

1 **TECHNICAL NOTE: CT CALIBRATION FOR PROTON TREATMENT PLANNING BY**
2 **CROSS-CALIBRATION WITH PROTON CT DATA**

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4
5 **ABSTRACT**

6 **Purpose:** This study explores the possibility of a new method for x-ray computed tomography (CT)
7 calibration by means of cross-calibration with proton CT (pCT) data. The proposed method aims at
8 a more accurate conversion of CT Hounsfield Units (HU) into proton stopping power relative to
9 water (SPR) to be used in proton-therapy treatment planning.

10 **Methods:** X-ray CT scans were acquired on an anthropomorphic phantom, composed of different
11 tissue equivalent materials (TEMs). A pCT apparatus was instead adopted to obtain a reference 3D
12 distribution of the phantom's SPR values. After rigid registration, the x-ray CT was artificially
13 blurred to the same resolution of pCT. Then a scatter plot showing voxel-by-voxel SPR values as a
14 function of HU was employed to link the two measurements and thus obtaining a cross-calibrated x-
15 ray CT calibration curve. The cross-calibration was tested at treatment planning system and then
16 compared with a conventional calibration based on exactly the same TEMs constituting the
17 anthropomorphic phantom.

18 **Results:** Cross-calibration provided an accurate SPR mapping, better than by conventional
19 calibration. The dose distribution of single beams optimized on the reference SPR map was
20 compared with the recalculations computed on cross-calibrated CT, showing minor deviation at the
21 dose fall-off, with range uncertainty lower than 1%.

22 **Conclusions:** The presented data demonstrated that, by means of reference pCT data, a
23 heterogeneous phantom can be used for CT calibration, paving the way to the use of biological
24 samples, with their accurate description of patients' tissues. This overcomes the limitations of
25 conventional CT calibration requiring uniform samples, which can be only obtained by synthetic
26 TEMs, which fails in accurately mimicking the properties of biological tissues. Once a
27 heterogeneous biological sample is provided with its corresponding SPR maps, a cross-calibration
28 procedure could be adopted by other PT centers, even when not equipped with a pCT system.

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31 **Keywords:** CT; proton CT; proton therapy
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34 INTRODUCTION

35 In proton therapy (PT), the dose computation is based on x-ray computed tomography (CT)
36 images of the patient, which are acquired to account for the effect of tissue inhomogeneity. The CT
37 Hounsfield Units (HU) are converted by a CT calibration into proton stopping power ratio (SPR),
38 relative to water. The proton SPR is then used for dose computation in the treatment planning
39 systems. Uncertainties in proton range can have a profound effect on proton treatments and one of
40 the main sources of uncertainty is currently represented by inaccuracies in the CT calibration.¹
41 Since range uncertainty is still an unresolved issue in PT it is a common practice to assume an
42 uncertainty of about 3% in the estimated particle range, compensating for that in the planning phase
43 and thus leading to an increased volume of healthy tissue being irradiated. In principle, by
44 decreasing the uncertainty on the proton estimated range with an improved CT calibration method,
45 it would be possible to significantly reduce the irradiated healthy tissues surrounding the tumour,
46 thus obtaining an increased treatment conformity.

47 For these reasons, different methods for x-ray CT calibration are under continuous
48 investigation.^{2,3,4} Conventionally, single-energy CT calibration is obtained by scanning a number of
49 tissue equivalent materials (TEMs), which have limitations in mimicking the properties of real
50 tissues. To partially overcome that issue, a stoichiometric calibration has been proposed or, more
51 recently, dual-energy CT methods were investigated.^{2,3,5} In general, in these methods the CT
52 calibration is a procedure performed in two steps.⁶ The first step involves the computation of the
53 relative electron or mass density and in some cases of the effective atomic number. The second step
54 consists in the translation of such quantities into proton SPR by an heuristic function, which
55 depends on specific material related properties such as the mean excitation energy. In principle,
56 accurate SPR maps could be directly obtained by proton computed tomography (pCT), thus
57 overcoming any limitation in the accuracy of such two-steps procedures. Unfortunately, clinically
58 approved pCT systems are not yet available to be routinely used on patients.

59 Direct methods for CT calibrations were proposed in a few studies. Those methods are based
60 on the use of additional water equivalent thickness (WET) measurements to determine a
61 relationship between CT numbers and SPR. Schneider et al⁷ anticipated this intriguing concept in an
62 experimental model, by optimizing x-ray CT calibration using in-vivo proton radiography. This
63 method operates in the projection-domain, being based on the use of projected images (proton
64 radiographies, 2D) to optimize the HU-SPR conversion. In successive studies, the combination of
65 x-ray CT with WET data was investigated in different scenarios. CT was optimized by i) one-
66 dimensional data obtained by range probing on biological phantoms,⁸ ii) in the projection-domain,
67 two-dimensional data obtained by proton radiography (theoretically^{9,10,11} and experimentally⁸

68 investigated) and finally, iii) multiple two-dimensional data obtained by multiple projection proton
69 radiography on a tissue equivalent phantom.¹² In this context it is reasonable to expect that
70 increasing the quantity of additional WET data, from 1D to multiple 2D, may allow an improved
71 and more robust solution to obtain an optimized x-ray CT calibration curve and that the best
72 performances could be obtained by full 3D data, i.e. by pCT. Methods that work with the pixel
73 values in 3D pCT reconstructed images can be considered as image-domain methods. So far, the
74 most advanced dual-energy CT methods were compared with pCT,¹³ but pCT has never been used
75 to optimize x-ray CT calibration.

76 In the present preliminary study, we aim to investigate the possibility of x-ray CT calibration
77 by cross-calibration with pCT data, presenting and discussing a first image-domain methodological
78 approach on a synthetic anthropomorphic phantom. Even though pCT is not yet clinically available,
79 it has been experimentally developed and it could be used to scan suitable biologic phantom to be
80 used to cross calibrate x-ray CT for PT treatment planning.

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85 MATERIALS AND METHODS

86 Proton and x-ray CTs were acquired on a neck portion of the head anthropomorphic
87 phantom Model 731-HN (CIRS, Inc., Norfolk, VA, USA), composed of different TEMs. Small
88 uniform cylinders (length 50mm, \varnothing 30 mm) were also available for the TEMs, separately from the
89 head phantom.

90 A detailed description of our pCT apparatus with tomographic reconstructions is reported
91 elsewhere.¹⁴ In summary, the pCT system is made of four planes of silicon microstrip tracker and a
92 YAG:Ce scintillating calorimeter. The object to be imaged is placed on a remotely controlled
93 rotating platform, between the second and third tracker plane, while the calorimeter is positioned
94 just after the fourth plane. For each proton, the tracker reconstructs the two trajectory segments
95 upstream and downstream of the phantom, while the calorimeter measures the residual energy. A
96 number of protons of the order of 10^8 while rotating the phantom in 400-800 angle positions were
97 acquired. Thus an algebraic iterative algorithm was applied to reconstruct SPR 3D distribution, with
98 voxel size $0.6 \times 0.6 \times 0.8 \text{ mm}^3$.

99 Conventional x-ray CT scans were acquired at single energy (120 kV) in a 512×512 matrix
100 with voxel size $0.8 \times 0.8 \times 1.0 \text{ mm}^3$ by a big bore Brilliance CT scanner (Philips Medical Systems,
101 Cleveland, OH, USA).

102 Cross calibration was obtained after pCT and x-ray CT data alignment by rigid registration,
103 which is legitimate when using non-moving phantoms. Image processing was performed by
104 MATLAB® (The MathWorks.inc, Natick, MA, USA). After rigid alignment of the data by an
105 intensity-based method, a volume of interest was selected considering all the voxel with $\text{SPR} > 0.5$ in
106 the pCT images. In order to account for the different image quality of the two modalities, the x-ray
107 CT was artificially blurred with an averaging filter to degrade the spatial resolution to a level
108 comparable to the lower resolution of pCT. A scatter plot was then obtained showing the voxel-by-
109 voxel SPR versus HU values, which were used to extract the calibration curve. In details, the data
110 points belonging to the volume of interest were sorted according to increasing HU and grouped in
111 equal-sized bins. For each bin, the mean values of the SPR was calculated and plotted against the
112 corresponding mean HU values. The CT calibration curve is thus obtained by the line connecting
113 the resulting mean data points. The effect of different bin sizes was preliminarily assessed,
114 considering that a small bin size corresponds to few data points and a resulting noisy lookup table,
115 while too large bins might smooth significant variations in the HU-SPR relationship.

116 Differential maps were computed to perform a consistency test of the procedure. In details,
117 the calibration curve obtained by cross-calibration was used to compute the synthetic SPR map,
118 which was compared with the reference SPR map measured by pCT by means of a differential map.

119 A difference map was also computed between the synthetic SPR map obtained by conventional x-
120 ray CT calibration (see details below) minus the reference SPR map measured by pCT.

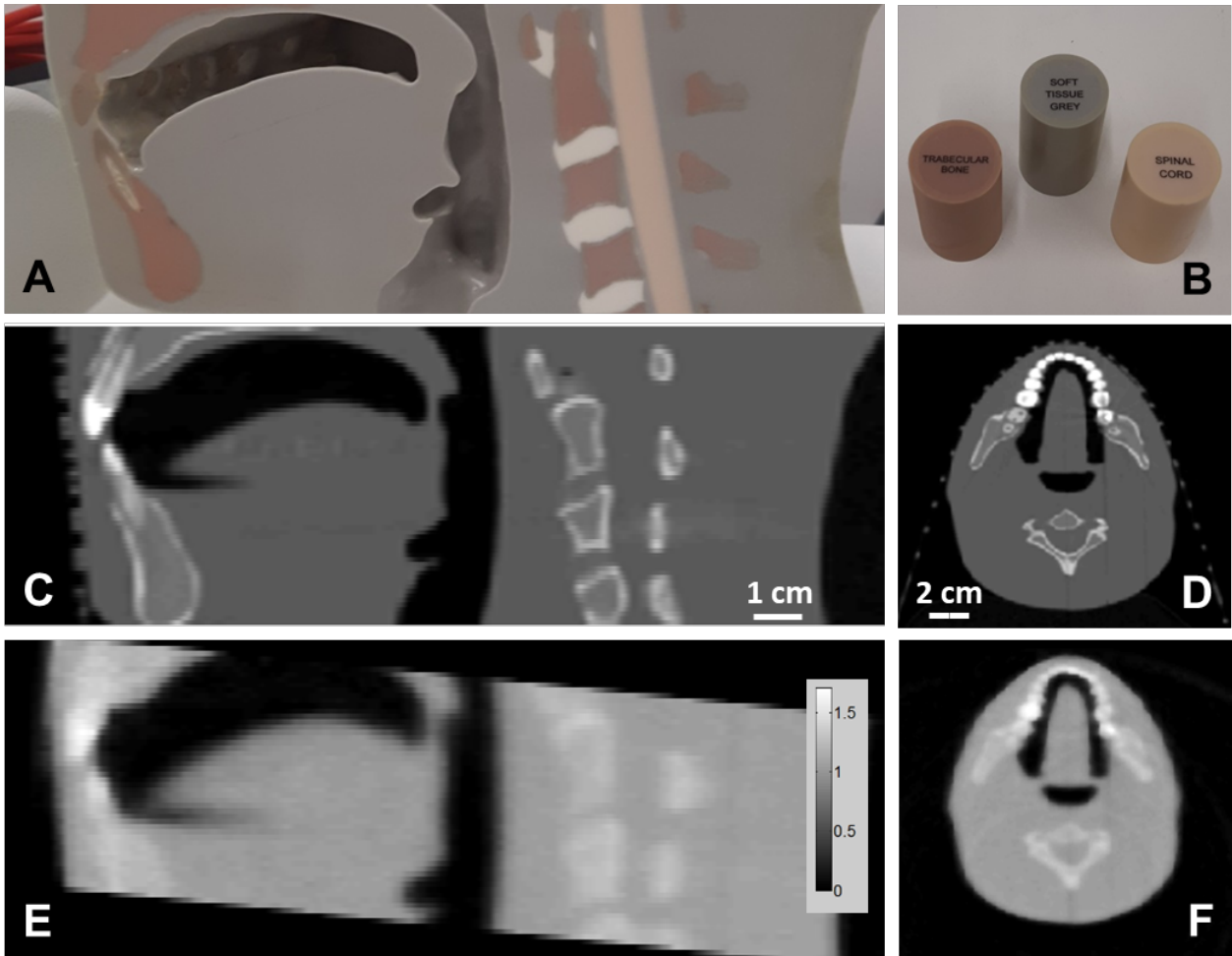
121 The cross calibration procedure was verified on a commercial (RaySearch Laboratories,
122 Stockholm, Sweden) treatment planning system (TPS). At TPS, the delivery of uniform dose by a
123 single proton beam optimization (SFO) to an exemplary target was simulated. SFO is best suited to
124 visualize range difference as there is a single distal surface of the dose volume and distal energy
125 layers have the highest weight. On the other hand, it is worth mentioning that multi field
126 optimisation has become clinical routine¹⁵ and the effect of range uncertainties can be slightly
127 different in that case. The optimization was run on the SPR map obtained from pCT images. The
128 dose delivered by the obtained spot distribution was then recalculated using the SPR map derived
129 from X-ray CT images by i) CT cross-calibration and ii) conventional x-ray CT calibration. The
130 latter was obtained exploiting the uniform cylinders made of the same TEMs as the head phantom.
131 For this purpose, the cylinders were inserted in the corresponding holes of a plastic water phantom
132 (180 mm diameter, 50 mm length) and scanned with the same x-ray CT acquisition protocol used
133 for the head phantom. A small region of interest was drawn on each cylinder and the corresponding
134 mean HU values were calculated. Starting from the mass density of the TEMs and the
135 corresponding mean HU, a standard CT calibration curve was obtained at the TPS. The conversion
136 of mass density into SPR is then performed by the TPS, by means of a dedicated algorithm
137 checking on a list of about fifty fixed materials,¹⁶ created by interpolation from a number of well-
138 established core materials. Each CT voxel is thus associated with the material closest in mass
139 density and its atomical composition as well as the mass density associated to the voxel is used to
140 compute the SPR.

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143 **RESULTS**

144 A section of the head anthropomorphic phantom is shown in **Figure 1A**, where the different
145 TEMs are visible in different colours (soft tissue in grey, spinal cord in yellow and trabecular bone
146 in brown). For these three types of TEMs a corresponding uniform rod cylinder was available
147 (**Figure 1B**), which was used for validation measurements. In the head phantom section there are
148 other visible TEMs, such as vertebral disk (in white) and a thin cortical layer (in grey). However,
149 for these tissue types a rod TEMs was not available to perform a corresponding validation.



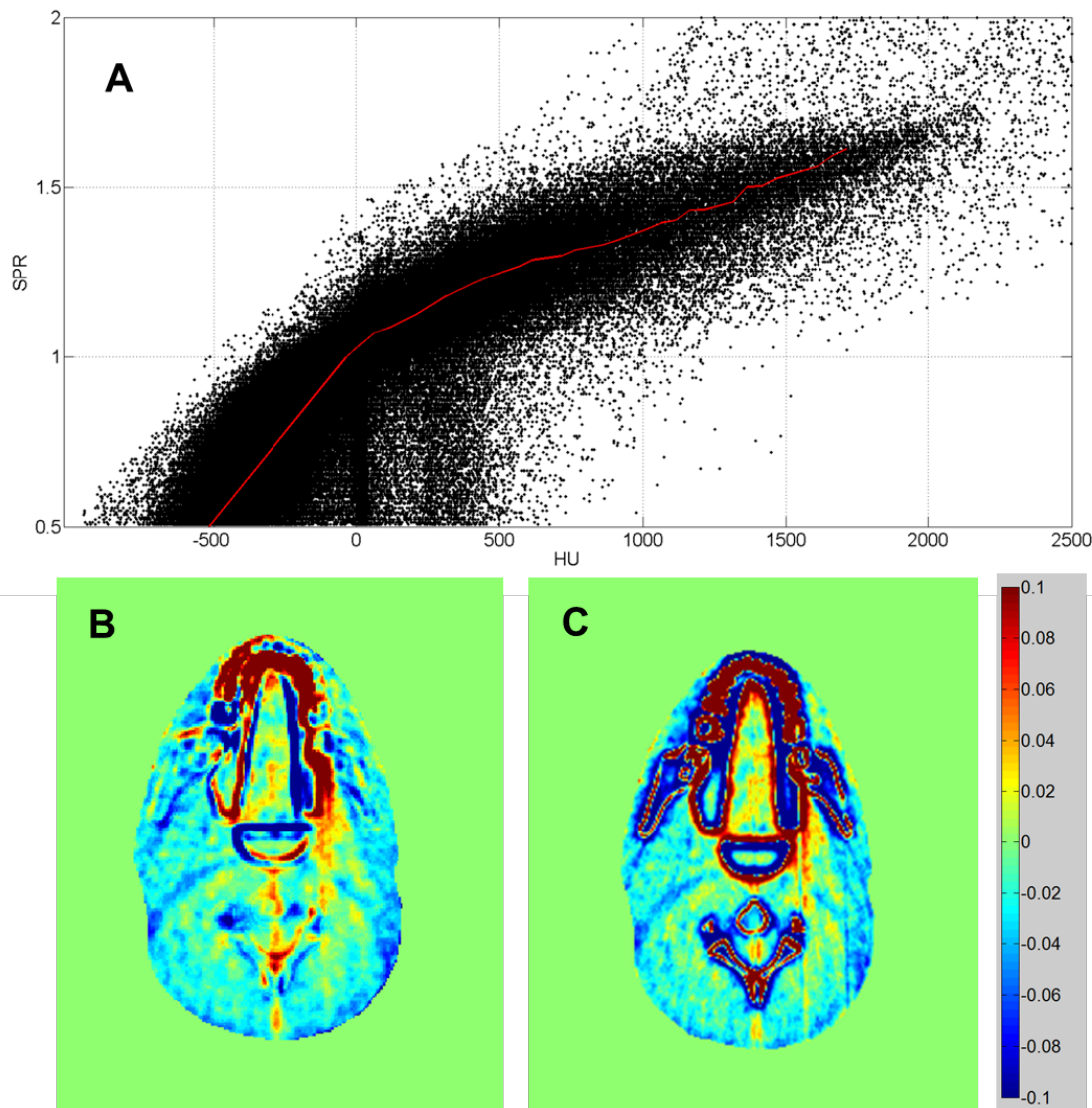
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151 **Figure 1.** A section of the head anthropomorphic phantom Model 731-HN (A), made of different
152 tissue equivalent materials (TEMs). Small uniform cylinders available for three of the TEMs (B),
153 i.e. soft tissue (1.05 g/cm³), spinal cord (1.07 g/cm³) and trabecular bone (1.16 g/cm³). X-ray CT
154 sagittal (C) and axial (D) projections. Proton CT sagittal (E) and axial (F) projections. In (E) the
155 greyscale represent SPR values.
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157 The x-ray CT images (**Figure 1C-D**) were registered with pCT images (**Figure 1E-F**), thus
158 obtaining a voxel-by voxel correspondence between HU and SPR, as reported in a scatter plot
159 (**Figure 2A**).

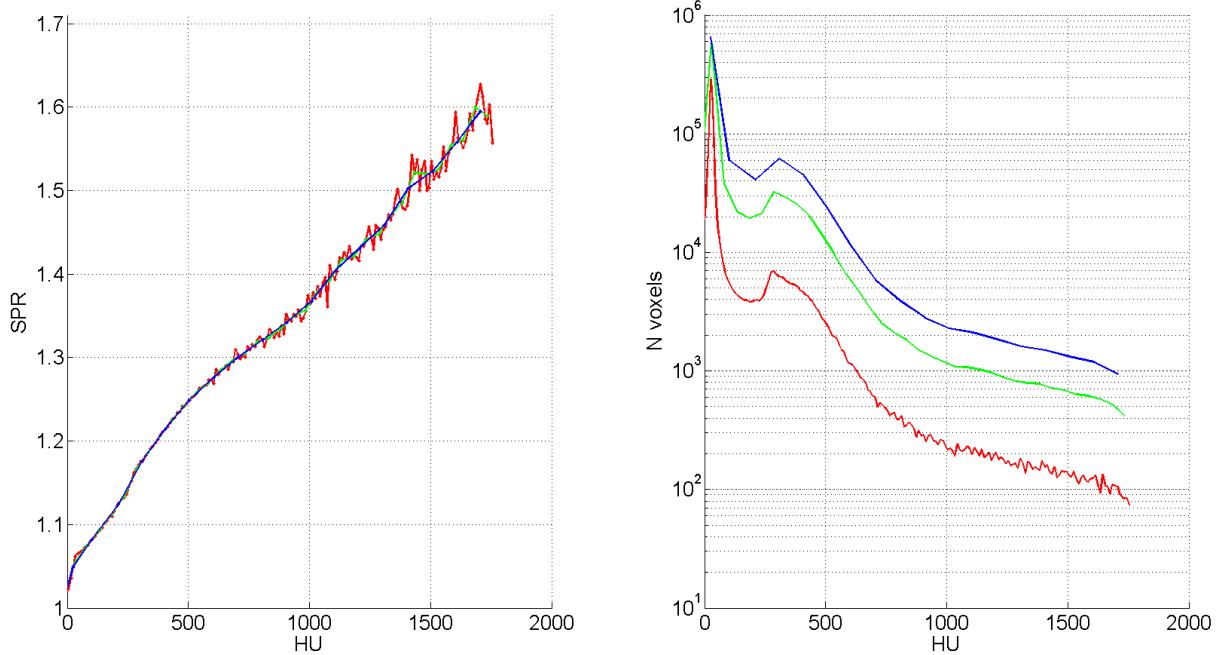
160 The effect of different bin size to obtain the calibration curve was preliminarily assessed at
161 10, 50 and 100 HU (**Figure 3**), confirming that increasing bin size may produce undesired

162 smoothing, while reducing bin size introduces noise in the calibration curve. According to the
163 reported data, a bin size collecting around 500 voxels (i.e. around 0.3 cm^3), with bins spaced every
164 50 HU seems to produce an acceptable curve. That volume could be reduced by decreasing the
165 noise in the source data, e.g. by increasing the CTs acquisition time. The calibration curve obtained
166 by 50 HU bin size is also shown in **Figure 2A** and it has been used in the following.

167 Differential maps of the synthetic SPR map minus the measured pCT were computed to
168 perform a consistency test of the procedure and are reported in **Figure 2B-C**. They evidenced a
169 better agreement by the calibration obtained by cross-calibration with respect to that obtained by
170 conventional x-ray CT calibration.

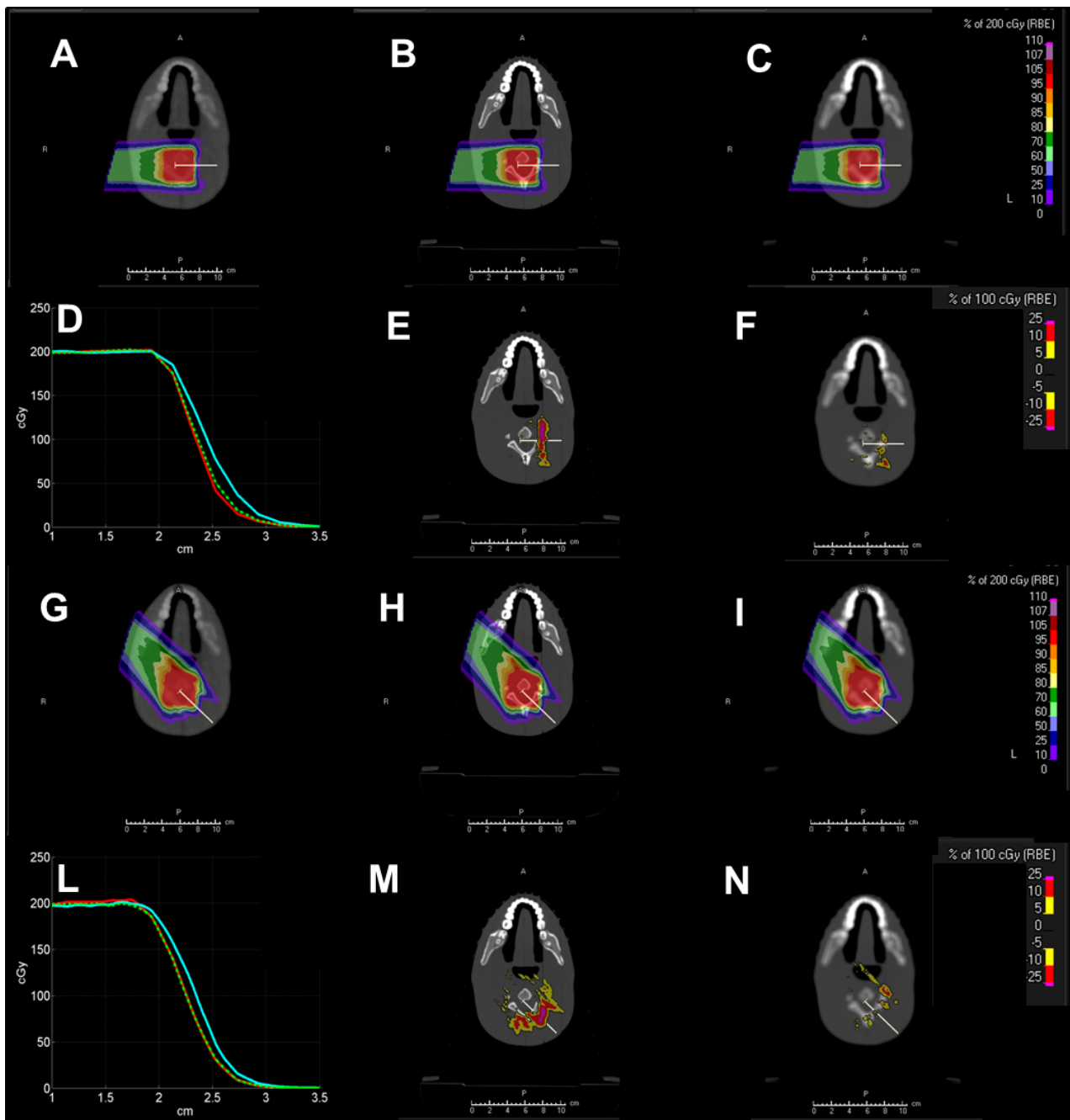


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172 **Figure 2.** Proton CT SPR vs HU x-ray scatter plot (A). The calibration curve obtained by cross-
173 calibration is shown as a red line. Difference between the SPR map obtained by cross-calibration
174 minus the SPR map obtained by pCT (B). Difference between the SPR map obtained by
175 conventional x-ray CT calibration minus the SPR map obtained by pCT (C).
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 178 **Figure 3.** At the left, the calibration curves obtained by a bin size of 10HU (red line), 50HU (green)
 179 and 100HU (blue) are shown. At the right the corresponding number of averaged voxels is reported.
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181 The cross-calibration was also compared with the standard CT calibration at TPS. The dose
 182 comparison is shown in **Figure 4** for a lateral beam and for an anterior-oblique beam optimized on
 183 the SPR map arising from pCT images, then recalculated on the SPR map arising from X-ray CT
 184 images by conventional CT calibration and by CT cross-calibration. On both the lateral beam and
 185 the anterior-oblique beam, compared to the results obtained with the pCT-based SPR map, the dose
 186 profile along a line crossing the isocenter showed a slight shift of around 1 mm at a depth of 100
 187 mm (i.e. the range uncertainty was around 1%) of the dose fall-off on the SPR map obtained by the
 188 conventional CT calibration and almost no shift with the cross-calibration (**Figure 4D, L**). On the
 189 oblique beam, the range of the dose fall-off on the conventionally calibrated CT was around 1%
 190 longer than on pCT, while on the cross-calibrated CT it was less than 1% shorter (**Figure 4H**). With
 191 the conventional calibration, on both the lateral beam and the anterior-oblique beam, dose
 192 difference maps evidenced a range shift on the distal side (**Figure 4E,M**). Correspondingly, a
 193 marked reduction in the difference was observed by using the cross calibration (**Figure 4F,N**).
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196 **Figure 4.** The dose distribution obtained with a single lateral (A-F) and a single oblique anterior
 197 (G-N) beam optimized on the SPR map arising from pCT (A, G) was recomputed on the SPR maps
 198 obtained by conventional x-ray CT calibration (B, H) and by cross-calibration (C, I). The
 199 corresponding dose profile along the white line in (A-C) and (G-I) are shown in (D, L), where the
 200 red continuous line corresponds to the dose (A, G), the cyan continuous line to (B-H) and the
 201 dashed green line to (C, I). Dose difference maps between A and B is shown in E, between A and C
 202 in F, between G and H in M and between G and I in N.

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205 **DISCUSSION**

206 In this note we present the proof of concept of an innovative approach to perform x-rays CT
207 calibration by means of a cross calibration with pCT data. The reported validation and consistency
208 tests demonstrated that by cross-calibration with pCT an heterogeneous sample can be used, without
209 needing homogeneous TEMs. In the reported tests, the resulting range uncertainty was around 1%
210 or lower and therefore smaller than the range uncertainty typically adopted in robust proton
211 treatment planning (around 3-3.5%).

212 It is worth noting that the conventional CT calibration was obtained by using exactly the
213 same material that composes the phantom, thus providing an accurate calibration. This condition
214 cannot be replicated with a real patient, as uniform samples of the corresponding tissue are not
215 available.

216 Indeed, the main advantage of the cross-calibration method lies in the possibility to use a
217 heterogeneous phantom for CT calibration instead of a phantom made of uniform samples, as
218 required by conventional CT calibration. Uniform samples can be obtained with synthetic TEMs,
219 but unfortunately they have limitations in mimicking the radiological properties of real biological
220 tissues. Besides that, a heuristic function must then be applied to compute the SPR at the end of the
221 two-step procedure to translate HU into SPR.

222 A calibration of the x-CT system directly using animal tissues of known SPR would produce
223 the most reliable calibration curves. Since biological tissues are intrinsically heterogeneous, a
224 uniform biological sample might be obtained only by homogenizing tissue samples, which would
225 mix all the different components, thus modifying the tissue structure and properties. On the
226 contrary, by pCT cross-calibration an actual tissue portion, even though markedly heterogeneous,
227 could be used for the calibration procedure.

228 In this perspective, the main issue in the calibration chain would be the availability of a
229 biological phantom. The production of stable phantoms is crucial in this respect. In a research
230 project funded by the Istituto Nazionale di Fisica Nucleare (INFN), a set of dedicated biological
231 phantoms will be designed and prepared. Once a customized and stable biological phantom will be
232 available, this calibration procedure could be easily extended to other PT centres not equipped with
233 a pCT system. This could be done by shipping the stable biological phantom to the remote centre
234 for an acquisition with the x-CT systems to be calibrated, while having the corresponding SPR
235 maps already reconstructed from pCT. The SPR map and the x-ray CT HU will be then processed
236 and a calibration function for the remote x-CT system can be extracted. A possible flowchart is
237 summarized in supplementary **Figure S1**, assuming a unique service provider (of the biological

238 phantom plus pCT data and cross-calibration software) supporting the calibration of a x-ray CT of a
239 generic remote PT centre.

240 The proposed method is based on an accurate image registration followed by the association
241 between measured SPR and HU. The method was refined by artificially blurring the x-ray CT
242 image to degrade the spatial resolution to a level comparable to the proton CT and only then
243 extracting the voxel-wise value pairs for further processing. A more sophisticated approach would
244 be to explicitly formulate the image formation process in both modalities and, based on that, to
245 devise a cost function, which compares the two images, to be minimized. Similar approaches have
246 been used in the literature when combining x-ray CT and proton radiography. Alternatively, voxel
247 based method by the concept of machine learning could be developed, in which part of the data is
248 used to train (optimize) a model which is then applied on the remaining HU data to predict the SPR
249 values. Those methods are under investigation for conversion of magnetic resonance imaging data
250 to HU maps relevant for radiotherapy planning,^{17,18} i.e. to generate the so called synthetic-CT (or
251 pseudo-CT or similar).

252 Finally, it is worth noting that there are uncertainties in the x-ray image itself that are not
253 related to the calibration. These uncertainties may originate from imperfections in the x-ray CT
254 acquisition and reconstruction including e.g. beam hardening artefacts. In fact, these latter cause
255 HU values of the same material to vary as a function of position within the image. Since the
256 proposed method relies on a lookup table (as current clinical methods do), it is intrinsically unable
257 to correct for spatially dependent uncertainties in the image. However, beam hardening and
258 correction of imperfection in CT images is an intense field of research and it is reasonable to expect
259 that CT image quality will be further improved in the future.

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261 **CONCLUSIONS**

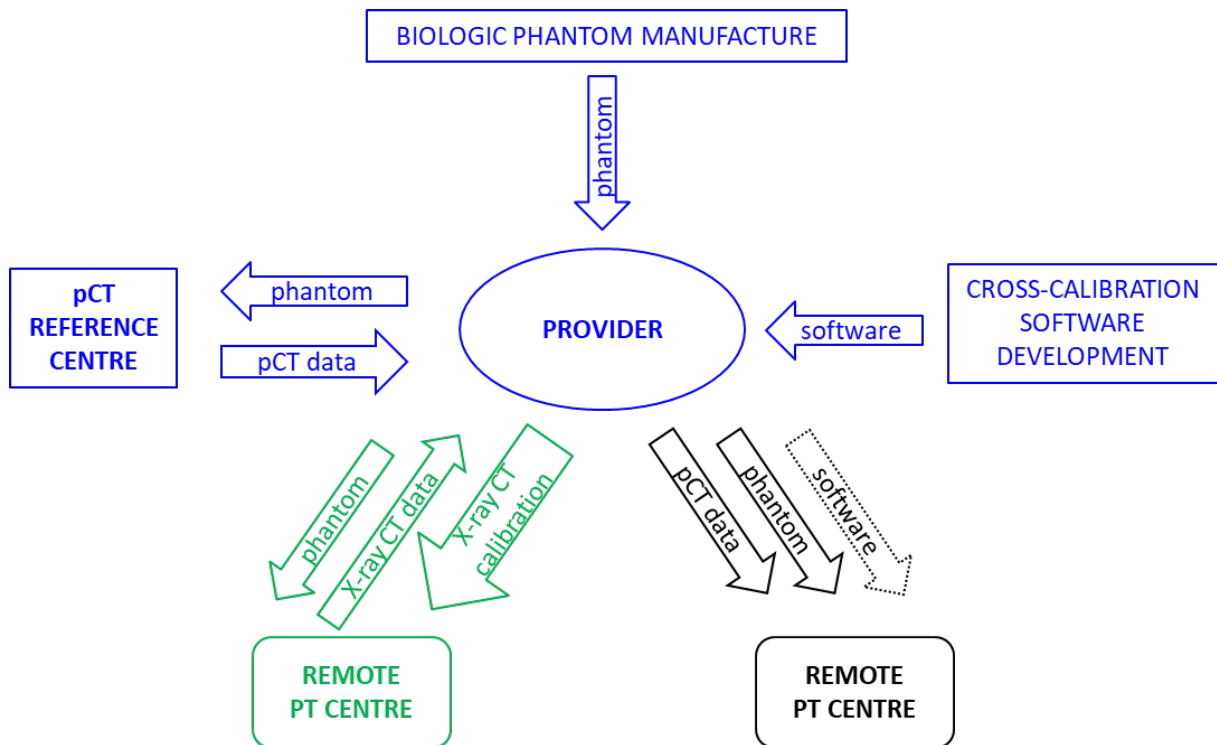
262 The data presented can be considered as a proof-of-principle of a new methodological
263 approach for CT calibration that, based on pCT data, allows using heterogeneous phantom for CT
264 calibration. This method overcomes the drawback of conventional CT calibration requiring
265 homogeneous samples, which can be only obtained by synthetic TEMs. These TEMs are associated
266 to limitations in the accurate mimicking the properties of biological tissues. The proposed method
267 paves the way to the use of heterogeneous biological tissues for CT calibration, obtaining a more
268 accurate description of patients' tissues by means of improved SPRs values. As a direct
269 consequence of the reduced uncertainty, this might eventually translate into the possibility of
270 delivering more conformal PT treatments. The same procedure could be easily adopted by other PT
271 centers, even when not equipped with a pCT system.

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274 **DISCLOSURE OF CONFLICTS OF INTEREST**

275 Authors have no conflict of interest to declare.



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Figure 4. A possible flowchart with a unique service provider facing a generic remote proton therapy (PT) centre. The provider (blue blocks) might outsource biologic phantom manufacture, development of the cross-calibration software and pCT acquisition of the phantom. When facing with the remote centre, the provider might ship both the phantom and the corresponding pCT data (black blocks) with or without (if the remote centre prefers to develop his own procedure) the cross-calibration software (dotted line). Alternatively (green blocks), the provider might ship only the phantom, the remote centre might acquire the x-ray CT data and send them to the provider who might finally transmit the computed CT calibration.

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