half of the distance migrated by bars in the long straight sub-reaches.  
303 A few steady bars can be observed at the inner bank of bends 5, 12, and 13, and also  
304 close to the second ramp. Similarly to Figure 5, where from km 15 to km 24 and from km  
305 24 to km 35 the proximal bars elongated and the distal bars shortened, in Figure 6 the  
306 proximal bars migrate at a faster than average rate, while distal bars migrate at a slower  
307 than average rate.

308 Bar migration is analyzed also at the time scale of the single flood event, by computing  
309 bar movement between each consecutive Landsat image. Bars migrated no more than a  
310 few hundred meters (i.e. a few channel widths) even during the largest floods and we never

311 observed a complete rearrangement of the bed topography, with disappearance of the bar  
312 structure and formation of a new sequence. Two different sets of bars are presented in  
313 Figure 7, as representative of the different behavior of steady and migrating bars. The first  
314 set of bars (bar 36 and bar 30, located at km 5 and 12, respectively) was chosen to represent  
315 non-migrating bars (closed symbols in Figure 7). The second set of bars (bar 23 and bar  
316 09, located at km 22 and 35, respectively) includes bars that are located sufficiently far  
317 from bends and ramps, so that they freely migrate downstream (open symbols). The  
318 step-by-step migration of these 4 bars shows that they move mainly during larger floods  
319 (see Figure 2 for a comparison). Periods without significant events (e.g., in 2006-2007) are  
320 characterized by hardly any migration, even in the case of the migrating bars. Figure 7  
321 shows also that steady bars (closed symbols) moved slightly upstream and downstream in  
322 a narrow range of about 2 river widths, and are not influenced by flood occurrence. These  
323 fluctuations around a fixed position may also be due to changes in the exposed area,  
324 as a consequence of the different discharge at which the Landsat images were acquired.  
325 Overall, the analysis of bar migration suggests that a migration threshold of 2 channel  
326 widths (i.e., 180 m) can be used to discriminate between migrating and steady bars by  
327 comparing it with the decennial (1999 - 2010) cumulative migration of each bar unit.

328 The effect of different floods on bar migration has been further analyzed for the entire  
329 period 1984-2012 by focussing on the bars in sub-reaches 7 and 13, which migrated the  
330 longest distance. Several floods were singled out by consecutive Landsat images, covering  
331 a range from  $780 \text{ m}^3\text{s}^{-1}$  to  $2650 \text{ m}^3\text{s}^{-1}$ . The value of  $780 \text{ m}^3\text{s}^{-1}$  was chosen as a morpholog-  
332 ically relevant threshold, because it corresponds to conditions of fully transporting cross  
333 sections, and because no significant migration of bars was observed for floods with a lower

334 peak discharge. The effect of different floods is reported in Figure 8 as a function of three  
335 potentially controlling factors on bar migration. Overall, none of these considered flow  
336 parameters provide clear explanatory trends for bar migration. There is a tendency of  
337 bar migration to increase for higher flood duration (Figure 8b) and flood volume (Figure  
338 8c), but the scatter of the data is high. A maximum migration value was observed at a  
339 peak discharge up to roughly  $1800 \text{ m}^3\text{s}^{-1}$ , and then decreases again, reaching values close  
340 to 0 m for the largest flood on record (Figure 8a).

### 3.3. Bar height

341 Bar height ranged between 2.5 m and 4 m and, in contrast to bar wavelength and mi-  
342 gration, did not show any particular spatial trend (Figure 10). These values of bar height  
343 correspond to approximately 1 - 1.5 times the reach averaged water depth calculated with  
344  $Q_2 = 780 \text{ m}^3\text{s}^{-1}$ . Bar height presents longitudinal fluctuations, often characterized by a  
345 minimum value near bends and ramps. In particular, the second ramp has a strong effect,  
346 reducing bar height to 2 m.

### 3.4. Application of bar theories

347 The following bar theories were applied to predict bar properties and to support in-  
348 terpretation of the field observations: the linear theories for free migrating bars, and for  
349 forced steady bars, in the versions proposed by *Colombini et al.* [1987] and by *Zolezzi and*  
350 *Seminara* [2001]; the non-linear theories for free migrating bars of *Colombini et al.* [1987]  
351 and of *Tubino* [1991].

352 First of all, the reach-averaged lower discharge limit for fully transporting cross-sections  
353 was computed to establish the meaningful discharge range for theory application. The

354 fully transporting discharge  $Q_{FT}$  ranges between  $500 \text{ m}^3\text{s}^{-1}$  and  $800 \text{ m}^3\text{s}^{-1}$  in the different  
355 sub-reaches (Table 2). These values are sensitive to the choice of the bed roughness and  
356 on the critical threshold for the incipient motion  $\theta_C$ .

357 The linear theory for free migrating bars was applied to predict the conditions of free  
358 bar occurrence and their wavelength. This theory predicts free bar instability whenever  
359 the width to depth ratio  $\beta$  is higher than a critical threshold  $\beta_{cr}$ , which depends on the  
360 shear stress and the average grain size roughness, and which generally ranges between  
361 10 and 20. We computed the discharge value  $Q_{cr}$  that determines critical conditions  
362 ( $\beta = \beta_{cr}$ ), for each of the three reaches. According to the theory, discharge values below  
363 this threshold are likely to induce bar formation. Values range between  $1850 \text{ m}^3\text{s}^{-1}$  and  
364  $1950 \text{ m}^3\text{s}^{-1}$  (Table 2). This is the second relevant discharge threshold that sets the flow  
365 conditions under which alternate bar formation is expected. These two thresholds ( $Q_{FT}$   
366 and  $Q_{cr}$ ) are depicted in Figure 2, considering the values for the center reach. The figure  
367 shows that almost every flood is characterized by a peak value that falls in the area where  
368 alternate bars should form, according to *Colombini et al.* [1987]. During the considered  
369 time interval of 30 years, only two floods peaked above the critical threshold  $Q_{cr}$ . Overall,  
370 for 99.9% of the time when discharge exceeded the fully transporting threshold, the study  
371 reach was in a condition of free bars instability ( $\beta > \beta_{cr}$ ).

372 Results from the linear theory show that the most unstable wavelength for free migrating  
373 bars is approximately 750 m and remains almost constant along the study reach, because  
374 the decline in grain size is almost counterbalanced by the decline in longitudinal slope.  
375 The intrinsic uncertainty in the choice of representative reach-average slope and grain  
376 size values due to their local variability, does not affect the theoretical prediction of bar

377 wavelength significantly. More precisely, from a sensitivity analysis performed on the  
378 values of the reach-averaged sediment size used as model inputs (Table 2), and within a  
379 range of formative discharges between  $400 \text{ m}^3\text{s}^{-1}$  and  $1000 \text{ m}^3\text{s}^{-1}$ , the value of the most  
380 unstable migrating bar wavelength changes by only 5% when grain size and slope are  
381 varied by 20% around their reach-average values. This also accounts for the influence of  
382 the grain size value on the roughness coefficient. From a sensitivity analysis performed  
383 on the critical shear stress, we saw that bar wavelength changes by only 5% using values  
384 of the critical shear stress in the range 0.03-0.05. Using a different bed-load formula  
385 (e.g. *Parker* [1990]), bar wavelength variability remains below 5%. The predicted value  
386 of the most unstable wavelength is slightly shorter than the measured wavelengths of  
387 the alternate bars that were observed to migrate, which range from 750 to 1000 m. On  
388 the other hand, the computed wavelength of forced steady bars ranges between 2000 and  
389 3200 m, i.e. almost twice as much as the observed wavelength (1200 to 1500 m) of the bars  
390 classified as non-migrating in our analysis, which mostly occurred in the straight reaches  
391 of the upstream sector.

392 Values of bar height presented in Figure 10 were compared to the values of the free  
393 migrating bars equilibrium amplitude predicted by *Colombini et al.* [1987] and also by the  
394 empirical formulation proposed by *Ikeda* [1984], which estimates bar height as a function  
395 of sediment diameter and the width to depth ratio. In the *Colombini et al.* [1987] weakly  
396 non-linear theory with steady flow conditions, bar height is a function of flow and sediment  
397 characteristics, and of the distance from the critical conditions for free bar instability ( $\beta -$   
398  $\beta_{cr}$ ). The two formulations give similar results, with bar height decreasing from upstream  
399 to downstream (ranging from 6.2 m to 4.8 m for  $Q = Q_2$ ), and decreasing for higher

400 discharges until disappearing when  $Q$  approaches  $Q_{cr}$ . Therefore, bar height computed  
401 with  $Q = Q_2$  can be considered an upper limit, as larger floods are likely to reduce  
402 bar height. The observed bar height is on average smaller than the predicted values.  
403 This could be the result of a series of larger floods occurred in the five years before the  
404 topographic survey (2005, see Figure 2).

405 Finally, an application of Tubino's (1991) theory for free bar evolution under unsteady  
406 flow conditions was attempted. The analytical non-linear model of *Tubino* [1991] allows  
407 the comparison of the relevant time scales of the morphological evolution and of the  
408 flood duration, through the dimensionless parameter  $U$  (see Section 2.5). The value of  
409  $U$  computed for several floods that occurred in the last 30 years in the Alpine Rhine is  
410 approximately 20, therefore falling in the case  $U \gg 1$ . This means that floods are short  
411 with respect to the time needed by free bars to grow to their equilibrium height.

#### 4. Discussion

412 The availability of a spatially and temporally long dataset of the Alpine Rhine proved  
413 useful to better understand the morphological properties and dynamics of alternate bars  
414 in channelized rivers. Although the observations are specific to the investigated reach, the  
415 comparison with the outcomes of existing analytical theories of free and forced alternate  
416 bars can help interpret other field studies (see Table 1). In the following, we discuss the  
417 results obtained in this study focussing on (i) the relevance of the developed dataset in  
418 comparison with existing ones; (ii) the comparison of the observed alternate bar properties  
419 with previous field observations; and (iii) the ability of analytical bar theories to predict  
420 and interpret field observations.

#### 4.1. The Alpine Rhine alternate bar dataset

421 The availability of a remotely sensed dataset of a 41.7 m long reach of the Alpine Rhine  
422 covering about 30 years allowed a thorough investigation of the morphology and dynamics  
423 of 40 bar units. This is a valuable source of information to understand the controls  
424 on alternate bar formation and migration, which may greatly increase the possibility to  
425 evaluate and predict the evolution of these bed forms. Landsat imagery proved to be  
426 an excellent source of freely available data, in terms of number of images per year and  
427 pixel resolution, confirming the findings reported by *Henshaw et al.* [2013]; *Constantine*  
428 *et al.* [2014]. The possibility to choose among several images allowed for combining a  
429 multi-decadal analysis, with details on the effect of single floods. Such an approach can  
430 be replicated to study the dynamics of bars (not only alternate bars) on river reaches of  
431 the same or of larger size worldwide.

432 The relevance of the developed dataset emerges in comparison to previous field studies,  
433 which generally considered a much smaller number of bars and/or a much shorter time  
434 period. The present study is the only multi-decadal study on alternate bar dynamics in  
435 a river reach that includes about 40 bar wavelengths and based on an average of nearly  
436 2 available surveys (i.e., Landsat images) per year. The reported results on the Alpine  
437 Rhine show that bar morphology and dynamics are variable in time and space. The effect  
438 of spatial discontinuities like bends, or temporal events like floods (or the absence of) can  
439 have an impact on bar wavelength and migration in relatively long reaches. This has to  
440 be taken into account to improve our general understanding of these bedforms. Spatially  
441 and temporally long observations are even more relevant when the aim is to quantify bar  
442 migration. Very few field data on bar migration are available in the literature and this

443 data set provides a valuable source of information for testing physical, numerical, and  
444 mathematical models.

445 Table 1 lists the main field observations reported in the literature in the last decades.  
446 Most previous field studies are limited to short artificial channels (e.g., *Lewin* [1976];  
447 *Welford* [1994]; *Ferguson et al.* [2011]; *Eekhout et al.* [2013]) or analyzed a relatively short  
448 time-scale (e.g., *Rodrigues et al.* [2012]; *Zolezzi et al.* [2012]; *Rodrigues et al.* [2015]). Our  
449 observations on the Alpine Rhine showed large variations in bar morphology both in space  
450 and in time. This suggests that local effects, as well as the occurrence of specific floods  
451 may affect bar morphodynamics. The only comparable cases in terms of space and time  
452 scale are the studies presented by *Church and Rice* [2009], *Ferguson et al.* [2011] and by  
453 *Jaballah et al.* [2015]. Though all these studies refer to alternate bars, their setting may  
454 slightly differ, suggesting that some care is required when comparing observations. For ex-  
455 ample, in the Fraser River [*Church and Rice*, 2009], channel width shows more pronounced  
456 spatial oscillations, which likely provide an additional forcing effect, enhancing the for-  
457 mation of steady bars [*Repetto et al.*, 2002]. This occurs also in the Arc River [*Jaballah*  
458 *et al.*, 2015], though to a much smaller extent and only before the engineering works that  
459 flattened the channel bed towards the middle of the observation period. In other cases,  
460 as in *Rodrigues et al.* [2012] and *Rodrigues et al.* [2015], the relatively short reach length  
461 may produce significant local effects, imposed by the upstream and downstream morpho-  
462 logical conditions. Moreover, in both the Fraser and Arc rivers, vegetation is reported  
463 as a relevant factor that tends to affect bar dynamics by stabilizing them, stopping their  
464 migration, as well as by changing their wavelength and amplitude (*Bertoldi et al.* [2014]).  
465 Furthermore, some of the existing field studies (e.g. *Eekhout et al.* [2013]; *Jaballah et al.*

466 [2015]) studied the initial development of alternate bars, while others (e.g. *Welford* [1994];  
467 *Rodrigues et al.* [2012, 2015]) as well as the present case have already completed this initial  
468 development and are nowadays presumably nearer a condition of quasi-equilibrium.

## 4.2. Observed bar morphodynamics: wavelength and migration

469 In terms of observed bar wavelength (as a function of channel width), the freely migrat-  
470 ing bars of the downstream part of the Alpine Rhine show comparable results to those  
471 reported in previous field studies, ranging between the shorter bars monitored by *Church*  
472 *and Rice* [2009] (4 to 5 times the width) and the longer (9 to 10 widths) reported by  
473 *Ferguson et al.* [2011]. This range is comparable also to laboratory findings (*Ikeda* [1984],  
474 *Jäggi* [1984], *Tubino et al.* [1999]).

475 Few other studies report on data about bar migration. The Alpine Rhine shows an  
476 average migration of the free bars located in the downstream reach that is of the order  
477 of 0.8 - 0.9 times the average channel width per year. Previous studies on the same river  
478 reach, though based on a different methodology, indicate migration rates in the 1960s  
479 and 1970s ranged between 1.5 and 3 times the average channel width per year (*Zeller*  
480 [1967] cited in *Jäggi* [1983], *Jäggi* [1983]). A close comparison between our estimate and  
481 previous estimates on the same river reach is barely possible because previous estimates  
482 were based on different observation time periods, and thus the discrepancy is likely due  
483 to the effect of a few relevant flood events. Moreover, the two ramps were built in the  
484 early 1980s, possibly adding a further effect that may have forced (some) of the bars in  
485 more stable locations.

486 An analogous result, with a bar migration equal to 0.7 times the channel width per year,  
487 can be inferred from data presented by *Rodrigues et al.* [2012] on the Loire river, which

488 has sandy bed material. Bar migration is a complex function of discharge (or sediment  
489 transport rate), bar morphology, and is also strongly affected by grain sorting (*Lanzoni*  
490 [2000b]) and presence of obstacles. Therefore, it is difficult to compare bar migration  
491 among different rivers, and between field observations and flume experiments, where the  
492 discharge is generally constant and the channel is perfectly regular and straight. *Crosato*  
493 *et al.* [2012] reported on long-term experiments on alternate bar dynamics, showing that  
494 there is a strong decreasing relationship between bar migration speed and bar wavelength,  
495 with bar migration reducing to half when the wavelength increases from 5 to 7.5 times the  
496 channel width. Our observations on the Alpine Rhine show a similar relationship, although  
497 with a few differences. The relationship between cumulative bar migration in the period  
498 1999 - 2010 and bar wavelength is explicitly plotted in Figure 9. Differently from Figure  
499 4, the wavelength value for each point in the plot is obtained as the average wavelength  
500 of the bar unit for which the cumulative (1999 to 2010) migration has been computed.  
501 The migration threshold of 180 m (two channel widths) used to discriminate between  
502 steady and migrating bars is represented through a horizontal dashed line. Average bar  
503 wavelengths fall into two markedly different clusters, resulting in a bar wavelength gap in  
504 the range 1090 m - 1190 m, where no bars plot. This allows to distinguish between "long"  
505 (i.e.,  $> 1190$  m) and "short" (i.e.,  $< 1090$  m) alternate bars. Long bars can be found only  
506 in the upstream sector (open symbols of Figure 9), while short bars are found only in  
507 the downstream sector (closed symbols of Figure 9). A rather close relation between bar  
508 wavelength and cumulative migration appears: short bars are mostly migrating, whereas  
509 long bars are mainly steady. More precisely, 75% of long bars are steady and 90% of short  
510 bars migrate. Maximum migration of the shorter bars occurs within a wavelength range

511 of 900 - 1000 m, though smaller migration values are possible in the same range. Only  
512 a few short bars show a different behavior, with much lower values of migration (10% of  
513 the short bars). These are generally bars close to bends or ramps, and their wavelength is  
514 strongly affected by these obstacles. In most cases, ramps determine the occurrence of a  
515 steady bar front immediately upstream, with bar wavelength adjusting accordingly. This  
516 could be caused by the forced flat bed cross section imposed by the fixed ramp and by the  
517 high sediment transport flux induced by the larger local longitudinal slope. The presence  
518 of bends is invariably associated with a reduction of bar migration rate (Figure 6), and  
519 presents a twofold effect on bar wavelength (Figure 4): in the upstream reach, bends  
520 trigger sharp changes in the spatial variability of bar lengths, while in the downstream  
521 reach they are associated with a large local variability of bar lengths.

522 *Crosato et al.* [2012] also reported on the formation of steady longer bars (particularly in  
523 the upstream part of the flume), which are likely to suppress the migrating bars. It is not  
524 clear whether the systematic occurrence of steady bars in the upper reach of the Alpine  
525 Rhine may be explained in these terms, or whether they are caused by the occurrence  
526 of sharp bends which may induce the formation of forced bed forms (see *Zolezzi and*  
527 *Seminara* [2001]; *Zolezzi et al.* [2005]). The recent extensive study of *Jaballah et al.* [2015]  
528 on alternate bar dynamics in the Arc River, France, showed the existence of migrating  
529 bars, along with steady, longer bars affected by spatial constraints such as a bend or a  
530 bridge. Similarly, *Ferguson et al.* [2011] reported the coexistence of steady and migrating  
531 bars in the Vedder Canal. *Jaballah et al.* [2015] pointed out the relevance of including  
532 flow unsteadiness, to better understand and predict river bar evolution. In particular, flow

533 conditions falling under the fully transport discharge may be responsible for the creation  
534 of shorter mid-channel bars that contribute to a more complex pattern.

### 4.3. A theoretical perspective on the observed bar dynamics

535 The results presented in the present work show that several bar properties (e.g. wave-  
536 length, migration) occurring over a 3-decade period in a long ( $> 400$  channel widths)  
537 reach of the Alpine Rhine are qualitatively consistent with analytical bar theories.

538 At the same time, discrepancies between observations and predictions can be high-  
539 lighted. According to linear theories, both free migrating and forced steady bars can  
540 occur in the upstream and in the downstream sectors of the study reach, while observa-  
541 tions suggest a spatially selective behavior, whereby long steady bars occur upstream and  
542 short migrating bars occur downstream. Moreover, the observed length of steady bars in  
543 the upstream straight reaches is shorter compared to the predictions of the linear theory  
544 for forced steady bars. We suggest that this discrepancy may be related to the effects  
545 of some of the assumptions on which the theories are built, which simplify the actual  
546 complexity of the real systems and allow focusing on "key" physical factors thought to  
547 act as major controls on bar morphodynamics. Clarifying what theories can and what  
548 they cannot predict is important to better illustrate how they can be used effectively to  
549 interpret field observations. In the following we focus on: (i) the unsteadiness of the flow;  
550 (ii) the finite length of straight reaches and (iii) the heterogeneity of the grain size.

#### 551 4.3.1. Flow unsteadiness

552 Application of *Tubino* [1991] non-linear theory for free migrating bars in straight chan-  
553 nels indicates that the time scale of flow unsteadiness is much shorter than the morpholog-  
554 ical time scale needed for free bars to reach their equilibrium amplitude. This underpins

555 the possibility to use the assumption of steady flow. Under this hypothesis, the linear free  
556 bar theory predicts the wavelength of migrating bars, which is also known to be almost  
557 unaffected by non-linear effects (*Colombini et al.* [1987]), and does not show significant  
558 changes during the 30 years of observation. Therefore, despite the fact that the observed  
559 alternate bar configuration was generated by the action of a long lasting ( $> 150$  years)  
560 sequence of unsteady flows, the present analysis strongly suggests the validity of assuming  
561 a constant, bar-forming value of discharge to predict the condition of occurrence and the  
562 wavelength of migrating bars. On the other side, floods with the same intensity and dura-  
563 tion can determine different migration properties of the same bar units: flow unsteadiness  
564 might then be relevant at shorter time scales (i.e. flood event), in locally reshaping and  
565 moving individual bars. Moreover, the analysis of the  $U$  parameter proposed by *Tubino*  
566 [1991] suggests that the two floods (in 1987 and 2005) that peaked at a discharge larger  
567 than  $Q_{cr}$  did not have enough time to flatten the riverbed, resetting the bar configuration.  
568 This confirms our observations, which exclude the possibility that the alternate bars were  
569 flattened during the 2005 flood, as the bar configuration before and after the flood was  
570 remarkably similar, with most bars only moving slightly downstream (Figure 8a).

#### 571 **4.3.2. Finite reach length**

572 The linear theory for free migrating bars is obtained referring to an infinite channel  
573 length, where a periodical analytical solution is derived in the streamwise direction. An  
574 analogous assumption characterizes the linear theory for forced steady bars, where the  
575 channel length is assumed infinite only in one direction, with an upstream (or down-  
576 stream) boundary where a local persistent perturbation of the straight, equiwidth channel  
577 geometry is present. The reported observations may help define a minimum reach length

578 that can satisfy the (semi) infinite length condition. Our study site included a total of six  
579 straight reaches (three in each main sector) longer than approximately 2 km, i.e. 3 times  
580 the predicted free bar wavelength. Every straight reach is bounded upstream and down-  
581 stream by local planform perturbations consisting of bends, ramps, confluences, which  
582 force steady bars in the nearby straight reaches. Only in some of the straight reaches,  
583 namely the three located in the downstream sector, migrating bars are observed. *Jabal-*  
584 *lah et al.* [2015] observed migrating bars in a 2.3 km long ( $\sim 45$  channel widths, or  $\sim 4$   
585 times the longest bar wavelength) straight reach of the Arc River in France, bounded by  
586 an upstream bend and by a downstream asymmetrical bridge pier. In their study, the  
587 number of migrating bars decreased with time. The migrating bars observed by *Eekhout*  
588 *et al.* [2013] occurred in a longer straight reach (in terms of bar wavelengths), while the  
589 secondary channel of the Loire River where alternate bar migration was observed by *Ro-*  
590 *drigues et al.* [2015] is not longer than 2 bar wavelengths. The above observations suggest  
591 that a straight reach length of several times the free migrating bar wavelength might be  
592 a necessary though not a sufficient condition for migrating bars to occur.

### 593 4.3.3. Sediment size heterogeneity

594 Another simplifying assumption in the examined theories is the uniformity of grain  
595 size. The mathematical modeling and experimental works by *Lanzoni and Tubino* [1999]  
596 and *Lanzoni* [2000a] showed that graded sediments cause elongation of migrating bars,  
597 as well as a decrease of the migration speed. Indeed, we observed also a much slower  
598 migration rate than that predicted by linear theories. In addition to the previous points,  
599 bar migration is affected also by non linear effects caused by bar amplitude. As a result,

600 bar migration cannot be accurately predicted by linear theories, and weakly non-linear  
601 theories or numerical models are needed.

602 The awareness of how much the theoretical assumptions may limit their applicability  
603 allows a more critical use of theories to interpret field observations. All of the observed  
604 bar wavelengths fall within the two limits set by linear theories for free migrating and  
605 forced steady bars in straight reaches. The range of variability of these limits is relatively  
606 narrow, when considering meaningful ranges for discharge, grain size, and channel slope  
607 (*Adami et al.* [2014]). Such analytically derived limits may therefore be viewed as the  
608 lower and upper boundaries of what can be actually observed in the corresponding real  
609 setting of straight river reaches. The alternate bars observed in the Alpine Rhine are likely  
610 to be the result of a non-linear interaction between the two types of bars (free and forced)  
611 predicted by the theories. This is in agreement with the experimental and numerical  
612 results of *Crosato and Mosselman* [2009] and *Crosato et al.* [2011] and with the analytical  
613 studies referring to weakly meandering channels with constant width (*Kinoshita and Miwa*  
614 [1967], *Tubino and Seminara* [1990]) and to straight channels with spatially oscillating  
615 width *Repetto and Tubino* [2001]. We argue that the result of such non-linear interaction  
616 would eventually result in bars with wavelengths falling within the limits predicted by  
617 linear theories. Interestingly, in the Alpine Rhine the observed migrating and steady bar  
618 lengths are closer to the computed limits for free and forced bars, respectively, which  
619 further supports this hypothesis. While the broad tendency can be therefore attributed  
620 to the physical processes already retained in the linear theories, further developments on  
621 the non-linear free-forced bars interaction in straight channels are needed to provide a  
622 complete picture of the controlling parameters and of the dominant effects. Furthermore,

623 an analytical theory that addresses the role of bed discontinuities, such as ramps, on  
624 alternate bars in straight channels is also still missing.

## 5. Conclusions

625 This paper reports on the morphological dynamics of alternate bars in the Alpine Rhine.  
626 The analysis resulted in the longest spatial and temporal field case study of river bars  
627 in channelized rivers with a temporal survey resolution allowing to investigate the effect  
628 of individual floods. This quantitative dataset on bar wavelength and migration proved  
629 valuable to better interpret bar dynamics at the reach scale and to demonstrate the  
630 applicability and limits of analytical theories. Bars show a spatially selective behavior,  
631 with short, migrating bars occurring in distinct straight reaches with respect to longer,  
632 steady bars. A full range of bar wavelengths and more complex patterns occur in reaches  
633 with bends and ramps. Bar height obtained from cross section monitoring was found to  
634 be much more uniform. The temporally long dataset, including approximately 30 floods  
635 with different magnitude and duration, allowed the investigation of bar migration as a  
636 function of discharge, showing that bars migrate faster during intermediate floods, as  
637 larger discharges are probably responsible for a slight flattening of the bed forms.

638 The dataset also provided useful information to assess the applicability of analytical bar  
639 theories, so far mainly tested against flume experiments, and following recent attempts in  
640 French and Dutch streams. Values predicted by linear theories for free and forced bars in  
641 straight channels are in good general agreement with field observations, when considering  
642 conditions of bar formation and bar wavelength. Comparing theories and observations  
643 suggests that theoretical outcomes may represent the boundaries of the actual, interme-  
644 diate behavior of bars, which likely reflects non-linear interactions, flow unsteadiness,

645 sediment size heterogeneity and finite length of straight reaches, which are not retained in  
646 linear theories. The comparison demonstrates the value of theories for the interpretation  
647 of field observations. For instance, the difference in the migration-wavelength relation  
648 may suggest the long, steady bars to be forced by local planform discontinuities and the  
649 short migrating bars to result from a free instability of the riverbed. Flow unsteadiness  
650 seems to have a minor role here while grain size sorting might affect bar wavelength and  
651 migration. Together with analytical theories set up to separately investigate both effects,  
652 a numerical analysis might also help to study bar dynamics subject to real flood sequences.

653 Despite the above limits, the work shows that bar theories not only provide information  
654 on bar geometry and dynamics, but they can also help interpret the physical processes at  
655 the basis of their occurrence, i.e., set a suitable framework to differentiate between free  
656 migrating or forced steady bars.

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## References

664 Adami, L., W. Bertoldi, and G. Zolezzi (2014), Morphodynamics of alternate bars in  
665 the alpine rhine river: Methods for the applicability of mathematical models using

666 fields observations, *Proceedings of the International Conference on Fluvial Hydraulics,*  
667 *RIVER FLOW 2014*, pp. 1213–1220.

668 Ashmore, P., W. Bertoldi, and J. Tobias Gardner (2011), Active width of gravel-bed  
669 braided rivers, *Earth Surface Processes and Landforms*, *36*(11), 1510–1521, doi:10.1002/  
670 esp.2182.

671 Bertoldi, W., A. Siviglia, S. Tettamanti, M. Toffolon, D. Vetsch, and S. Francalanci  
672 (2014), Modeling vegetation controls on fluvial morphological trajectories, *Geophysical*  
673 *Research Letters*, *41*(20), 7167–7175, doi:10.1002/2014GL061666.

674 Callander, R. A. (1969), Instability and river channels, *Journal of Fluid Mechanics*, *36*,  
675 465–480.

676 Church, M., and S. P. Rice (2009), Form and growth of bars in a wandering gravel-bed  
677 river, *Earth Surface Processes and Landforms*, *34*(10), 1422–1432, doi:10.1002/esp.1831.

678 Colombini, M., G. Seminara, and M. Tubino (1987), Finite-amplitude alternate bars,  
679 *Journal of Fluid Mechanics*, *181*, 213–232, doi:10.1017/S0022112087002064.

680 Constantine, J. A., T. Dunne, J. Ahmed, C. Legleiter, and E. D. Lazarus (2014), Sediment  
681 supply as a driver of river meandering and floodplain evolution in the Amazon Basin,  
682 *Nature Geoscience*, *7*(12), 899–903, doi:10.1038/ngeo2282.

683 Crosato, A., and E. Mosselman (2009), Simple physics-based predictor for the number  
684 of river bars and the transition between meandering and braiding, *Water Resources*  
685 *Research*, *45*(3), n/a–n/a, doi:10.1029/2008WR007242, w03424.

686 Crosato, A., E. Mosselman, F. Beidmariam Desta, and W. S. J. Uijttewaal (2011), Ex-  
687 perimental and numerical evidence for intrinsic nonmigrating bars in alluvial channels,  
688 *Water Resources Research*, *47*(3), n/a–n/a, doi:10.1029/2010WR009714.

- 689 Crosato, A., F. B. Desta, J. Cornelisse, F. Schuurman, and W. S. J. Uijttewaal (2012), Ex-  
690 perimental and numerical findings on the long-term evolution of migrating alternate bars  
691 in alluvial channels, *Water Resources Research*, *48*(6), doi:10.1029/2011WR011320.
- 692 Eekhout, J. P. C., A. J. F. Hoitink, and E. Mosselman (2013), Field experiment on  
693 alternate bar development in a straight sand-bed stream, *Water Resources Research*,  
694 *49*(12), 8357–8369, doi:10.1002/2013WR014259.
- 695 Engels, H. (1914), *Handbuch des Wasserbaues: für das Studium und die Praxis*, Engel-  
696 mann.
- 697 Engelund, F. A., and E. Hansen (1967), *Monograph on sediment transport in alluvial*  
698 *streams. / By Frank Engelund and Eggert Hansen*, Copenhagen: Teknisk forlag.
- 699 Ferguson, R. I., D. J. Bloomer, and M. Church (2011), Evolution of an advancing gravel  
700 front: observations from Vedder Canal, British Columbia, *Earth Surface Processes and*  
701 *Landforms*, *36*(9), 1172–1182, doi:10.1002/esp.2142.
- 702 Fredsøe, J. (1978), Meandering and braiding of rivers, *Journal of Fluid Mechanics*, *84*(pt  
703 4), 609–624, cited By 73.
- 704 Henshaw, A. J., A. M. Gurnell, W. Bertoldi, and N. A. Drake (2013), An assessment of the  
705 degree to which Landsat TM data can support the assessment of fluvial dynamics, as  
706 revealed by changes in vegetation extent and channel position, along a large river, *Ge-*  
707 *omorphology*, *202*(0), 74 – 85, doi:http://dx.doi.org/10.1016/j.geomorph.2013.01.011.
- 708 Hunziker, Zarn, and Partners (2001), Morphologie und geschiebehalt alpenrhein  
709 (morphology and sediment budget of alpine rhine), *Project A-108*, Internationale  
710 Regierungskommission Alpenrhein (International Government Commission of Alpine  
711 Rhine).

- 712 Ikeda, S. (1984), Prediction of alternate bar wavelength and height, *Journal of Hydraulic*  
713 *Engineering*, 110(4), 371–386, doi:10.1061/(ASCE)0733-9429(1984)110:4(371).
- 714 Jaballah, M., B. Camenen, L. Pnard, and A. Paquier (2015), Alternate bar development in  
715 an alpine river following engineering works, *Advances in Water Resources*, 81(available  
716 on-line), 103–113, doi:http://dx.doi.org/10.1016/j.advwatres.2015.03.003.
- 717 Jäggi, M. (1983), Alternierende kiesbanke (Alternate bars), Ph.D. thesis, Swiss Federal  
718 Institute of Technology Zürich Laboratory of Hydraulics, Hydrology and Glaciology,  
719 Switzerland.
- 720 Jäggi, M. (1984), Formation and effects of alternate bars, *Journal of Hydraulic Engineer-*  
721 *ing*, 110(2), 142–156, doi:10.1061/(ASCE)0733-9429(1984)110:2(142).
- 722 Johannesson, H., and G. Parker (2013), *Linear Theory of River Meanders*, pp. 181–213,  
723 American Geophysical Union, doi:10.1029/WM012p0181.
- 724 Kinoshita, R., and H. Miwa (1967), River channel formation which prevents downstream  
725 translation of transverse bar (in japanese), *Shinsabo*, 94, 12–17.
- 726 Lanzoni, S. (2000a), Experiments on bar formation in a straight flume: 1. uniform sedi-  
727 ment, *Water Resources Research*, 36(11), 3337–3349, doi:10.1029/2000WR900160.
- 728 Lanzoni, S. (2000b), Experiments on bar formation in a straight flume: 2. graded sediment,  
729 *Water Resources Research*, 36(11), 3351–3363, doi:10.1029/2000WR900161.
- 730 Lanzoni, S., and M. Tubino (1999), Grain sorting and bar instability, *Journal of Fluid*  
731 *Mechanics*, 393, 149–174, doi:10.1017/S0022112099005583.
- 732 Lewin, J. (1976), Initiation of bedforms and meanders in coarse grained sediment, *Bulletin*  
733 *of the Geological Society of America*, 87(2), 281–285.

- 734 Nelson, J. (1990), The initial instability and finite-amplitude stability of alternate bars  
735 in straight channels, *Earth Science Reviews*, *29*(1-4), 97–115, doi:10.1016/0012-8252(0)  
736 90030-Y.
- 737 Parker, G. (1976), On the cause and characteristic scales of meandering and braiding in  
738 rivers, *Journal of Fluid Mechanics*, *76*(3), 457–480, doi:10.1017/S0022112076000748.
- 739 Parker, G. (1990), Surface-based bedload transport relation for gravel rivers, *Journal of*  
740 *Hydraulic Research*, *28*(4), 417–436, doi:10.1080/00221689009499058.
- 741 Parker, G., P. R. Wilcock, C. Paola, W. E. Dietrich, and J. Pitlick (2007), Physical  
742 basis for quasi-universal relations describing bankfull hydraulic geometry of single-  
743 thread gravel bed rivers, *Journal of Geophysical Research: Earth Surface*, *112*(F4),  
744 doi:10.1029/2006JF000549.
- 745 QGIS Development Team (2009), *QGIS Geographic Information System*, Open Source  
746 Geospatial Foundation.
- 747 Repetto, R., and M. Tubino (2001), Topographic expressions of bars in channels with  
748 variable width, *Physics and Chemistry of the Earth, Part B: Hydrology, Oceans and*  
749 *Atmosphere*, *26*(1), 71–76, doi:10.1016/S1464-1909(01)85017-6, cited By 4.
- 750 Repetto, R., M. Tubino, and C. Paola (2002), Planimetric instability of channels with vari-  
751 able width, *Journal of Fluid Mechanics*, *457*, 79–109, doi:10.1017/S0022112001007595.
- 752 Rodrigues, S., N. Claude, P. Juge, and J.-G. Breheret (2012), An opportunity to connect  
753 the morphodynamics of alternate bars with their sedimentary products, *Earth Surface*  
754 *Processes and Landforms*, *37*(2), 240–248, doi:10.1002/esp.2255.
- 755 Rodrigues, S., E. Mosselman, N. Claude, C. L. Wintenberger, and P. Juge (2015), Alter-  
756 nate bars in a sandy gravel bed river: generation, migration and interactions with

- 757 superimposed dunes, *Earth Surface Processes and Landforms*, 40(5), 610–628, doi:  
758 10.1002/esp.3657.
- 759 Schielen, R., A. Doelman, and H. de Swart (1993), On the nonlinear dynamics of free bars  
760 in straight channels, *Journal of Fluid Mechanics*, 252, 325–356.
- 761 Struiksma, N., and A. Crosato (2013), *Analysis of a 2-D Bed Topography Model for Rivers*,  
762 pp. 153–180, American Geophysical Union, doi:10.1029/WM012p0153.
- 763 Struiksma, N., K. Olesen, C. Flokstra, and H. De Vriend (1985), Bed deformation in  
764 curved alluvial channels, *Journal of Hydraulic Research*, 23(1), 57–59, doi:10.1080/  
765 00221688509499377.
- 766 Tubino, M. (1991), Growth of alternate bars in unsteady flow, *Water Resources Research*,  
767 27(1), 37–52, doi:10.1029/90WR01699.
- 768 Tubino, M., and G. Seminara (1990), Free-forced interactions in developing meanders and  
769 suppression of free bars, *Journal of Fluid Mechanics*, 214, 131–159, cited By 57.
- 770 Tubino, M., R. Repetto, and G. Zolezzi (1999), Free bars in rivers, *Journal of Hydraulic*  
771 *Research*, 37(6), 759–775, doi:10.1080/00221689909498510.
- 772 Welford, M. R. (1994), A field test of Tubino’s (1991) model of alternate bar formation,  
773 *Earth Surface Processes and Landforms*, 19(4), 287–297, doi:10.1002/esp.3290190402.
- 774 Werth, K. (2014), *Geschichte der Etsch zwischen Meran und San Michele Flussreg-*  
775 *ulierung, Trockenlegung der Mser, Hochwasserschutz.*, Athesia.
- 776 Zeller, J. (1967), Flussmorphologische studie zum mäanderproblem / meandering channels  
777 in switzerland, *Project 74*, ETH Zürich.
- 778 Zolezzi, G., and G. Seminara (2001), Downstream and upstream influence in river me-  
779 andering. part 2. planimetric development, *Journal of Fluid Mechanics*, 438, 183–211,

780 doi:10.1017/S002211200100427X.

781 Zolezzi, G., M. Guala, D. Termini, and G. Seminara (2005), Experimental observations  
782 of upstream overdeepening, *Journal of Fluid Mechanics*, 531, 191–219.

783 Zolezzi, G., W. Bertoldi, and M. Tubino (2012), *Morphodynamics of Bars in Gravel-Bed*  
784 *Rivers: Bridging Analytical Models and Field Observations*, pp. 69–89, John Wiley &  
785 Sons, Ltd, doi:10.1002/9781119952497.ch6.

**Figure 1.** Overview of the study area with the catchment of the Rhine River in light gray and the catchment of the Alpine Rhine highlighted in dark gray. Within the left panel, locations of bends and ramps in the study reach are identified.

**Figure 2.** Discharge record for the period 1984-2012. Circles represent acquisition date and corresponding discharge value of the analyzed Landsat imagery. Horizontal lines indicate the fully wet discharge  $Q_{FW}$  (continuous line); the fully transporting discharge  $Q_{FT}$  (dashed line) and the critical discharge for alternate bar formation following *Colombini et al.* [1987],  $Q_{cr}$  (dotted line). See Table 2 for further details.

**Figure 3.** Three examples of Landsat images acquired at different flow stages: a) March 04, 2002,  $Q = 53.5 \text{ m}^3\text{s}^{-1}$ ; b) July 21, 2006,  $Q = 152.5 \text{ m}^3\text{s}^{-1}$ ; c) May 01, 2000,  $Q = 313.0 \text{ m}^3\text{s}^{-1}$ . d) Example of digitized bars of a short reach, pointing out location and definition of bar fronts, bar tails, and bar wavelength. Dotted lines represent digitized bars of LANDSAT L4-5 TM, March 28, 1984,  $Q = 127 \text{ m}^3\text{s}^{-1}$ ; solid lines represent LANDSAT L7 ETM+, July 16, 2010,  $Q = 154 \text{ m}^3\text{s}^{-1}$

**Figure 4.** Bar wavelength of each monitored bar unit on the complete Landsat imagery dataset (1984-2013). Vertical lines represent bends (dashed) and ramps (continuous). Light grey area represents the theoretical wavenumber range of free bars, while dark grey area represents the theoretical range of forced bars.

**Figure 5.** Bar elongation in the period 1999-2010. Length along river centerline refers to bar fronts in 1999. Vertical lines represent bends (dashed) and ramps (continuous).

**Figure 6.** Cumulative bar migration in the period 1999-2010. Each point represents the total migration of single bars. Vertical lines represent bends (dashed) and ramps (continuous).

**Figure 7.** Four examples of bar migration as a function of time in the period 1999-2010. Open symbols refer to migrating bars, closed symbols refer to steady bars. Vertical lines refer to the discharge record of the same period, where the discharge ( $Q$ ) is scaled with the fully transporting discharge ( $Q_{FT}$ ).

**Figure 8.** Bar migration during single floods as function of: i) peak flood discharge; ii) flood duration, considering a threshold equal to  $Q_2$ ; iii) flood flow volume above the threshold discharge  $Q_2$ . Two migrating bars are considered over several flood events: bar 09 (km 35, squared symbols) and bar 23 (km 22, circled symbols) of Figure 7.

**Figure 9.** Cumulative bar migration in the period 1999-2010 as a function of bar wavelength.

**Figure 10.** Bar height for each surveyed cross section as a function of the length along river centerline. Vertical lines represent bends (dashed) and ramps (continuous).

**Table 1.** References, geometric and hydraulic data of the field studies reported in the literature.

Authors	River	$d_{50}$ [mm]	$s$ [m/km]	$W$ [m]	$Q_{mean}$ [ $m^3 s^{-1}$ ]	$L_R$ [km]	$n_{bars}$ [-]	$\Delta T$ [year]
<i>Lewin</i> [1976]	Ystwyth (UK)	0.7 – 42	3.7	36	5.5	0.5	4	2
<i>Welford</i> [1994]	Embarras, Illinois (US)	0.53	0.6	12	0.1	4	-	0.25
<i>Church and Rice</i> [2009]	Lower Fraser, British Columbia (Canada)	17 – 53	0.48	1000 – 2000	3410	50	20	51
<i>Ferguson et al.</i> [2011]	Vedder Canal, British Columbia (Canada)	12 – 35	2 – 5	100 – 240	67	4.7	9	57
<i>Rodrigues et al.</i> [2012]	Loire (France)	0.83	0.25	145 – 200	850	3	2	2
<i>Zolezzi et al.</i> [2012]	Tagliamento (Italy)	40	3.6	840	1400	3	braided	5
<i>Eekhout et al.</i> [2013]	Hooge Raam (The Netherlands)	0.218	0.18	7.5	0.22	0.6	6	3
<i>Jaballah et al.</i> [2015]	Arc (France)	80	6 – 11	35 – 50	12	8	10	30
<i>Rodrigues et al.</i> [2015]	Loire (France)	0.83	0.25	145 – 200	850	3	2	2
present paper	Alpine Rhine (Switzerland-Austria)	20 – 60	1.3 – 2.9	86 – 106	230	41.7	80	30

**Table 2.** Geometrical and hydraulic properties of the three sub-reaches of the Alpine Rhine.  $W$  is channel width,  $d_s$  a representative sediment diameter,  $s$  longitudinal slope,  $Q_{FW}$  is the fully wet discharge,  $Q_{FT}$  the fully transporting discharge,  $Q_{cr}$  the critical discharge for bar formation. Discharge parameters were calculated following *Colombini et al.* [1987].

Sub-reach	Position	Geometry			Discharge		
	from - to [km]	$W$ [m]	$d_s$ [mm]	$s$ [‰]	$Q_{FW}$	$Q_{FT}$	$Q_{cr}$
					[m <sup>3</sup> s <sup>-1</sup> ]		
Upstream	0.00 - 12.27	85	60 - 50	2.9	381	829	1845
Center	12.27 - 30.94	95	50 - 30	2.0	270	628	1942
Downstream	30.94 - 41.70	106	30 - 20	1.3	230	511	1880