



## Sintering of mixed Ca–K–Na phosphates: Spark plasma sintering vs flash-sintering



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### ARTICLE INFO

#### Keywords:

Calcium phosphates  
Ceramic  
Flash-sintering  
Spark plasma sintering

### ABSTRACT

A comparison between different field-assisted sintering methods (FAST), namely Spark Plasma Sintering (SPS) and flash-sintering (FS), is reported for calcium and alkaline phosphates especially with regards to their microstructure. A reduced average grain size upon SPS is shown when pressure is decreased. Shrinkage curves during flash sintering are compared with similar conventional sintering curve. Flash sintered ceramics possess unusual microstructural features, including a density/grain size gradient where the surface of the specimen is denser and possesses a coarser grains with respect to the core. Such microstructural gradient is opposite to what generally observed, the surface being colder due to the heat radiation toward the environment. The change in the average grain size for each sintering method is related to the process parameters.

### 1. Introduction

Sintering of calcium phosphates for bone implants is still a non-trivial task despite a fairly large number of publications on this topic [1–4]. This problem is especially acute in the case of substituted calcium phosphates, which show a suitable level of resorption in the body and also have sufficient strength to produce bone replacement implants.

However, obtaining strong ceramics based on substituted Ca–K–Na phosphate is challenging because of the difficulties of their sintering. The main difficulty in sintering is the predominance of recrystallization processes over densification. Grains grow fast because at high temperature (above 600 °C) these materials become cationic-conductors [5]. At the same time, phosphate-anions do not have to move, they just have to reorient to start to belong another grain. However, densification process goes very slow because here phosphates diffusion plays more important role while their mobility is still much lower comparing to cation mobility. The noticeable difference in mobility between cations such as calcium, potassium and sodium and phosphate anions was shown and discussed in numerous works concerning alkali metals and phosphate based ceramic conductors [5–8]. As a result, the microstructure of the resulting ceramics consists of relatively large grains, and pores are observed in a

significant amount [5,9,10]. To improve densification, pores should go out of grains to dissolve on a grain boundary but, due to fast coarsening and relatively low mobility of big phosphate anions, pore-grain boundary separation occurs, and they do not stay on grain boundary enough time to dissolve.

Possible methods for solving this problem have been discussed for a long time in the scientific literature. As such, it was proposed to use both modifications of traditional consolidation methods (for example, multi-step sintering [11,12], reaction sintering [10,13]) and methods involving additional factors, for example, an electromagnetic field - FAST (Field Assisted Sintering Techniques) methods - such as Spark Plasma Sintering (SPS) [14–18] and Flash Sintering (FS) [19–23]. SPS is a consolidation technology where a moderate electric potential (<10V) is used to Joule heat a graphite die that contains the ceramic powder, while an external pressure is applied to promote densification. Being the electric potential quite low, most of the electric current passes through the graphite die when processing ceramic materials. Conversely, FS is a pressureless technique which adopts much larger electric field (from a few to 10<sup>3</sup> V/cm). In FS experiments whole the electric current is forced to pass through the ceramic while sintering.

The multi-step sintering allows to form grains contact and stop exceed

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**Table 1**  
Characteristics of phase transitions in  $\text{CaK}_{0,6}\text{Na}_{0,4}\text{PO}_4$  taken from Ref. [5].

	$T_{p,L}, ^\circ\text{C}$	$\Delta V_{p,L}, \%$	$\Delta H_{p,L}, \text{kJ/mol}$
$\text{CaK}_{0,6}\text{Na}_{0,4}\text{PO}_4$	667	-0,1	1,4

coarsening and simultaneously maintain the densification by decreasing sintering temperature. However, in case of mixed calcium and alkali metals phosphates which are ion conductor above  $660^\circ\text{C}$  coarsening always prevails over densification [5]. As a result, it is not possible to reach the temperature at which the predominant mechanism changes and the pores begin to dissolve faster than grain growth occurs [24].

In contrast to conventional sintering, consolidation methods using an electric field are distinguished by the fact that, in addition to the temperature factor, sintering is promoted by the application of electric current and field. In the case of SPS, densification is further enhanced by the external pressure which increases the driving force for sintering. The result is, in many cases, a significant densification of the ceramic without noticeable grain growth. Thus, model ceramic systems such as  $\text{Al}_2\text{O}_3$  [25, 26],  $\text{ZrO}_2$  [27–29], and also compounds with apatite structure such as HA were effectively densified (relative density > 95%) in the minutes timescale maintaining nanometric grains [15,16,23,30,31]. Recent studies [30,32–35] have shown that similar methods can also be successfully applied to tricalcium phosphate, which raises the question of the possible expediency of their application for the preparation of dense

ceramics based on mixed calcium and alkali metal phosphates.

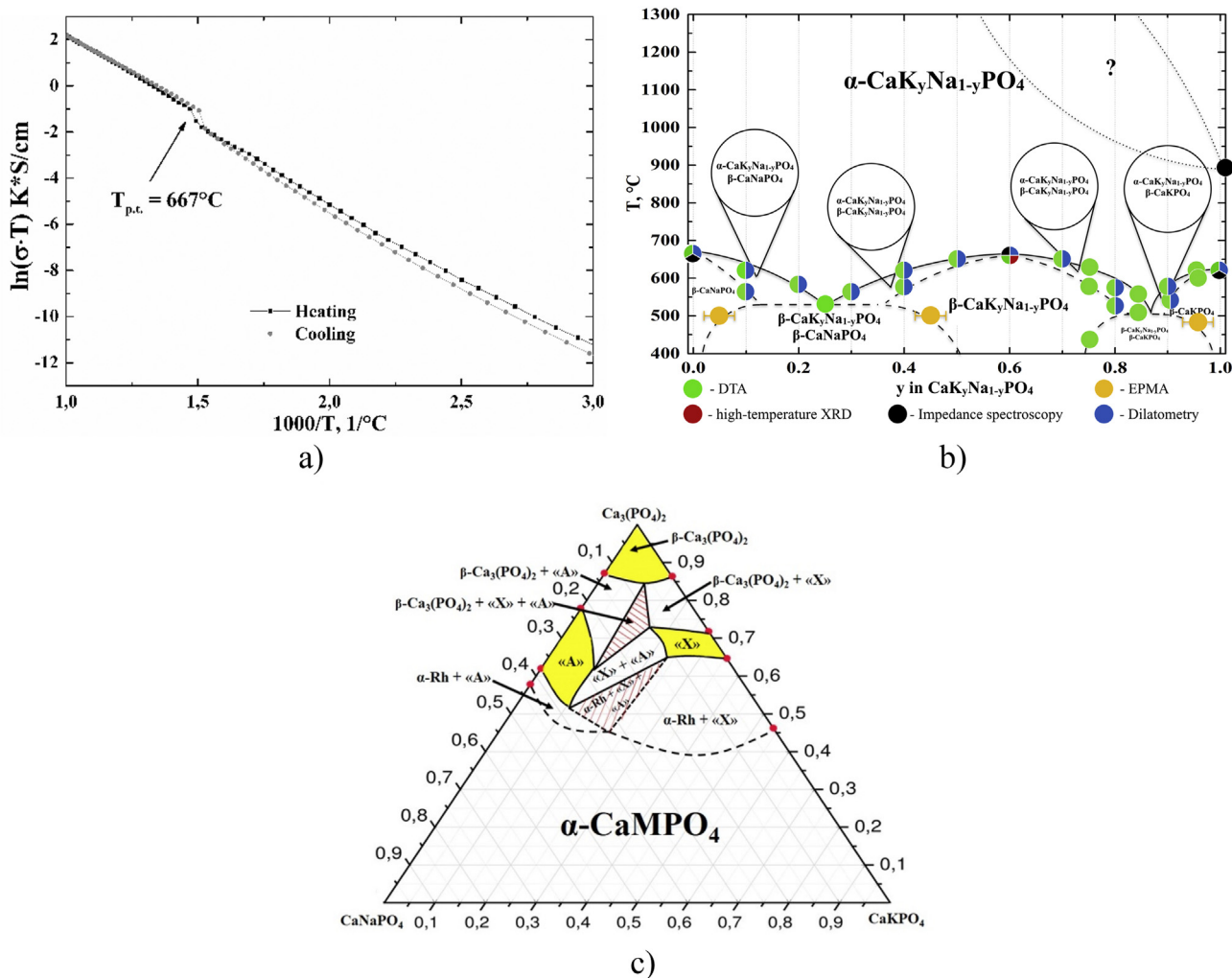
The aim of the present work is to compare two different field-assisted sintering technologies, namely spark plasma sintering and flash sintering, for the consolidation of phosphate ceramics with  $\text{CaK}_{0,6}\text{Na}_{0,4}\text{PO}_4$  composition. Such material is a promising formulation to make resorbable bioceramics for bone tissue regeneration.

**2. Experimental procedures**

To determine the possibility of using spark plasma sintering and flash sintering to obtain dense ceramics based on mixed calcium and alkali metal phosphates, the model composition  $\text{CaK}_{0,6}\text{Na}_{0,4}\text{PO}_4$  was chosen due to the fact that it has only one phase transition at  $667^\circ\text{C}$  with minimal negative volumetric effect (Table 1) (which was established quite accurately in Refs. [5,36,37] by dilatometry and measuring the temperature dependence of conductivity (Fig. 1a). Moreover, there is room for solid solution based on  $\beta\text{-CaK}_{0,6}\text{Na}_{0,4}\text{PO}_4$  spread in the widest part between  $\text{CaK}_{0,38}\text{Na}_{0,62}\text{PO}_4$  and  $\text{CaK}_{0,82}\text{Na}_{0,18}\text{PO}_4$  (Fig. 1b).

In addition, this compound contains all types of ions that are usually present in substituted calcium-phosphate ceramics - calcium, potassium, sodium and phosphate (Fig. 1c), which makes it possible to study the effect of each of them on the sintering process, namely, their diffusion mobility upon sintering and promoting densification.

Mixed ternary phosphate  $\beta\text{-CaK}_{0,6}\text{Na}_{0,4}\text{PO}_4$  was synthesized from Sigma-Aldrich precursors (p.a.) via the following reactions:



**Fig. 1.** a) Arrhenius plots for ionic conductivity in  $\text{CaK}_{0,6}\text{Na}_{0,4}\text{PO}_4$  (taken from Ref. [5] with small changes), phase diagrams b)  $\text{CaNaPO}_4$  -  $\text{CaKPO}_4$  (taken from Ref. [5] with small changes), c)  $\text{Ca}_3(\text{PO}_4)_2$  -  $\text{CaNaPO}_4$  -  $\text{CaKPO}_4$  ( $T = 1200^\circ\text{C}$ ) (taken from Ref. [9] with small changes).

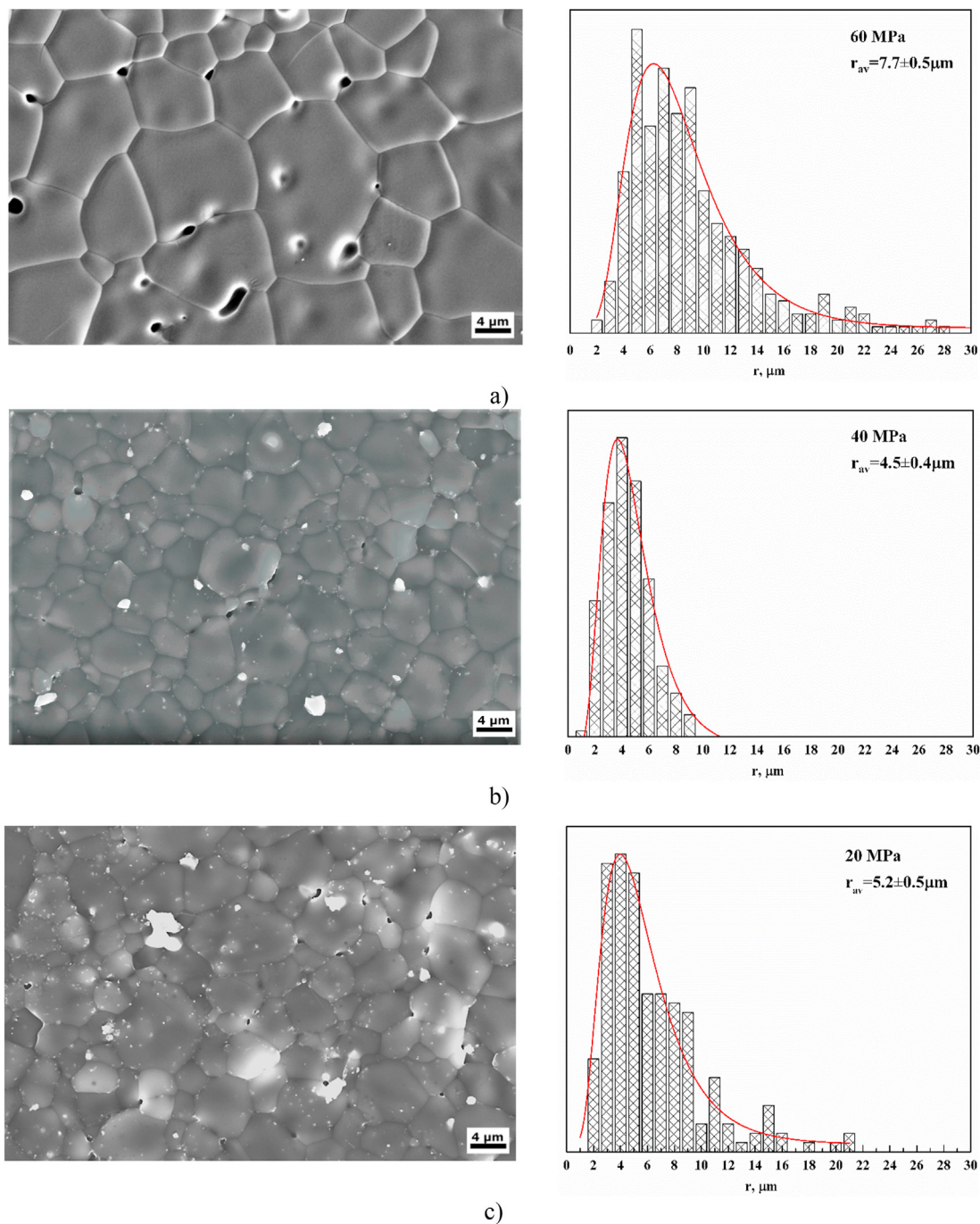
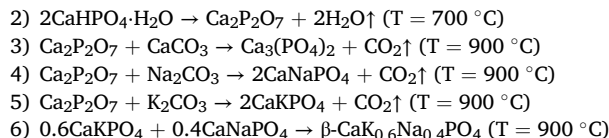
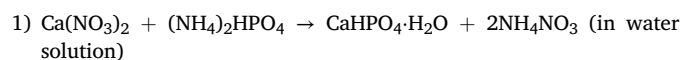


Fig. 2. Microstructure and grain size distribution of  $\beta\text{-CaK}_{0.6}\text{Na}_{0.4}\text{PO}_4$  ceramics after SPS at different pressures a) 60MPa, b) 40MPa, c) 20MPa.

Table 2

$\beta\text{-CaK}_{0.6}\text{Na}_{0.4}\text{PO}_4$  ceramic characteristics after conventional and two-step sintering [5].

	Schedule	Relative density, %	Average grain size, $\mu\text{m}$
Conventional sintering	1200°C, 12 h	92%	20
Two-step sintering	1200°C, 0 min, 1100°C, 48 h	85%	20



The synthesis of mixed ternary phosphate has been described in detail in previous works [5]. First brushite was synthesized in water solution from the soluble salts calcium nitrate ( $\text{Ca}(\text{NO}_3)_2 \cdot 4\text{H}_2\text{O}$ , 0.6 M) and ammonium hydrophosphate ( $(\text{NH}_4)_2\text{HPO}_4$ , 0.6 M) and then calcium pyrophosphate was obtained by firing at  $700^\circ\text{C}$ . Tricalcium phosphate and potassium and sodium rhenanites were obtained by mixing calcium pyrophosphate with the respective carbonates and then firing at  $900^\circ\text{C}$ ,



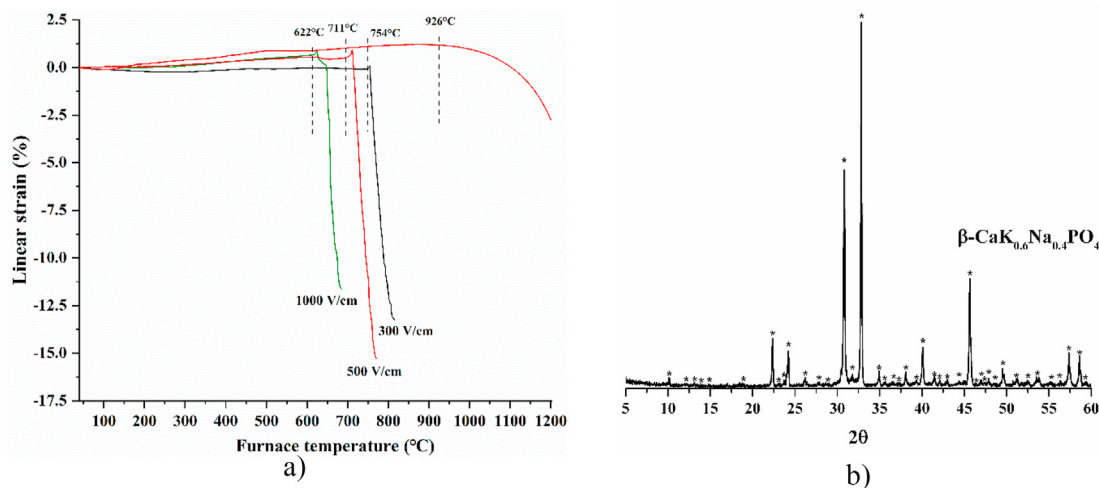


Fig. 3. a) Linear strain during flash sintering and conventional sintering vs furnace temperature; b) XRD of the sample after flash-sintering at 1000 V/cm (\* - peaks specific to the low-temperature phase).

from which mixed calcium and alkali phosphates were obtained by firing at 900 °C.

The mixtures of reactions 2–6 were ground in a planetary ball mill (Pulverisette, Fritsch, Germany) for 10 min (4000 rpm) in an acetone medium and then dried in air and calcined in Al<sub>2</sub>O<sub>3</sub> crucibles. The obtained powders were analyzed by XRD analysis.

In the SPS approach,  $\beta$ -CaK<sub>0.6</sub>Na<sub>0.4</sub>PO<sub>4</sub> powder was consolidated in a LABOX-625 SinterLand Inc. (Japan) system into a graphite mold with an inner diameter of 10 mm. To protect the surface of the mold, graphite paper was placed between the inner walls of the mold and the powder. Sintering was carried out at various pressures (20, 40, and 60 MPa) and a temperature of 970 °C (heating rate from 600 °C was 120 K/min and dwelling time 4 min). The temperature was measured with a pyrometer on the surface of the mold at 360 mm from the die.

Flash sintering was carried out in a modified Linseis L75 dilatometer (Germany) with a constant heating rate of 20 K/min. The powders were pressed using a Carver press (USA) into cylinders with 5 mm diameter and 7 mm height. A 5% solution of polyethylene glycol in water was used as a plasticizer. The uniaxially pressed pellets were placed in the dilatometer between two Pt–Rh disks acting as electrodes. To improve the ceramic/metal electric contact, Ag paste was spread on the parallel, flat faces of the pellets. A DC field was applied using a Glassman EW series 5 kV–120 mA (Singapore) power supply. The electric potential was applied when the sample reached 350 °C and it was maintained until the current limit was reached. The imposed field ranged from 300 to 1000 V/cm until the set current limit value (120 mA, corresponding to 6 mA/mm<sup>2</sup>) was achieved. After reaching the set current, the power source switched to the current control mode and the current was allowed to flow for 2.5 min. The current and voltage were recorded using a KEITHLEY 2100 6½ Digit Multimeter (USA).

The crystalline phase compositions and unit cell parameters were studied via X-ray diffraction (XRD), which was performed using a diffractometer with a rotating anode (D/Max- 2500, Rigaku, Japan). Spectra were acquired in reflection mode (Bragg-Brentano geometry for reflection) using Cu K $\alpha$  radiation (wavelength = 1.54183 Å).

Bulk and apparent densities, as well as the open porosity, were determined by the Archimedes' technique according to ISO 18754:2013:Method B. For the experiment, scales (Sartorius, Germany) with a hydrostatic weighing frame were used. Filling the pores of the samples was carried out under vacuum.

To study the microstructures of the sintered bodies, the samples were polished (DAP-V/Pedemin, Struers, Denmark, and TegraPol-11, Struers, Denmark) with an automatic rotating sample holder (TegraForce-1, Struers, Denmark) according to method F of the user manual (Metalog

Guide, Struers, Denmark). Polished surface was thermally etched at 900 °C for 30 min.

The samples were observed on a LEO SUPRA 50VP scanning electron microscope (SEM) with a field emission gun (Carl Zeiss, Germany), as well as by a NVision 40 SEM (Carl Zeiss, Germany) using a SE2 secondary electron detector. A layer of carbon or chromium was preliminarily deposited on the samples (Quorum Technologies deposition device, QT-150T ES, United Kingdom). X-ray microanalysis with energy dispersion (EDX) was performed on a SUPRA 50VP microscope equipped with the INCA Energy 300 microanalysis system (Oxford Instruments, United Kingdom) at accelerating voltage of 20 kV. Ca K $\alpha$ , P K $\alpha$ , Na K $\alpha$ , and K K $\alpha$  spectral lines were chosen for the analysis. Matrix correction was carried out using  $\phi(\rho z)$  – technique in XPP-modification.

The measurement of grain sizes was carried from SEM images by measuring the area of the grain in ImageJ software and then calculating the radius of the circle of the corresponding area. To construct histograms, at least 100 particles were measured.

### 3. Results and discussion

The microstructures of  $\beta$ -CaK<sub>0.6</sub>Na<sub>0.4</sub>PO<sub>4</sub> ceramic samples after SPS are shown in Fig. 2.

It can be observed that the density of the mixed phosphates obtained by SPS (c.a. 97% of the theoretical one) significantly exceeds that of those obtained by conventional sintering that typically ranges from 85 to 92% (Table 2) [5]. In addition, the microstructure of the SPSed ceramics shows a small number of pores, which are located mainly at the grain boundaries and triple junctions. This situation is undoubtedly favorable for further densification of the ceramics [24].

In agreement with previous research activities it is shown that the grain size increases with pressure especially at 60 MPa. The relative density of all samples is 97 ± 1%. The microstructure (Fig. 1) gives again an evidence of the presence of pores at grain boundaries.

Faster grain growth with increasing pressure and wide grain size distribution at 60 MPa (which is opposite to common experience from hot pressing [38]) is described in several works [39–42]. The origin is not clear but one of possible explanation of this phenomenon could be a plastic deformation of grains as well by their sliding and rotation. Along with atom jumps across the grain boundary this leads to diminishing in misorientation of contiguous grains and, therefore, to faster boundary movement. In fact, coalescence of neighboring grains takes place. In a single-phase material, the existence of different grains is explained by the different orientations of the crystallographic planes. In the process of applying pressure, the grains shift relative to each other with

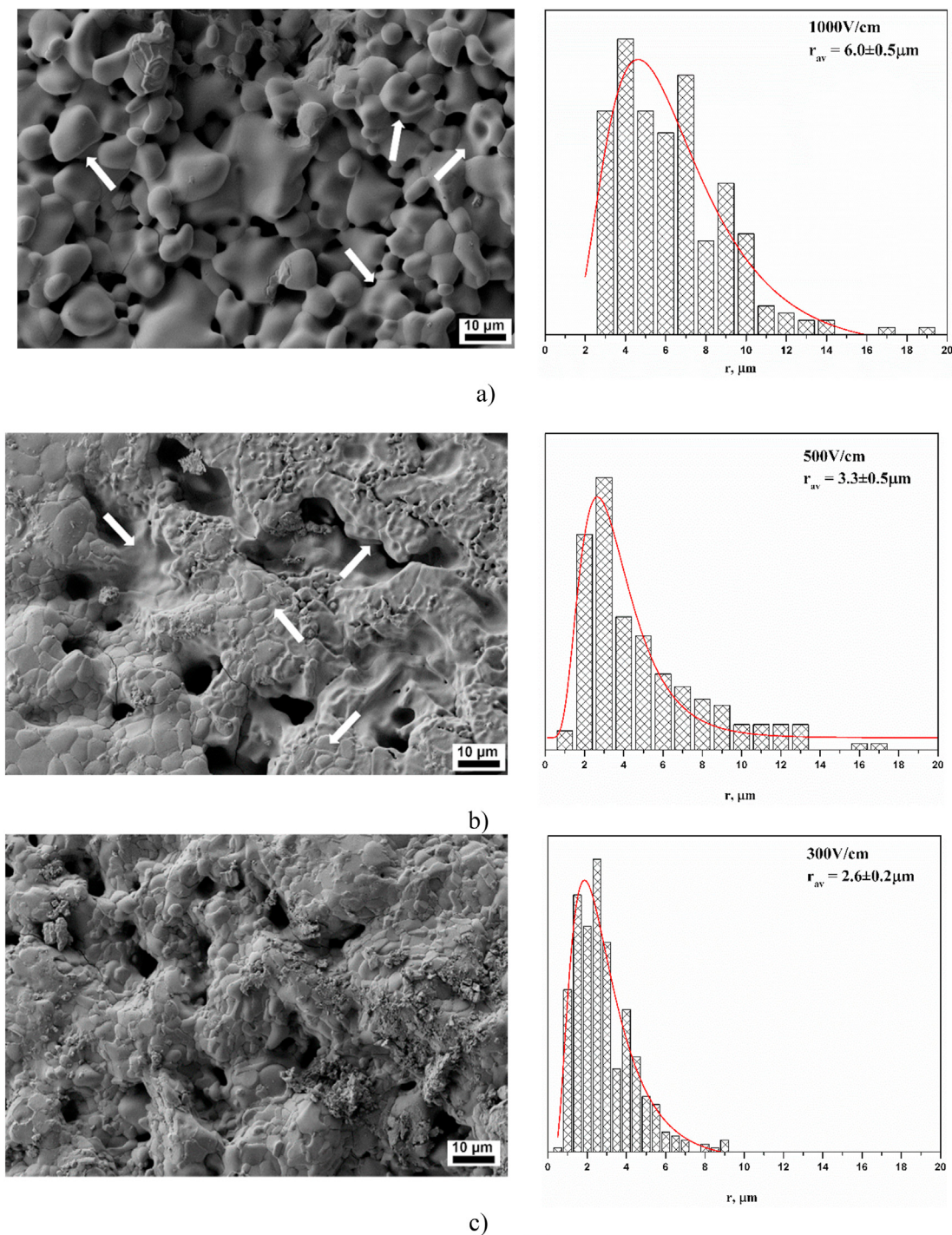


Fig. 4. Microstructure and grain size distribution of  $\beta\text{-CaK}_{0.6}\text{Na}_{0.4}\text{PO}_4$  ceramics after flash-sintering at different field strength a) 1000V/cm, b) 500V/cm, c) 300V/cm. Arrows show a few examples of melted places without sharp edges and with uniform continuous material between grains.

simultaneous plastic deformation. As a result of this movement of grains or the displacement of some of the atoms into the grain boundary region, the planes of two neighboring grains can become oriented in the same way, which, with subsequent small diffusion of atoms, leads to the formation of large grains. With increasing pressure, these grains unification are more intensive, especially in ionic bodies with rather weak energy of crystal lattice where ion diffusion is even more active (this is the case for  $\text{CaK}_{0.6}\text{Na}_{0.4}\text{PO}_4$ , see e.g. Ref. [43]), which is the reason for the results in Fig. 2.

Another explanation of the effect expects that with increasing pressure the onset of sintering is anticipated. Indeed, grain coarsening could

not take place via solid state diffusion until necks are formed (unless other phenomena like evaporation/condensation are activated). Since the sintering cycle was the same for all pressure values, the sample treated at 60 MPa has, in fact, “more time” to coarsen its microstructure. However, in the case of the SPS experiments described above holding at a given temperature (as well as heating time) consists several minutes (4 min for holding and 3 min for heating from 600 to 970 °C). Therefore, the difference in time for grain growth at different pressures occupies also few minutes.

The results indicate that a significant improvement in densification of mixed Ca–K–Na phosphates is achieved by SPS which appears not only



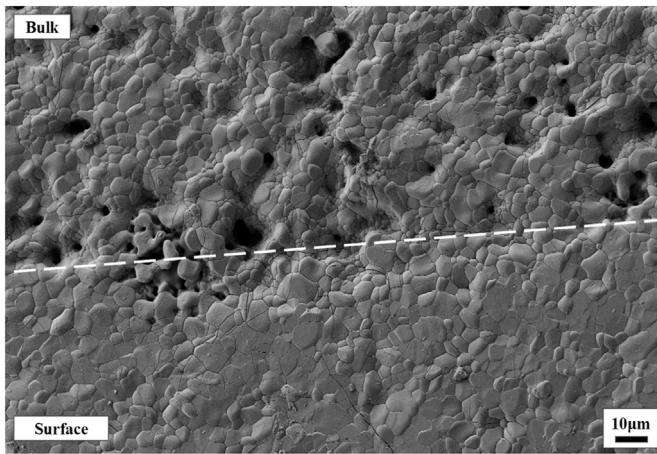


Fig. 5. Microstructure of near-the-surface region of  $\beta$ -CaK<sub>0.6</sub>Na<sub>0.4</sub>PO<sub>4</sub> ceramics after flash-sintering (300V/cm).

related to the external pressure application but could involve additional factors like high heating rate and possible athermal field-activated phenomena. It was mentioned above (Fig. 1a) that the CaK<sub>0.6</sub>Na<sub>0.4</sub>PO<sub>4</sub> demonstrates weak ionic conductivity even after phase transition [5]. As a result, under SPS conditions, very limited current flows through the sample, it passes mainly through graphite mold. In this sense, the reason for better sintering of the mixed phosphates under SPS could be the fast heating caused by the contact with the hot walls of the mold. It is also worth considering the possibility of the effect of electrical field on the diffusion processes during sintering even in the absence of a significant current through the sample.

It should be noted that there is a significant difference in the field strength and applied current in the case of SPS and flash sintering. In the case of SPS, small values of the field are used, but the current can reach a few thousand amperes (in the graphite die). While in flash sintering, at least small currents (hundreds of mA) and hundreds of volts of field

strength are applied directly to the ceramic. The nature of field assistance to sintering is still debatable and several mechanisms have been proposed, including (i) thermal runaway caused by Joule heating [44], (ii) localized grain boundary overheating/melting [45]; (iii) field-assisted Frenkel's pairs nucleation [19,27,44]; (iv) electrochemical phenomena [46,47], and (v) thermodiffusion [48]. In order to study effect of the current flowing through the sample during sintering, the samples were also subjected to flash sintering. The shrinkage curves are shown in Fig. 3a.

Upon heating, the flowing current increases leading to fast heating of the sample and, therefore, to thermal expansion. This is clearly visible on the dilatometric curves as small expansions just at flash event followed by a stage of sharp shrinkage. One can observe that the highest the applied voltage, the lowest the sintering onset temperature, which ultimately leads to the onset temperature below the  $\beta \rightarrow \alpha$  phase transition temperature ( $T_{ph.t.} = 670$  °C). The slope modification of the sintering curve at 1000 V/cm probably corresponds to the moment of the phase transition. The XRD analysis of the samples after sintering show the presence of low-temperature  $\beta$ -CaK<sub>0.6</sub>Na<sub>0.4</sub>PO<sub>4</sub> only (Fig. 3b).

The microstructure the FSed samples is shown in Fig. 4. One can observe that sintering under high fields (1000V/cm and 500V/cm) traces of melt are visible. Thus, grains have no sharp edges, the surface is very smooth and there is uniform continuous phase between grains after 500V/cm (a few examples are represented by arrows in microstructures, Fig. 4 a, b). However, the number of pores is lower compared to the microstructure after conventional sintering. At the same time, the large size of the round particles ( $6.0 \pm 0.5$   $\mu\text{m}$ ) and, at the same time, the small area of interconnections between them at 1000 V/cm correspond to liquid-phase sintering. Observed melting stems between grains could be initiated by intensive thermal runaway during flash event in the field of 1000 V/cm. In a previous work [5], we concluded that in Ca–K–Na phosphate ceramics recrystallization processes prevail over densification. However, the use of fast-firing techniques (i.e., high heating rate) allows enhanced consolidation. During FS, high heating rates are achieved, and this can be considered beneficial for sintering. But, the thermal runaway at 1000 V/cm was probably too intense leading to the formation of a

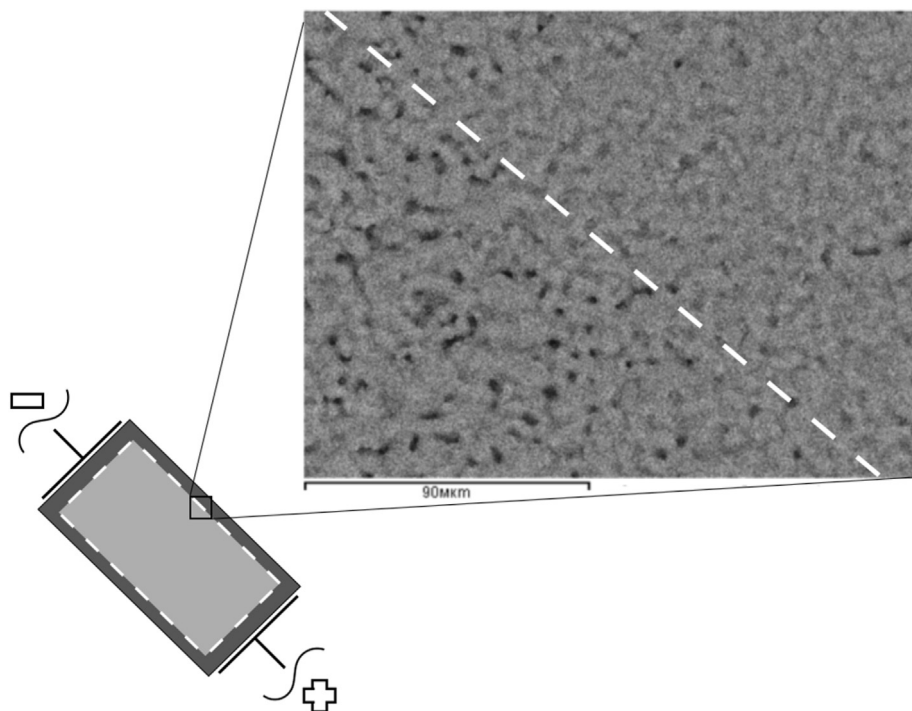
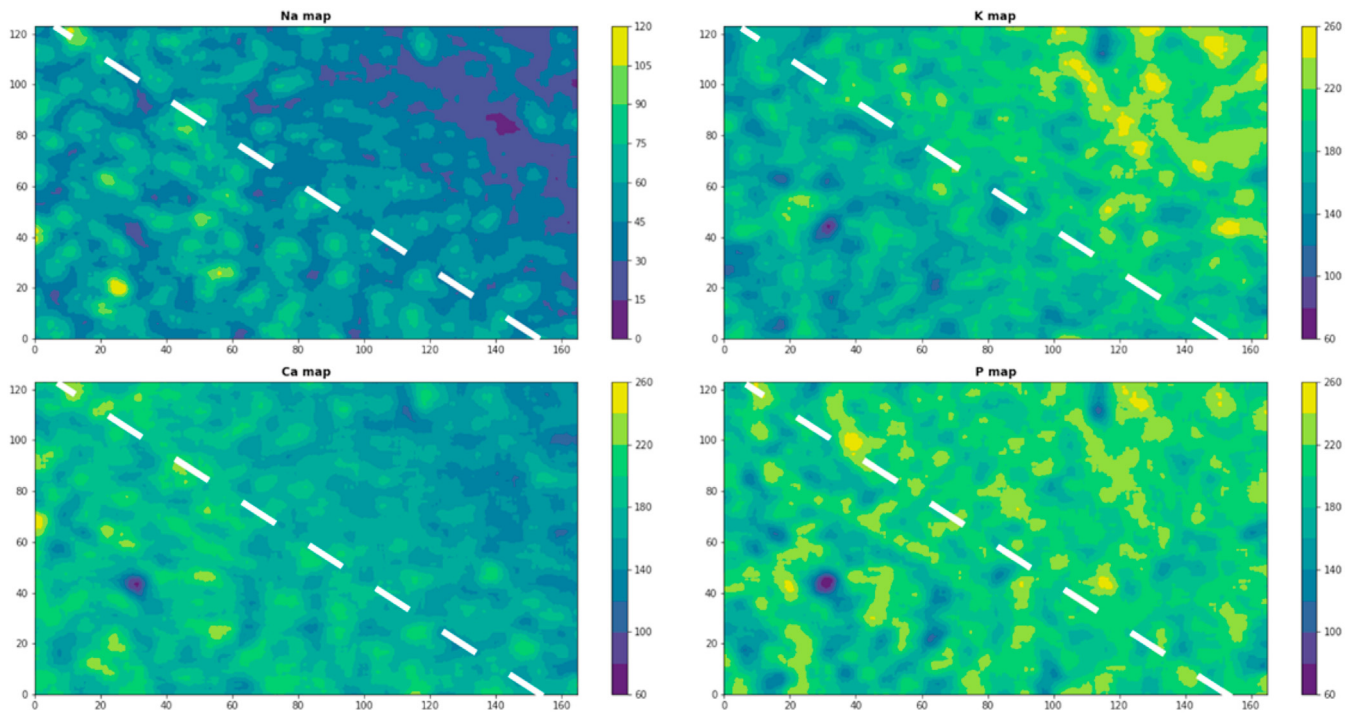
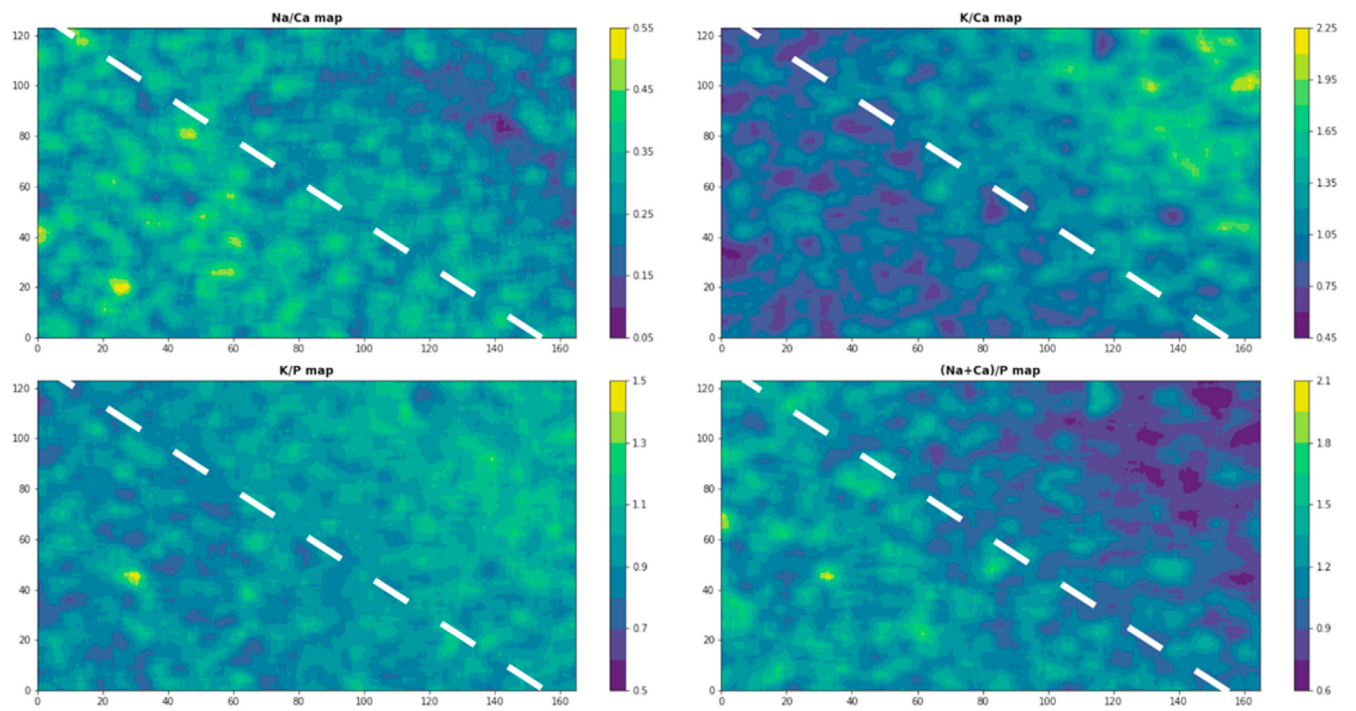


Fig. 6. Non-uniform sintering of the ceramic at 300 V/cm; the rectangular area taken from the border between dense near-the-surface area and less dense core demonstrates different microstructure.



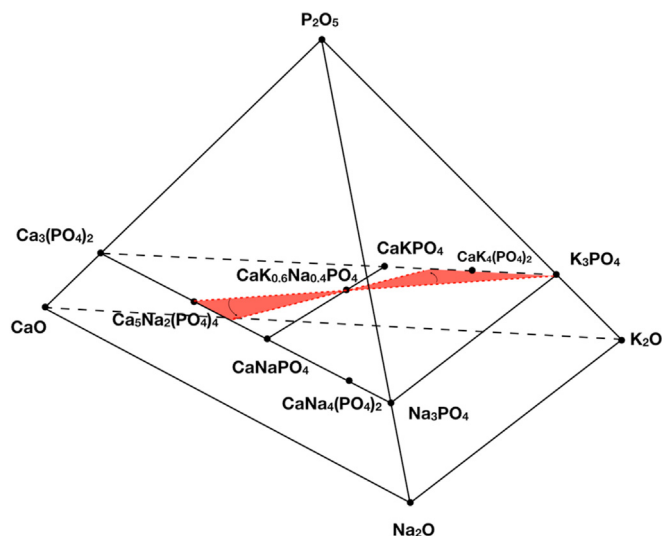
a)



b)

Fig. 7. EDXS elements distribution maps at the border between core and dense regions (from the rectangular area depicted in Fig. 6); the relative amount of elements or their combinations can be recognized using color scale-bars (arbitrary units). (For interpretation of the references to color in this figure legend, the reader is referred to the Web version of this article.)





**Fig. 8.** Phase relationships (schematically) in the system  $P_2O_5$ - $CaO$ - $Na_2O$ - $K_2O$  (the red area includes possible paths of  $CaK_{0.6}Na_{0.4}PO_4$  decomposition during flash-sintering). (For interpretation of the references to color in this figure legend, the reader is referred to the Web version of this article.)

liquid phase. From this viewpoint, moderate fields (300V/cm or even less) better suit for solid-state sintering of  $CaK_{0.6}Na_{0.4}PO_4$  ceramic.

It is also interesting to observe that flash sintering of this particular ceramic proceeds non-uniformly. In the near-the-surface region in curve sample side, the sample is denser than in the remaining volume (Fig. 5), this probably indicating a temperature difference in the specimen. The thickness of such shell is nonuniform through the sample and does not depend on field strength. In average it is in range of 50–150 $\mu$ m. Generally speaking, the microstructure of the core can be attributed to incomplete sintering. It looks like if sintering proceeds from the surface to the core of the sample. Well discernible sintering front sweeps out pores like a grain boundary during boundary control regime of sintering. This is evidenced by the attachment of pores to the interface of sintering front and partial coalescence of pores in the core area (Figs. 5 and 6). Neglecting preferred path of current through the surface region (leading to overheating the surface), one should conclude that due to thermal runaway in the volume and irradiation from the surface, the core of the sample is hot, and the surface is chiller. Thus, our results showing a higher level of densification/coarsening on the surface (Figs. 5 and 6) which are quite surprising and interesting, revealing a behavior never reported in flash sintered specimen.

One can also attempt to compare the occurrence of the surface dense layer with hot spots formed during flash sintering - places where stochastic variations of the electric current result in stable current concentrations in small overheated spots (i.e., the current fluctuation is stabilized thanks to the negative temperature coefficient for electrical resistivity) [18]. However, the presence of a well-distributed dense region all around the specimen does not match the typical morphological features of the hot spots which involve the overheating of small localized regions (usually in the sample center). We can conclude that the formation of the surface/core microstructural gradient reported in Figs. 5 and 6 is not related to hot spots formation.

To unravel the origin of the surface/core microstructural gradients, EDXS analysis of the sample area including the border between dense and less dense inner parts of the sample (Fig. 6) was carried out.

As one can see from the EDXS maps (Fig. 7), there is a migration of potassium towards a denser region, while sodium and calcium were shifted to a more porous part. At the same time, the intensity of phosphorus signal remained approximately at the same level over the entire area of the analyzed area.

From the point analysis it is possible to estimate roughly the

composition variation in the vicinity of the border after flash sintering. In the lower left part of the map, corresponding to a less dense area (the core), the ratio of sodium to calcium is of about 0.4–0.45; the ratio between cations and phosphorus in this region is slightly higher than 1.5. This suggests that the composition is shifted toward the compound  $Ca_5Na_2(PO_4)_4$ . At the same time, in the upper right part (surface), as already mentioned, there is a larger content of potassium. The ratio of potassium to phosphorus in this area also increases up to 1.3–1.4; the ratio of potassium to calcium is close to 2. According to these ratios, the resulting compositions of these regions lie on the  $Ca_5Na_2(PO_4)_4$ - $K_3PO_4$  line, or bearing in mind different diffusivity of Ca, Na, K cations on the curve situated in the vicinity of this line, as it is shown in Fig. 8.

At the sintering temperature (which is higher than the observed flash onset temperature, 754 °C at 300 V/cm, Fig. 3a)  $CaK_{0.6}Na_{0.4}PO_4$  composition belongs to extended area of a solid solution of  $\alpha$ - $Ca(K,Na)PO_4$  with glaserite structure (Fig. 1c); the solid solution of this type shows cationic conductivity [5]. If a surface/core thermal gradient is established at the flash transition (this is likely because the surface radiate heat toward the environment), there is a possibility of changing the initial uniform composition of the solid solution (demixing) due to thermomigration of mobile cationic species (Ludwig-Soret effect). It is known from the theory of thermal diffusion that concentration gradient of each mobile specie caused by temperature gradient can be expressed as (stationary conditions, diluted solution) [49,50]:

$$\frac{d \log C}{dT} = \frac{-Q}{RT^2} \quad (1)$$

where  $C$  – local concentration of the diffusant,  $T$  – local temperature,  $R$  (=8.31 J mol<sup>-1</sup> K<sup>-1</sup>) – gas constant,  $Q$  – heat of transfer of the specie along gradient. It is accepted that  $Q = H_1 - H_2$ , where  $H_1$  – enthalpy related to leaving by atom (ion) its regular position, while  $H_2$  – enthalpy related to landing by atom (ion) to a new position along gradient. For light, highly mobile species, usually  $H_1 < H_2$ , so according to (1) highly diffusive atoms are concentrated in a hot zone (abnormal Ludwig-Soret effect). In the case of  $CaK_{0.6}Na_{0.4}PO_4$ , in accordance with charge and radius, the ions can be ordered in the following row of decreasing their diffusivity:  $Na^+ > Ca^{2+} > K^+$ . Taking the above assumptions into account, it is possible to conclude that Na and Ca can concentrate in a hot core, while K goes to chiller surface layer. Better sintering ability of K-rich layer does not contradict our data on sintering of different compositions in  $CaNaPO_4$  –  $CaKPO_4$  system where K-rich composition demonstrated better densification [5]. Clearly, it is necessary to measure temperature gradient as well as  $Q$  values for the diffusants to confirm unambiguously such a conclusion. It is also of interest whether the described demixing of the solid solution in temperature gradient can proceed further leading to a phase separation, i.e. formation of multi-phase mixtures (depicted in Fig. 1c) as it was observed for other materials in gradient of chemical potentials [49,51]. These issues are addressed to a forthcoming paper.

#### 4. Conclusions

The possibility to sinter ceramics based on substituted calcium phosphates  $CaK_{0.6}Na_{0.4}PO_4$  to a 96% of relative density and grain size is about 4.5  $\mu$ m by SPS technique was shown. Grain size of ceramic increases with applied pressure. This phenomenon was explained by plastic deformation of grains as well by their sliding and rotation during sintering under pressure. Materials with an average grain size of about 2.6  $\mu$ m were obtained by Flash sintering. It was shown higher field strength correspond to lower average grain size. Density difference between the surface of the sample and its core was observed and this was accounted for by radial temperature gradient.

The migration of potassium towards denser region, and sodium/calcium to more porous parts during flash-sintering was revealed. According to observed elemental ratios in the near-the-surface region, the resulting



compositions of these regions lie in the vicinity of  $\text{Ca}_5\text{Na}_2(\text{PO}_4)_4\text{-K}_3\text{PO}_4$  line. The possible explanation can include a thermal diffusion phenomenon (Ludwig-Soret effect).

## Acknowledgments

The reported study was funded by RFBR, projects numbers 19-38-90199 and 19-03-00940 and in part by the Lomonosov Moscow State University program of development.

V.M. Sglavo and M. Biesuz kindly acknowledge the support from the Italian Ministry of University and Research (MIUR) within the programs PRIN2017 - 2017FCFYHK "DIRECTBIOPOWER", PRIN2017 - 2017PMR932 "Nanostructured Porous Ceramics for Environmental and Energy Applications" and Departments of Excellence 2018–2022 (DII-UNITN).

Prof. J. Günster and N. Orlov acknowledge State of Lower Saxony, Germany within the PhD Program "Self-organizing multifunctional structures for adaptive lightweight constructions".

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