Scale up to infinity: the UWB Indoor Global Positioning System

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Abstract—Determining assets position with high accuracy and scalability is one of the most investigated technology on the market. The accuracy provided by satellites-based positioning systems (i.e., GLONASS or Galileo) is not always sufficient when a decimetre-level accuracy is required or when there is the need of localising entities that operate inside indoor environments. Scalability is also a recurrent problem when dealing with indoor positioning systems. This paper presents an innovative UWB Indoor GPS-Like local positioning system able to tracks any number of assets without decreasing measurements update rate. To increase the system’s accuracy the mathematical model and the sources of uncertainties are investigated. Results highlight how the proposed implementation provides positioning information with an absolute maximum error below 20 cm. Scalability is also resolved thanks to DTDoA transmission mechanisms not requiring an active role from the asset to be tracked.

Keywords—Ranging-based positioning, Ultra-Wide Band, Global Positioning System, Indoor positioning

I. INTRODUCTION

As an accurate positioning system is the mainstay of most mobile robot applications [1], researchers have proposed to implement different LPS to provide an indoor localisation infrastructure. As described in [2] positioning systems can be classified into two macro classes: 1) Global Position Systems (GPS) and 2) Local Positioning Systems (LPS). In the last decades, significant progress was registered in the development of positioning systems [3], especially to find a low-cost, accurate and local alternative to GPS for the indoor environment [4]–[7]. This also thanks to the ground-breaking improvements made to industries such as healthcare [8], [9], livestock farming [10], [11], warehousing [12], [13] and, more recently, in the robotic field [14], [15].

LPSs can be categorised [2] by: 1) Computation approach: centralised, decentralised; 2) Environment type: underwater, outdoor, and indoor; 3) Communication Technology: optical, acoustic and radio frequency. For example, in [16] authors localise the position of an acoustic source in underwater environments. In [17] authors improve the navigation system providing more accurate pose information to aid the odometry using infrared sensors. Based on optical waves as transmission medium, in [18] conventional lights are used to enable the localisation.

A promising approach to localise a moving entity – with decimetre accuracy level – is assessing Radio Frequency (RF) signal propagation. Different RF positioning solutions have been tested: like RFID [19], WLAN [20] and cellular network [21]. In the class of RF technology, ultrawide-band (UWB) has attracted increasing interest due to its excellent characteristics, like robustness to multipath error, obstacle penetration, high accuracy and low cost [22]. In the case of RF-based localisation systems the fundamentals ranging techniques to estimate the distance from two nodes are: Received Signal Strength (RSS); Time of Arrival (ToA); Time Difference of Arrival (TDoA) and Angle of Arrival (AoA). RSS is the simplest approach to estimate the distance between two nodes [23], [24]. In this case, the path loss model is exploited to estimate the distance by measuring the signal’s received power. ToA implementations are based on the time of arrival of a signal, which allows to determine the distance from the RF wave propagation speed. The location information can be determined using algorithms like trilateration or multilateration solving the associated geometrical problem (i.e., circle or sphere intersections) [25]. In TDoA, as for the ToA case, the distance estimation is based on the propagation speed. However, in this case, the difference in receiving times of a signal is considered, leading to a geometrical problem based on hyperbolas [26]. AoA implementation exploits the capabilities of unknown nodes of detecting the angles of incoming signals. One common approach to obtain AoA measurements is to use an antenna array on each sensor node. It is then possible to discover both the position and the orientation by exploiting the angle measurements [27].

In the UWB localisation systems, ToA and TDoA ranging techniques are commonly adopted. In the case of the ToA approach, two different communication schemes can be implemented: Single-side (SS) or double-side (DS) two way ranging (TWR) [28]. With TWR, a synchronisation mechanism between nodes is not required. In this case, an accurate calibration of the crystal oscillators is sufficient to increase the measurement accuracy, especially in SS-TWR. The drawback
The main contributions of this paper are:

- The main idea underlying this approach is that no message exchange should be carried out from the tag to the anchors, but only from the anchors to the tag. This to ensure infinite scalability in terms of trackable number of tags. In the ideal case, the quantities \( o_i \), \( \nu_i \) (with \( i = 1, \ldots, n \)) in (2) with respect
to the master reference time are retrieved through the following
synchronisation algorithm: starting at a generic time $t$, the
master anchor sends two messages $\tau^m(t)$ and $\tau^m(t + \Delta_i,m)$ to
$a_i$, whose timestamps at the receiving side are $\tau^i(t + \delta_i,m)$ and
$\tau^i(t + \Delta_i,m + \delta_i,m)$, where $\delta_i,m$ is the Time of Flight (ToF)
from the master to the anchor. By denoting with $[x_m,y_m]^T$ and
$a_i = [x_i,y_i]^T$ respectively the master and the anchor known
Cartesian coordinates in the $X_w \times Y_w$ plane with respect to a
fixed reference frame $\langle W \rangle = \{X_w,Y_w,Z_w\}$, it turns out that
\[
\rho_{i,m} = \| [x_m,y_m]^T - a_i \| = \sqrt{(x_m-x_i)^2 + (y_m-y_i)^2},
\]
is the distance among the two anchors (where $\| \cdot \|$ is the usual Euclidean norm). Therefore, assuming that $c$ is the known propagation speed of the radio frequency signal in LOS
conditions, we have that $\delta_{i,m}$ can be obtained as
\[
\delta_{i,m} = \frac{\rho_{i,m}}{c}. \tag{4}
\]
As a consequence, using (1) and (2) we can derive the relative
clock rate
\[
\nu_i = \frac{\nu_m}{\nu_m} = \frac{\tau^i(t + \Delta_{i,m} + \delta_{i,m}) - \tau^i(t + \delta_{i,m})}{\tau^m(t + \Delta_{i,m}) - \tau^m(t)}, \tag{5}
\]
and the relative offset
\[
\begin{align*}
\tau^i(t + \delta_{i,m}) - \tau_{i,m} \tau^m(t) - \delta_{i,m} = \\
\delta_{i,m} &= \nu_{i,m} o_m - (1 - \nu_i) \delta_{i,m} = \bar{\nu}_{i,m} = \\
\tau^i(t + \Delta_{i,m} + \delta_{i,m}) - \tau_{i,m} \tau^m(t + \Delta_{i,m}) - \delta_{i,m}.
\end{align*} \tag{6}
\]
By assuming that the clock rates $\nu_m$ and $\nu_i$ are approximately constant among two synchronisation periods (usually executed every tens of seconds), and that the master and the anchors do not change their relative positions (i.e., the ToF $\delta_{i,m}$ is constant), we can derive that the relative offset $\bar{\nu}_{i,m}$ is constant as well. Furthermore, the term $(1-\nu_i)\delta_{i,m}$ is usually negligible with respect to the relative offset between the master and the anchor. In turns, by using $\nu_{i,m}$ representing the correction factor that transforms the timestamped measured quantities in master time-scale into the $i$-th anchor time-scale – a generic timestamp $\tau^i(t)$ of an anchor can be translated to the master
time-scale using (1) and
\[
\frac{\tau^i(t) - \delta_{i,m}}{\bar{\nu}_{i,m}} = o_m + \nu_{i,m} t + \frac{1 - \nu_i}{\bar{\nu}_{i,m}} \delta_{i,m} = \tau^m(t) + \epsilon_{i,m}. \tag{7}
\]

### B. Tags clock analysis

Due to the DTDooA approach used, also tag’s clock have to be corrected. Let’s consider the tag at time $t$ be in position $p(t) = [x(t), y(t)]^T$ in $\langle W \rangle$. By denoting with
\[
\rho_i(t) = \| p(t) - a_i \| = \sqrt{(x(t) - x_i)^2 + (y(t) - y_i)^2},
\]
the actual distance between the tag and the $i$-th anchor, we have that the ToF $\delta_i(t)$ is given by (4) when $\rho_{i,m}$ is substituted with $\rho_i(t)$. Therefore, considering that the $i$-th anchor sends two timestamped messages to the tag at time $t_i$ and $t_i + \Delta_i$, respectively, by using (7) we get that $\tau^i(t_i) = \tau^m(t_i) + \epsilon_{i,m}$ and $\tau^i(t_i + \Delta_i) = \tau^m(t_i + \Delta_i) + \epsilon_{i,m}$. These two messages
will be received by tag time-scale at $\tau(t_i + \delta_i(t_i))$ and $\tau(t_i + \Delta_i + \delta_i(t_i))$.

Considering the motion of the tag, that can be expressed as
\[
p(t + \Delta_i) = p(t) + \Delta_i \begin{bmatrix} v_x(t) \\ v_y(t) \end{bmatrix} = p(t) + \Delta_i v(t),
\]
a first-order discrete time kinematics with a velocity $v(t)$, we have
\[
\rho_i(t_i + \Delta_i) = \| p(t_i) + \Delta_i v(t_i) - a_i \|,
\]
which of course depends on the velocity vector $v(t_i)$. However, an upper bound can be found noticing that the maximum increase (or decrease) of the distance takes place when $v(t_i)$ is directed towards the anchor $a_i$, i.e., along the direction $u_i(t) = [x(t) - x_i, y(t) - y_i]^T$. In such a case, denoting with $d_i(\Delta_i) = \| \Delta_i v(t_i) \|$ the tag displacement taking place at time $t_i$ in the period $\Delta_i$, we have that
\[
\rho_i(t_i) - d_i(\Delta_i) u_i(t_i) \leq \rho_i(t_i + \Delta_i) \leq \rho_i(t_i) + d_i(\Delta_i) u_i(t_i),
\]
which yields for the ToF in (4) to
\[
\delta_i(t_i) - \frac{d_i(\Delta_i)}{c} u_i(t_i) \leq \delta_i(t_i + \Delta_i) \leq \delta_i(t_i) + \frac{d_i(\Delta_i)}{c} u_i(t_i). \tag{8}
\]

For what concerns the TDoA, the last missed ingredients is the synchronisation algorithm between the tag and the anchor $a_i$. To this end, we used an algorithm that is the same of (5), i.e.,
\[
\begin{align*}
\frac{\tau(t_i + \Delta_i + \delta_i(t_i + \Delta_i)) - \tau(t_i + \delta_i(t_i))}{\bar{\nu}_{i,m} - \tau^m(t_i) - \tau^m(t_i + \Delta_i)} &= \\
\frac{\tau(t_i + \Delta_i + \delta_i(t_i + \Delta_i)) - \tau(t_i + \delta_i(t_i))}{\bar{\nu}_{i,m}} &= \\
\frac{\tau(t_i + \Delta_i) - \tau^m(t_i)}{\bar{\nu}_{i,m}} &= \\
\frac{\nu_i \Delta_i}{\bar{\nu}_{i,m}} &= \tau^m(t_i) = \tau^i(t_i + \Delta_i).
\end{align*}
\tag{9}
\]
where
\[
\bar{\nu}_{i,m} = \frac{\nu_{i,m}}{\nu_m} \left( 1 + \alpha \frac{d_i(\Delta_i) u_i(t_i)}{c \Delta_i} \right),
\]
and $\alpha \in [-1,1]$.

### C. Indoor GPS TDoA

The UTDooA relies on an implicit event: all the anchors receive a tag’s generated broadcast message that acts as an implicit synchronisation event. In the case of an indoor GPS-like system with unbounded scalability – like the proposed DTDooA – the messages are transmitted from anchors side to the tags side; meaning that a synchronisation event cannot be defined. Strictly speaking, if such a possibility would exist, the master and anchors would send their packets simultaneously at time $t_m$. The tag would then measure the difference in reception times as $\tau(t_m + \delta_m(t_m))$ and $\tau(t_m + \delta_i(t_m))$ and, hence be able to compute the TDoA as
\[
c [\tau(t_m + \delta_i(t_m)) - \tau(t_m + \delta_m(t_m))] = \\
c \nu_i \delta_i(t_m) - \delta_m(t_m) \nu_m = \nu_i (\rho_i - \rho_m), \tag{10}
\]


∀i = 1, ..., n. Notice that such a measure is only affected by the relative clock rate ν, which is of course negligible since it generates an error in the order of some micrometers.

Since such a synchronised event cannot be generated (the anchor will transmit at slightly different time instants and the tag cannot receive all the messages at once), the synchronisation between tags and anchors (i.e., estimation of the relative clock rates) cannot be neglected. Let’s considering a system composed by a master, a number of anchors i and a tag. At time $t_m$ a broadcast message is transmitted from the master, followed by a second message at time $t_m + \Delta_m$. The tag timestamps the messages at reception times, denoted as $\tau(t_m + \delta_m(t_m))$ and $\tau(t_m + \Delta_m + \delta_m(t_m + \Delta_m))$. Finally the tag stores the two transmission timestamp encapsulated inside the broadcast message, defined as $\tau^m(t_m)$ and $\tau^m(t_m + \Delta_m)$. The same happens with the anchor i transmitting at time $t_i$ and $t_i + \Delta_i$, with tag’s timestamped reception times $\tau(t_i + \delta_i(t_i))$ and $\tau(t_i + \Delta_i + \delta_i(t_i + \Delta_i))$, and the two transmitted timestamps $\tau^m(t_i) - \tau^m(t_m)$ and $\tau^m(t_i + \Delta_i) - \tau^m(t_m)$, as corrected anchor clock in master time scale using (7). It is then possible to compute at the tag side the relative clock rates $\nu_i$ using (9) (that explaining the necessity to send/receive two messages) and a function $g(\Delta_i)$ of the protocol time interval $\Delta_i = t_i - t_m$ by means of the clock model (1)

$$g(\Delta_i) = \nu_i \left( \frac{\tau^m(t_i) - \nu_i \tau^m(t_m)}{\nu_i \tau^m(t_m)} - \frac{\tau_i}{\tau^m(t_m)} \right) = \nu_i \left( \tau^m(t_i) - \tau^m(t_m) + \epsilon_i \right) = \nu_i \nu_m (t_i - t_m) + \nu_i \epsilon_i = \nu \Delta_i + \nu \Delta_i.$$

By defining the corresponding tag timestamps and the clock model (3) as

$$\tau(t_i + \delta_i(t_i)) - \tau(t_m + \delta_m(t_m)) = \nu \delta_i(t_i) - \delta_m(t_m) + \nu t_i - t_m = \nu (\nu_i(t_i + \Delta_i) - \nu_i(t_m + \Delta_i)).$$

and considering (8) as

$$\nu_i(t_i + \Delta_i) = \nu_i(t_m + \Delta_i) + \alpha \frac{d_i(\Delta_i)}{c} u_i(t_m),$$

we can finally have the DTDoA equation:

$$\nu \left( \tau^m(t_i + \Delta_i) - \tau^m(t_m + \Delta_m) \right) = \nu \left( \nu_i(t_i + \Delta_i) - \nu_i(t_m + \Delta_m) \right).$$

computed using (4) and (11).

Those quantities can be equivalently computed for the delayed messages, by considering $\tau^m(t_i + \Delta_i) + \delta_i(t_i + \Delta_i)$ in (11) and $\tau(t_i + \Delta_i + \delta_i(t_i + \Delta_i))$ in (12). Of course, comparing (13) and (10), we can notice that in the presence of multiple time sources (i.e., having i anchors) induces potential errors stemming from the imperfect synchronisation with the master, highlighted in (7), which is, unfortunately unavoidable.

### III. Uncertainties

The main source of uncertainties – neglecting the effects of ageing or the drift changes induced by harsh environmental conditions (e.g., mechanical vibrations or temperature effects [34]) – is related to timestamping accuracy operation. Albeit those effects can be dramatically reduced by implementing double consecutive message transmissions (i.e., the timestamp is acquired when the message is sent, and then transmitted in a second message, as in [34]), the effect cannot be entirely removed. As a consequence, by denoting with $\eta$ the generic timestamping uncertainty affecting each clock in the network, we can rewrite the clock models as

$$\tau^m(t_i + \Delta_i) + \eta(t_i + \Delta_i) = \tau_i + \eta_i + \tau^m(t_i + \Delta_i),$$

by assuming a first-order Taylor approximation for the uncertainty, the relative clock rates $\nu_i$ in (5), when computed with (14) becomes

$$\nu_i(t_i + \Delta_i) + \frac{\tau_i + \Delta_i}{\tau^m(t_i + \Delta_i)} \approx \nu_{i,m} + \beta = \nu_{i,m},$$

having the uncertainty mean $\mu_\beta = E \{ \beta \} = 0$ (the E \{ \} is the usual expected operator) and its variance

$$E \{ \beta^2 \} = \sigma^2_\beta = \frac{2}{\nu_{i,m}^2} \sigma^2_{\eta_i} + \sigma^2_{\eta_{i,m}}.$$
which may or may not be more useful than (15) depending on the value of $\Delta t_i$. This is a direct consequence of the fact that $\delta t_i(t \pm \Delta t)$ and $\delta t_i(t \pm \Delta t_i)$ are correlated by $\sigma_{\hat{t},i,m}$.

For what concerns equation (7), if the time $t$ in which the anchor time scale is converted into the master time scale is different from $\tilde{t}$, $\tilde{t} + \Delta t_i$, $\tilde{t} + \delta t_i$ and $\tilde{t} + \Delta t_i + \delta t_i$ (i.e., the times in which (5) and (6) are used), we can again use a first-order Taylor approximation to re-write (7) as

$$\tau^{\ast}(t) - \tilde{\delta}_{i,m} \approx \tau_{m}(t) + e_{i,m} + \varepsilon(t).$$

Having $E \{ \varepsilon(t) \} = 0$ and

$$\sigma^2_{\varepsilon}(t) = \frac{\sigma^2_{\varepsilon,m}}{\tau_{m}^{\ast}} + \frac{\sigma^2_{\varepsilon,\tilde{t}}}{\tau_{m}^{\ast}} + \left[ \frac{(\tau_{m}(t) + e_{i,m})^2}{\tau_{m}^{\ast}} - 2 \frac{\tau_{m}(t) + e_{i,m}}{\tau_{m}^{\ast}} \tau^{\ast}(t) \right] \sigma^2_{\beta},$$

allow us to compute the uncertain version of (9) as

$$\tau^{\ast}(t_i + \Delta t_i + \delta t_i(t_i)) - \tau^{\ast}(t_i + \delta t_i(t_i)) \approx \frac{\tau^{\ast}(t_i + \Delta t_i) - \tilde{\delta}_{i,m}}{\tau_{m}^{\ast}} - \frac{\tau^{\ast}(t_i) - \tilde{\delta}_{i,m}}{\tau_{m}^{\ast}} + \varepsilon(t_i) \approx \varepsilon(t_i) + \xi(t_i) = \varepsilon(t_i),$$

with $E \{ \xi(t_i) \} = 0$ and

$$\sigma^2_{\xi}(\Delta t_i) = \frac{2\tau_{m}^2}{\tau_{m}^{\ast}} \sigma^2_{\varepsilon,m} + \frac{2}{\nu^2} \Delta^2 \sigma^2_{\delta} + \frac{\nu^2}{\nu^*_{i,m}} \sigma^2_{\beta}.$$

Similarly, to compute the noisy protocol interval in (11), we have

$$g^{\ast}(\Delta t_i) = \varepsilon(t_i) + \varepsilon(t_m) \approx \xi(t_i) + \xi(t_m).$$

In this case $E \{ \varphi(t_i, t_m) \} = 0$ and

$$\sigma^2_{\varphi}(t_i, t_m) = \sigma^2_{\varepsilon,m} + \sigma^2_{\nu^*_{i,m}} + \nu_{i,m}^2 (\Delta t_i + \delta t_i) \sigma^2_{\varepsilon} + \nu_{i,m}^2 \sigma^2_{\xi},$$

where $\sigma_{\varepsilon}(t_i, t_i + \Delta t)$ is the correlation between the uncertainties $\varepsilon(t_i)$ and $\varepsilon(t_i + \Delta t)$ leading to

$$E \{ \varepsilon(t_i) \varepsilon(t_i + \Delta t) \} = \frac{\tau_{m}(t_i) + e_{i,m} \tau_{m}(t_i + \Delta t)}{\tau_{m}^{\ast}} \sigma^2_{\beta} + \frac{2\tau_{m}^2}{\tau_{m}^{\ast}} \tau_{m}(t_i + \Delta t) + \frac{\nu^2}{\nu^*_{i,m}} \tau_{m} \left( \tilde{t} + \frac{\Delta t_i}{2} \right) \sigma^2_{\beta}.$$

We are now ready to conclude the uncertainty analysis by computing the final DTDOA relation (13) once the measured quantities in (14) are used:

$$c \left[ \tau^{\ast}(t_i + \delta t_i(t_i)) - \tau^{\ast}(t_m + \delta t_m(t_m)) - g^{\ast}(\Delta t_i, m) \right] =$$

$$= \nu(\rho_i - \rho_m) - \sigma_{\tilde{t},i,m} e_{i,m} + \lambda(t_i, t_m),$$

resulting in an overall uncertainty with mean $E \{ \lambda(t_i, t_m) \} = 0$ and variance

$$\sigma^2_{\lambda}(t_i, t_m) = c^2 \left[ 2 \left( \nu_{i,m} \Delta t_i + e_{i,m} \right) \sigma^2_{\eta} + \sigma^2_{\lambda}(t_i, t_m) \right].$$

A. Numerical analysis

In this section we present the simulation results about the validity of the uncertainty analysis presented in the previous subsection. The first simulation analyse the tightness of the approximations of the uncertainties introduced by the first-order Taylor linearisation. Figure 2 presents the absolute relative error, expressed in percentage, between the theoretical values of the mean $\mu_{\gamma}(\tilde{t})$ and the standard deviation $\sigma_{\gamma}(\tilde{t})$ in (15) for the uncertainty $\gamma(\tilde{t})$, with respect to the values obtained through 10000 Monte Carlo Simulations, here denoted with $\mu_{\gamma}^{MC}(\tilde{t})$ and $\sigma_{\gamma}^{MC}(\tilde{t})$:

$$\mu_{\gamma}^{MC}(\tilde{t}) = 100 \left| \frac{\mu_{\gamma}(\tilde{t}) - \mu_{\gamma}^{MC}(\tilde{t})}{\mu_{\gamma}^{MC}(\tilde{t})} \right|,$$

and

$$\sigma_{\gamma}^{MC}(\tilde{t}) = 100 \left| \frac{\sigma_{\gamma}(\tilde{t}) - \sigma_{\gamma}^{MC}(\tilde{t})}{\sigma_{\gamma}^{MC}(\tilde{t})} \right|,$$

respectively. The Monte Carlo simulations assume 10 anchors (on the abscissa of Figure 2) with randomly generated clock time offsets, clock rates, positions, delays $\Delta t_i$ and $\Delta t_i, m$, having zero-mean, Gaussian time stamping uncertainties $\eta_{\gamma}(t)$, $\eta_{\delta}(t)$, and $\eta_{\tau}(t)$, with a maximum value of plus/minus 15.65 ps (i.e., one clock tick, as per the available hardware, see Section IV). As can be seen from Figure 2, whatever uncertainty is considered, i.e. $\gamma(\tilde{t})$, $\gamma(\tilde{t} + \Delta t_i, m)$ or the average of the two $\overline{\gamma}(\tilde{t})$ reported in (16), the theoretical analysis matches remarkably well with the simulations (the mean, for example, are all overlapped with negligible errors in Figure 2). Similar results are obtained for all the other quantities, here not reported for space limits.
Fig. 3. Distribution of the DTDoA uncertainties $\sigma^2(t_i, t_m)$ in (17) in the case of (a) Gaussian and (b) Uniform timestamping uncertainties.

Of course, the approximation becomes less accurate when the timestamping uncertainties are uniformly distributed between plus/minus 15.65 ps, as reported in Figure 3 that presents the DTDoA uncertainties in (17) for the anchor $a_1$.

IV. EXPERIMENTAL RESULTS

To evaluate and validate the statistical model discussed in the previous section, we have implemented the proposed DTDoA algorithm using UWB radios. UWB radio transmission is based upon impulse radio (IR) schemes. The pulses being applied in IR have a very short temporal duration (typically in order of nanoseconds), which results in an ultra-wide band spectrum [35]. This very large spectrum allows to achieve excellent time and spatial resolution by evaluating the Channel Impulse Response (CIR) of the signal.

A. Hardware Implementation

To implement our LPS, we decided to use the commercial-off-the-shelf (COTS) Decawave DWM1001\(^1\) SoM, which attracted many interests for implementing indoor positioning systems [36]. The DWM1001 is a compact module that integrates both a low power nRF52832 MCU and the Decawave DW1000\(^2\) UWB transceiver. It also integrates RF circuitry, an UWB antenna and a motion sensor for sensor fusion applications [37].

The DW1000 chip is an IEEE 802.15.4-2011 [38] compliant UWB transceiver which can operate on 6 different frequency bands with centre frequencies between 3.5 to 6.5 GHz and a bandwidth of 500 or 900 MHz. It provides the possibility of ranging measurements and retrieving the measured CIR. The chip also offers three different data rates: 110 kbps, 850 kbps and 6.8 Mbps.

The DW1000 clocking scheme is based on 3 main circuits; crystal oscillator (trimmed in production to reduce the initial frequency error to approximately 3 ppm), Clock Phase-Locked Loop (PLL) and RF PLL. The on-chip oscillator is designed to operate at a frequency of 38.4 MHz. This clock is then used as the reference input to the two on-chip PLLs. The clock PLL generates a 63.8976 GHz reference clock required by the digital backend for signal processing. The RF PLL generates the clock for the receive and transmit chain. The DW1000 automatically timestamps transmitted and received frames with a precision of 40-bit. In turns, working at a nominal 64 GHz resolution, packets are timestamped with a 15.65 ps event timing precision\(^3\).

During the experimental tests, the DWM1001 SoM was configured to use UWB Channel 5 ($f_c = 6489.6$ MHz, $BW = 499.2$ MHz), a preamble length of 128 symbols, the highest Pulse Rate $PR = 64$ MHz, and the highest Data Rate $DR = 6.8$ Mbps.

B. Network infrastructure

To exploit the UWB protocol to implement an LPS, a specific number of DWM1001 module must be programmed to act as anchors and, hence, provide a reference infrastructure for the tags. In our case, the reference infrastructure comprises six reference anchors mounted on the wall of our laboratory. Each anchor is mainly composed of a Raspberry PI 3 and a DWM1001 module. Finally, data sharing and acquisition is implemented by leveraging the MQTT protocol. In this way, both anchors and tags data can be retrieved easily also by a remote system.

C. Positioning Results

To evaluate and characterise the statistical properties of the developed positioning infrastructure, two experiments were conducted. The first test is done in static conditions with a tag positioned in two known locations. Figure 4 depicts the histogram of the estimation error along the $X_w$ (left) and $Y_w$ (right) reference axes over 30000 repeated measurements.

\(^1\)https://www.decawave.com/sites/default/files/dwm1001_datasheet.pdf
\(^3\)https://www.decawave.com/dw1000/usermanual/
reflections due to the presence of metallic objects. Nonetheless, the precision is below the claimed 20 cm of error.

The second test was conducted while moving the receiver along a planned path to evaluate the effectiveness of the infrastructure, both for tracking or navigation purposes. The result is reported in Figure 5 where the green dashed line represents the planned path. The asymmetry in the estimated positions, can be explained using the Position Dilution of Precision (PDoP) (see Figure 6 for the PDoP map of the adopted environment). Although the PDoP does not consider complex non-line-of-sight and multipath problems, it can be considered a valid simple metric to express positioning accuracy [40].

As described in Section I, the main purpose of the presented solution is to determine the position of an unlimited number of assets (e.g., robots) inside the environment. As presented in Figure 7, which shows the execution time needed for receiving all the messages from the reference anchors, the positioning routine is scheduled at the receiver side. In this example, Receiver 1 completes its pose estimation before the others, while the second and the third receivers estimate their position simultaneously. This confirms that the system allows simultaneous position estimates from different tags, thus empirically prove that the system can scale up to infinity.

V. Conclusion

This paper presents the solution to the scalability problem of LPSs. The introduced DTDoA scheme enables the possibility to supply the pose information to an infinite number of entities and robots endowed with an UWB receiver. The source of uncertainties analysis highlighted the critical points for the DTDoA scheme and guided the development of an LPS with a maximum absolute position error below 20 cm. The maximum pose information update rate reached in this work is 67 Hz. In future work, we investigate alternative downlink schemes to increase the update rate of the localisation, removing the limit given by the number of active anchors. Another goal is to increase the accuracy of localisation system exploiting hybrid techniques to take care of the non-line-of-sight and multipath problems.

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