

# LOOKING FOR STOKES THEOREM IN AN ELEMENTARY TRAPEZOID.

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ABSTRACT. The aim of this very short note it to show that even in a totally elementary framework, it is possible to glimpse the Stokes theorem.

## THE NOTE

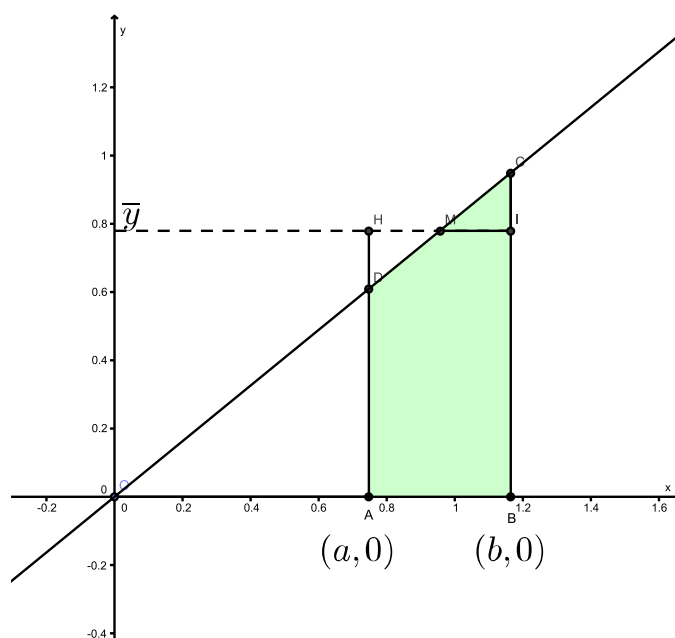


FIGURE 1

The Stokes theorem tell us that

$$(1) \quad \int_{\Omega} d\omega = \int_{\partial\Omega} \omega.$$

where  $\Omega$  is a suitable domain and  $\partial\Omega$  its boundary. Even in the calculation of the area of an elementary trapezoid, we use, almost certainly in a non-conscious way, either the LHS or the RHS of equation (1). Let

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us consider a rectangular trapezoid  $ABCD$  as shown in Figure 1 and let be  $y = mx$  the straight line through  $O$  and  $C$ . Of course we can calculate the area of the trapezoid in two different ways:

- (1) We can think to the trapezoid as equivalent to the rectangle  $ABIH$ .
- (2) We can think to the trapezoid as the difference between the triangles  $COB$  and  $DOA$ .

If we think to the trapezoid as equivalent to the rectangle  $ABIH$  then, since its area is  $\mathcal{A} = \bar{y}(b - a)$ , we can imagine this as theas the LHS of (1) where  $\Omega$  is the interval  $[a, b]$  and  $d\omega = (mx)dx$ . If we calculate the area as difference between the area of the triangle  $OCB$  and the area of the triangle  $DOA$  then we have

$$A = \frac{b(mb)}{2} - \frac{a(ma)}{2} = \frac{1}{2}mb^2 - \frac{1}{2}ma^2 = \omega(b) - \omega(a) = \int_{\partial\Omega} \omega$$

namely, the RHS of (1) because the boundary of  $\Omega$ , trivially is given by  $\{b, a\}$ .

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