

1           **Multiple Optimal Depth Predictors Analysis (MODPA) for River Bathymetry:**  
2           **Findings from Spectroradiometry, Simulations, and Satellite Imagery**

3   Milad Niroumand-Jadidi\*<sup>a, b, c</sup>, Alfonso Vitti <sup>a</sup> and David R. Lyzenga <sup>d</sup>

4  
5   <sup>a</sup> *Department of Civil, Environmental, and Mechanical Engineering, University of Trento, Via Mesiano,*  
6   *77 - 38123 Trento, Italy. Email: m.niroumand@unitn.it*

7   <sup>b</sup> *Department of Biology, Chemistry, and Pharmacy, Freie Universität Berlin, Altensteinstraße 6, 14195*  
8   *Berlin, Germany.*

9   <sup>c</sup> *Leibniz-Institute of Freshwater Ecology and Inland Fisheries, Müggelseedamm 310, 12587 Berlin,*  
10   *Germany*

11   <sup>d</sup> *Department of Naval Architecture and Marine Engineering, College of Engineering, University of*  
12   *Michigan, 115 NAME Bldg., 2600 Draper Dr. Ann Arbor, MI 48109-2145, Michigan, USA.*  
13

14   **Abstract:**

15   Remote mapping of bathymetry can play a key role in gaining spatial and temporal insight into fluvial  
16   processes, ranging from hydraulics and morphodynamics to habitat conditions. This research introduces  
17   Multiple Optimal Depth Predictors Analysis (MODPA), which combines previously developed depth  
18   predictors along with additional predictors derived from the intensity component of the HSI color space  
19   transformation. MODPA empirically selects a set of optimal predictors among all candidates utilizing  
20   partial least squares (PLS), stepwise, or principal component (PC) regression models. The primary focus  
21   of this study was on shallow (< 1 m deep) and clearly flowing streams where substrate variability could  
22   have a pronounced effect on depth retrieval. Spectroscopic experiments were performed under controlled  
23   conditions in a hydraulic laboratory to examine the robustness of bathymetry models with respect to  
24   changes in bottom type. Further, simulations from radiative transfer modeling were used to extend the  
25   analysis by isolating the effect of inherent optical properties (IOPs) and by investigating the performance  
26   of bathymetry models in optically complex and deeper streams. The bathymetry of the Sarca River, a  
27   shallow river in the Italian Alps, was mapped using a WorldView-2 (WV-2) image, for which we  
28   evaluated the atmospheric compensation (AComp) product. Results indicated the greater robustness of  
29   multiple-predictor models particularly MODPA rather than single-predictor models, such as Optimal

30 Band Ratio Analysis (OBRA), with respect to heterogeneity of bottom types, IOPs, and atmospheric  
31 effects. The HSI intensity component enhanced the accuracy of depth retrieval, particularly in optically-  
32 complex waters and also for low spectral resolution imagery (e.g., GeoEye). Further, the enhanced  
33 spectral resolution of WV-2 imagery improved bathymetry retrieval compared to 4-band GeoEye data.

34 **Keywords:** bathymetry, river, Lyzenga model, ratio model, depth predictors, spectroscopy, WorldView-2,  
35 atmospheric compensation (AComp)

## 36 **1- Introduction**

37 Remote sensing techniques provide an alternative to traditional field-based measurements and have the  
38 potential to enhance our understanding of fluvial systems by providing spatially and temporally explicit  
39 information (Marcus and Fonstad, 2008; Carbonneau et al., 2012; Legleiter and Overstreet, 2012;  
40 Niroumand-Jadidi and Vitti, 2016; Shintani and Fonstad, 2017; Niroumand-Jadidi and Vitti, 2017a). The  
41 recent integration of remote sensing and river sciences has emerged as a growing research field termed  
42 “fluvial remote sensing” (Marcus and Fonstad, 2010; Carbonneau et al., 2012). Advancements in sensors,  
43 such as water-penetrating, green-wavelength light detection and ranging (LiDAR), or platforms, such as  
44 unmanned aerial vehicles (UAVs), have recently provided new tools for characterizing fluvial systems  
45 (Kinzel et al., 2013; Flener et al., 2013; Shintani and Fonstad, 2017). However, green LiDAR  
46 observations are mainly feasible by means of low-altitude platforms (e.g., manned aircrafts), which leads  
47 to a lower spatial and temporal coverage compared to optical sensing by means of satellites. Furthermore,  
48 the application of green LiDAR in riverine environments is hindered by low point density of observations  
49 and also the confusion among laser returns from the water surface, water column, and riverbed (Legleiter  
50 and Overstreet, 2012; Kinzel et al., 2013). UAVs offer the potential for higher spatial and temporal  
51 resolution, but at the cost of spatial coverage. In this context, passive optical remote sensing aboard  
52 airborne and spaceborne platforms remains a broadly applicable means of characterizing a wide range of  
53 attributes in fluvial systems, including bathymetry (Legleiter and Overstreet, 2012; Niroumand-Jadidi and

54 Vitti, 2016), substrate type and composition (Legleiter et al., 2016), grain size (Carbonneau et al., 2004;  
55 Niroumand-Jadidi and Vitti, 2017b), and hydromorphological units (Legleiter et al., 2004).

56 Bathymetry is one of the key applications of remote sensing to fluvial systems that facilitates  
57 understanding river form, process, and function (Shintani and Fonstad, 2017). Information on water depth  
58 can play a valuable role in mapping in-stream habitats (Carbonneau et al., 2012; Hugue et al., 2016),  
59 parameterization and analysis of hydro-morphological processes (Bryant and Gilvear, 1999; Flener et al.,  
60 2012), and river management (Fonstad and Marcus, 2005; Legleiter and Overstreet, 2012). Optical  
61 sensors onboard aerial and satellite platforms have long been used for studying shallow coastal  
62 environments (Lyzenga, 1978; Lyzenga, 1981, Philpot, 1989; Dierssen et al., 2003; Louchard et al., 2003;  
63 Lesser and Mobley, 2007). Because of their smaller spatial scales, fluvial systems have mostly utilized  
64 aerial imagery to derive bathymetric data (Winterbottom and Gilvear, 1997; Jordan and Fonstad, 2005;  
65 Walther et al., 2011; Legleiter, 2013). With recent enhancements in spatial resolution of satellite imagery,  
66 mapping river bathymetry from space is receiving more interest due to larger spatial coverage and higher  
67 temporal resolution of satellite sensors than those onboard aerial platforms. Legleiter and Overstreet  
68 (2012) performed a feasibility assessment of mapping the bathymetry of gravel-bed rivers from space  
69 using WorldView-2 (WV-2) imagery.

70 The theoretical basis for optical remote sensing of bathymetry in riverine environments is built upon  
71 research conducted in optically shallow coastal environments (Legleiter et al., 2004; Legleiter et al.,  
72 2009). Bathymetric techniques fall into two main approaches: through-water photogrammetry (Fryer,  
73 1983; Westaway et al., 2001) and spectrally based analysis (Lyzenga, 1978; Lee et al., 1998). Through-  
74 water photogrammetry utilizes stereo imagery to produce a digital elevation model by accounting for  
75 refraction of light at the air-water interface (Westaway et al., 2001; Lane et al., 2010). One particular type  
76 of photogrammetric approach known as Structure from Motion (SfM) has received growing interest for  
77 measuring bathymetry and characterizing riverbed topography (Woodget et al., 2015; Dietrich, 2017).  
78 SfM is capable of reconstructing three-dimensional geometry using multiple overlapping images taken

79 from a wide range of angles (Shintani and Fonstad, 2017). Spectrally based approaches to deriving  
80 bathymetric data can be divided into physics-based and empirical models (Brando et al., 2009; Dekker et  
81 al., 2011). The first rely on inversion of radiative transfer models and account for the physics of how light  
82 interacts with the water surface, water-column, and bottom (Lee et al., 1998; Lee et al., 1999; Lesser and  
83 Mobley, 2007; Brando et al., 2009), while the latter provide regression-based predictions of bathymetry  
84 (Lyzenga, 1978; Philpot, 1989).

85 The seminal work of Lyzenga (1978, 1981) provides a basis for empirical retrieval of water depths from  
86 optical imagery, which was the focus of this research. Lyzenga's model assumes a linear relation between  
87 an image-derived quantity ( $X$ ) and the water depth ( $d$ ), where  $X$  is a predictor obtained from log-  
88 transformation of image values in a given spectral band. Multiple regression (Lyzenga, 1985; Lyzenga et  
89 al., 2006) and ratio methods (Stumpf et al., 2003) have been demonstrated to enhance the robustness of  
90 bathymetry retrieval with respect to substrate variability and water quality heterogeneity. The first  
91 employs multiple spectral bands to perform a multiple linear regression between image-derived predictors  
92 ( $X$ ) and water depths ( $d$ ) while the latter model considers a log-transformed band ratio as a single  
93 predictor of water depth. More recently, Optimal Band Ratio Analysis (OBRA) was introduced to identify  
94 the pair of bands, among all possible pairs, for which the ratio model yields the strongest correlation with  
95 water depth (Legleiter et al., 2009). Each of these types of predictors has been reported as optimal in  
96 different case studies (Legleiter et al., 2012; Bramante et al., 2013; Jawak and Luis, 2016).

97 Further development of new techniques is required to systematically select and combine a set of  
98 predictors that provide robust retrievals in the presence of all the complicating factors that might impact  
99 depth retrieval (e.g., variations in bottom types, IOPs and water-surface roughness). We pursued five  
100 main objectives in this study:

101 (1) Developing a new approach called Multiple Optimal Depth Predictors Analysis (MODPA) for  
102 bathymetry retrieval. This method seeks to identify and incorporate optimal depth predictors among all  
103 the possible Lyzenga and ratio predictors as well as additional predictors from color space transformation.

104 The selection of optimal predictors was performed using several feature selection methods including  
105 stepwise, partial least square (PLS), and principal component (PC) regressions;

106 (2) Assessing the robustness of the proposed MODPA compared to existing models with respect  
107 to heterogeneity in substrate types, IOPs, and atmospheric effects. Bathymetry models were  
108 comprehensively examined using spectroscopic experiments, radiative transfer simulations, and WV-2  
109 imagery. The spectroscopic experiments were conducted under controlled conditions in a hydraulic  
110 laboratory and involved collecting a set of spectra in a range of water depths with variable substrates. The  
111 effects of IOPs, as influenced by chlorophyll-a (Chl-a), suspended sediment concentration (SSC), and  
112 colored dissolved organic matter (CDOM), were isolated using the simulated data. Moreover, we  
113 considered an optically complex testing scenario where bottom type and IOPs were both allowed to vary;

114 (3) Examining the performance of the proposed MODPA method for bathymetry mapping of the  
115 Sarca River, a shallow and narrow alpine river in Italy, using WV-2 imagery. This analysis quantified the  
116 effectiveness of MODPA compared to other models in the spectrally complex environment of a real case  
117 study. Different strategies were considered for the validation of results including an approach built upon  
118 comparison of image-derived depths with the estimates based on principles of river hydraulics;

119 (4) Assessing the effect of atmospheric correction on bathymetry retrieval of the Sarca River,  
120 which is an important consideration due to the low reflectivity of water bodies and accordingly sizable  
121 contribution of the atmosphere to the total at sensor radiance (Gitelson and Kondratyev, 1991; Mouw et  
122 al., 2015). The newly released surface reflectance product of DigitalGlobe (2016), called atmospheric  
123 compensation (AComp), was assessed to understand the robustness of bathymetric models with respect to  
124 atmospheric effects;

125 (5) Assessing the efficacy of WV-2 sensor's additional spectral bands compared to traditional  
126 high resolution satellite imagery (HRSI, less than 5 m pixel size) with only four bands such as GeoEye.

## 127 **2- Bathymetry from Optical Imagery**

128 In the context of optical remote sensing of water bodies, the total radiance reaching the sensor at a given  
129 wavelength  $\lambda$ ,  $L_T(\lambda)$ , consists of four main components: upwelling radiances from the bottom,  $L_b(\lambda)$ ,  
130 water column,  $L_c(\lambda)$ , and surface of the water body,  $L_s(\lambda)$ , as well as the atmospheric path radiance,  
131  $L_p(\lambda)$ . These components are summarized in the following equation (Legleiter et al., 2004; Legleiter et  
132 al., 2009):

$$133 \quad L_T(\lambda) = L_b(\lambda) + L_c(\lambda) + L_s(\lambda) + L_p(\lambda) \quad (1)$$

134 Aside from  $L_p(\lambda)$ , each of these radiance components can be associated with a specific property of the  
135 water body. For instance, the surface-reflected component of the radiance can be linked to the roughness  
136 of the water surface, which in turn is a function of local hydraulics in riverine environments and can  
137 potentially reveal information about flow velocity (Overstreet and Legleiter, 2017; Legleiter et al., 2017).  
138 Information on bathymetry is embedded in the bottom-reflected radiance component, which is affected  
139 not only by water depth but also by bottom type and indirectly by water column optical properties (Lee et  
140 al., 1998; Stumpf et al., 2003; Legleiter et al., 2009). Thus, it is essential to isolate the radiance  
141 component of interest or to reduce the effect of other extraneous components in order to retrieve the  
142 desired parameter, which in this study is the water depth.

143 Lyzenga's model (1978, 1981) is built upon the Beer-Lambert law, which describes the exponential  
144 attenuation of light travelling through the water column. This model includes a deep-water correction  
145 term,  $L_w(\lambda)$ , equated with the radiance observed over optically-deep water, to account for the radiance  
146 scattered from the water column, water surface, and atmosphere (Eq. 2).

$$147 \quad L_w(\lambda) = L_c(\lambda) + L_s(\lambda) + L_p(\lambda) \quad (2)$$

148 The bottom-reflected radiance can be considered negligible for optically-deep waters. Therefore,  
149 subtracting  $L_w(\lambda)$  from all water pixels leaves the bottom-reflected radiance, which contains bathymetry  
150 information. According to Lyzenga's model, the water depth ( $d$ ) depends linearly on the predictor ( $X$ )  
151 derived from image values in a given spectral band (Eqs. 3 and 4).

152

153  $X = \ln (L_T(\lambda) - L_w(\lambda))$  (3)

154  $d = aX + b$  (4)

155 Note that deep-water correction required for Lyzenga's model has been demonstrated to be  
156 negligible for shallow rivers (Mumby and Edwards, 2000; Flener et al., 2012; Flener, 2013). This is  
157 mainly because the bottom signal is the dominant component of radiance reaching the sensor, particularly  
158 if the image has been atmospherically corrected. Therefore, there is low probability to approach to the  
159 deep-water signal in shallow and clear rivers (Legleiter et al., 2009). Note that type of the substrate is also  
160 an important factor influencing the total water-leaving radiance. For instance, depth retrieval in very  
161 shallow waters could be hindered by the presence of a dark, low-reflectance substrate that absorbs most of  
162 the downwelling radiance. However, this would be a rare case where the bottom-reflected radiance is not  
163 sufficient to propagate through the thin water column in riverine environments. The unknown parameters  
164 ( $a, b$ ) can be estimated by means of a simple regression between  $X$  and in-situ depths ( $d$ ). However, these  
165 parameters depend on the IOPs of the water column and the bottom reflectance, which might vary within  
166 a given scene. To deal with these problems, a linear combination of the predictors ( $X_i$ ) derived from  
167 multiple ( $n$ ) spectral bands (Eq. 5) has been suggested for depth estimation (Lyzenga et al., 2006).

168  $d = \sum_{i=1}^n a_i X_i + b$  (5)

169 Note that water-surface roughness and accordingly surface-reflected radiance can also vary  
170 significantly within a given river channel on small spatial scales (Legleiter et al., 2009). These effects  
171 cause variations in near-infrared bands, which do not contain significant bottom-reflected signals because  
172 of strong attenuation of near-infrared light. Thus, scaled versions of the near-infrared bands can be  
173 instrumental for enhancing the robustness of depth retrieval with respect to variations in water surface  
174 roughness, as well as atmospheric effects (Lyzenga et al., 2006; Kay et al., 2009).

175 Stumpf et al. (2003) proposed using a ratio model for depth retrieval to mitigate the undesirable  
176 effect of variations in bottom reflectance (Eq. 6).

177 
$$X = \ln \left[ \frac{L_T(\lambda_1)}{L_T(\lambda_2)} \right] \quad (6)$$

178 The ratio model relies on the fact that different substrates at the same depth have approximately  
179 equal values of the ratio between total radiances at two different wavelengths. Such a ratio can be used as  
180 a robust depth predictor with respect to substrate variability (Stumpf et al., 2003; Flener, 2013). Note that  
181 Equation 6 is a special case of Equation 5, with  $n = 2$  and  $a_2 = -a_1$ . So this method is similar to that of  
182 Lyzenga, but does not involve deep-water correction. Legleiter et al. (2009) extended the idea of the ratio  
183 model in the form of OBRA. This model examines all the possible pairs of bands to identify the pair that  
184 provides the highest coefficient of determination ( $R^2$ ) in a regression of  $X$  against  $d$ .

185 Bathymetric models originally developed for coastal environments have only recently been translated to  
186 fluvial systems, particularly using HRSI (Legleiter and Overstreet, 2012). The key distinction between  
187 coastal and riverine environments is the thinner water-column in rivers. Therefore, a relatively high  
188 contribution from the river substrate and a relatively low contribution from the water column can be  
189 expected, especially in shallow and clearly flowing streams. Although this is advantageous for depth  
190 retrieval due to having stronger bottom-reflected radiance, the pronounced effect of substrate variability  
191 complicates depth retrieval. Moreover, as mentioned before, highly variable water-surface roughness in  
192 fluvial systems can induce additional challenges. Therefore, development of robust methods is needed to  
193 produce reliable and consistent bathymetric maps for large spatial extents using optical imagery.

### 194 **3- Multiple Optimal Depth Predictors Analysis (MODPA)**

195 Existing bathymetric models employ one or more Lyzenga predictors or a single ratio predictor. Although  
196 OBRA identifies the optimal ratio predictor, the model is based on a sole ratio predictor. The selection  
197 between predictor types (Lyzenga or ratio) can be challenging in practice, as the results of previous  
198 studies indicated that each type of predictor can possibly lead to more accurate results than the other,  
199 depending on the case study. For instance, Jawak and Luis (2016) reported that the Lyzenga model  
200 derived the bathymetry of a shallow lake (depth < 8 m) more precisely (with 15% higher  $R^2$  and 0.98 m  
201 lower RMSE) than the ratio model using WV-2 imagery. Bathymetry models that rely on a simple



202 regression (e.g., OBRA) attempt to explain the dependent variable (i.e., depth) using only one predictor;  
203 other informative predictors might be neglected.

204 This research aimed to integrate previously developed depth predictors by initially considering all of the  
205 possible Lyzenga and ratio predictors rather than relying upon only one of the predictor types. In addition,  
206 we considered some additional predictors derived from the RGB to HSI (hue, saturation, intensity) color  
207 space transformation. More specifically, the intensity component of the HSI space (hereafter called  
208 intensity) was added to the original image feature space and included as a potential predictor along with  
209 the associated Lyzenga and ratio predictors. The intensity (I) component refers to the total brightness or  
210 luminance of the pixels, which is associated with the human perception of brightness (Carper et al., 1990).  
211 The intensity component would potentially contribute to depth retrieval because the overall brightness of  
212 image pixels is influenced by the optical properties of the water body (Stumpf et al., 2003), which  
213 provides a physical basis for considering intensity components as candidate depth predictors. However, as  
214 a general rule in regression analysis, new features created through transformation of the original spectral  
215 data can provide a better discriminative ability but might not have a clear physical meaning (Markovitch  
216 and Rosenstein, 2002; Qian et al., 2012). Note that the color space transformation can be applied to each  
217 combination of three spectral bands so that several intensity bands can be added to the feature space (e.g.,  
218 four intensity bands can be derived for a 4-band GeoEye image). A multiple regression approach was then  
219 considered to retain and exploit most of the variability of the predictors. However, making use of all the  
220 predictors can pose the problem of overfitting (Howley et al., 2006). Furthermore, high dimensional  
221 predictors can invite redundant or correlated predictors which can lead to degradation of regression  
222 model's prediction accuracy (Reunanen, 2003; Howley et al., 2006). For example, 36 initial predictors  
223 can be derived from 8-band WV-2 imagery (8 Lyzenga predictors and 28 ratio predictors), and this  
224 number will increase by intensity predictors. Therefore, performing a dimensionality reduction on all the  
225 candidate predictors is essential. This study attempted to select the optimal predictors by using three

226 different regression methods: partial least squares (PLS), stepwise, and principal components (PC). The  
227 resultant optimal predictors can then be a combination of Lyzenga, ratio, and intensity predictors.

228 Stepwise regression is a systematic method for adding and removing terms (predictors) from a linear  
229 model based on their statistical significance in explaining the response variable. Stepwise regression uses  
230 the  $p$ -value of an  $F$ -statistic to test models with and without a potential term at each step. PC and PLS are  
231 both regression methods that construct new predictors called components as linear combinations of the  
232 original predictors. A subset of components then can be selected as optimal predictors in such a way as to  
233 keep most of the variability of the original predictors. The number of components can be chosen by  
234 looking at the percent of variance explained in the response variable as a function of the number of  
235 components. However, PC creates the components without considering the response variable (i.e., depth)  
236 while PLS takes the response variable into account (Haenlein and Kaplan, 2004; Matlab, 2018). The PLS  
237 regression optimizes the prediction power of the model by simultaneous implementation of  
238 dimensionality reduction and regression (Haaland and Thomas, 1988). This means that PLS minimizes  
239 the dimensionality of the data while maximizing the covariance between predictor and response variables.  
240 A detailed description of the PLS regression is given by Wold et al. (2001). These methods provide  
241 powerful modeling tools to deal with large number of predictors when the collinearity among the  
242 variables is strong (Abdi, 2003; Li et al., 2014).

#### 243 **4- Hydraulically Assisted Assessment of Bathymetry (HAAB)**

244 In previous studies, bathymetry models were assessed mainly by reserving samples selected at random  
245 from in-situ or simulation data (Legleiter et al., 2004; Legleiter et al., 2009). However, the number of  
246 field measured samples might not be sufficient for both calibration and validation of models. Moreover,  
247 assessment of the depth estimates would not be feasible in reaches not covered during the field survey. In  
248 this study, along with the traditional assessment method, we have used an additional approach, which  
249 integrates some basics of river hydraulics to estimate independent water depths for accuracy assessment.  
250 Fonstad and Marcus (2005) introduced hydraulically assisted bathymetry (HAB), which determines cross-

251 sectional depths based on principles of open channel flow in order to calibrate the bathymetry model in  
 252 the absence of in-situ data. We have used the same model but for the assessment of depth estimates,  
 253 which is termed, hereafter, as hydraulically assisted assessment of bathymetry (HAAB).

254 The basic formula of discharge (Eq. 7) and the flow resistance equation of Manning (Eq. 8) form the basis  
 255 of the HAB model (Fonstad and Marcus, 2005).

$$256 \quad Q = W\bar{d}\bar{V} \quad (7)$$

$$257 \quad \bar{V} = R^{2/3}S^{1/2}/n \quad (8)$$

258 where  $Q$  is the discharge of river.  $\bar{d}$  and  $\bar{V}$  denote average cross-sectional depth and velocity, respectively.  
 259  $W$  stands for the width of the cross-section.  $R$  is the hydraulic radius equivalent to the average depth of  
 260 cross-section ( $\bar{d}$ ).  $S$  represents the average energy gradient (channel slope), which can be extracted from  
 261 digital elevation model or counter maps (Fonstad and Marcus, 2005).  $n$  is hydraulic resistance, which can  
 262 be determined for mountain streams according to the following equation (Jarrett, 1984; Fonstad and  
 263 Marcus, 2005):

$$264 \quad n = 0.32S^{0.38}R^{-0.16} \quad (9)$$

265 By combining Eqs. 7, 8, and 9,  $\bar{d}$  can be estimated for a given cross-section based on the river discharge  
 266 ( $Q$ ), width measurement from image, and slope measurements from topographic maps/data:

$$267 \quad \bar{d} = (Q/3.12WS^{0.12})^{0.55} \quad (10)$$

268 In addition, HAB model approximates the maximum depth of each cross-section ( $d_{max}$ ) based on  
 269 Robison and Beschta's (1989) assumption:

$$270 \quad d_{max} = 2\bar{d} \quad (11)$$

271 We have estimated  $\bar{d}$  and  $d_{max}$  for a number of cross-sections along the Sarca River in order to assess  
 272 the depth estimates from the proposed MODPA compared to other techniques. The HAAB provided an  
 273 additional means of accuracy assessment, which allowed us to assess the bathymetry methods  
 274 ubiquitously along the channel and independent from in-situ depths. Note that  $Q$  is the only field

275 information required for this assessment approach, which was available from the gaging station in the  
 276 study area.

## 277 **5- Datasets**

278 The effectiveness of MODPA compared to the Lyzenga model and OBRA was examined by performing a  
 279 wide range of analyses on three independent datasets: (1) Spectroscopic experiments were performed at a  
 280 hydraulic laboratory to acquire measurements of water depth and reflectance under controlled conditions.  
 281 As substrate variability would be the key challenge for bathymetry retrieval in shallow and clearly  
 282 flowing streams, robustness of the models was examined through experiments with two different bottom  
 283 types (Section 5-1); (2) Simulated spectra were used to test the robustness of bathymetry models by  
 284 isolating the effect of IOPs and also to evaluate their performance under optically complex conditions  
 285 (Section 5-2); (3) A WV-2 image was used to map the bathymetry of the Sarca River from space  
 286 considering both top of atmosphere (TOA) and AComp reflectances. A field survey was performed to  
 287 collect in-situ depths for calibration and validation of models (Section 5-3). To perform consistent  
 288 analyses, the spectral reflectances from different sources were convolved with the spectral response  
 289 functions of the WV-2 and GeoEye sensors. The band designations of sensors are given in Table 1.

290 **Table 1.** Spectral band specifications for GeoEye and WV-2 sensors (DigitalGlobe, 2013).

<b>GeoEye</b>			<b>WV-2</b>		
Band	Center wavelength (nm)	Bandwidth (nm)	Band	Center wavelength (nm)	Bandwidth (nm)
Blue (B)	484	76	Coastal-Blue (CB)	427	62
Green (G)	547	81	Blue (B)	478	73
Red (R)	676	42	Green (G)	546	80
NIR	851	156	Yellow (Y)	608	48
			Red (R)	659	70
			Red Edge (RE)	724	50
			NIR1	833	136
			NIR2	949	187

291

### 292 **5-1- Laboratory Experiments**

293 A set of spectral reflectances was collected in an indoor hydraulic laboratory to test bathymetry models  
 294 under controlled conditions of illumination, water level, IOPs, and bottom properties. These experiments

295 are, to the best of our knowledge, the first to integrate spectroscopic and hydraulic facilities in an indoor  
296 laboratory, although similar experiments have previously been carried out by Legleiter and Overstreet  
297 (2014) in an outdoor environment. Two water flumes with different bottom properties were used to  
298 examine depth retrieval from spectral measurements (Fig. 1). Flume-1 was an 18 m long, 1 m wide and  
299 0.7 m high channel with a layer of uniform fine sand on the bottom. Flume-2 was a 6 m long, 0.4 m wide,  
300 and up to 0.4 m deep with a semi-natural substrate consisting of natural sands combined with larger (3 cm  
301 diameter) ball-shape gravels with plastic material. Suspended sediment was considered as the main  
302 parameter defining the water column optical properties due to the fact that sediment load is the primary  
303 control on the IOPs of clear rivers (Legleiter and Overstreet, 2012; Legleiter et al., 2016). SSC was about  
304  $2 \text{ g/m}^3$  whereas the variation of this parameter was negligible between two flumes.

305 The channels were equipped with a flowmeter to measure the discharge and an adjustable tailgate weir  
306 was located at the end of the flume to control the water level and ensure a uniform flow condition.  
307 Experiments were focused on an area in the longitudinal and cross-sectional middle of each channel to  
308 ensure a well-developed flow and also to mitigate as much as possible the reflections and shadows from  
309 the flume sidewalls. Moreover, two sides of the smaller flume (flume-2) were covered with a low-  
310 reflective black material in the test area to minimize possible side reflections. The water depths were  
311 measured using a point-gage. The spectra were collected by installing over the test area a fiber optic  
312 jumper cable connected to an Analytical Spectral Devices (ASD) HandHeld2 spectroradiometer that  
313 allowed measurement of reflectance in the 325–1075 nm spectral range with 1 nm spectral resolution.  
314 Unstable lighting conditions were eliminated by covering the experiment area on flume-1 while flume-2  
315 was located in a darkroom. A standard ASD illuminator was used to produce highly stable light across the  
316 full spectral range (350 – 2500 nm), which entirely covers the above mentioned operation range of the  
317 spectroradiometer. Spectra for a range of depths were collected from the two flumes by changing the  
318 water level in one cm increments. For each flow condition, three spectra were recorded as the average of

319 25 individual samples. Dark current and white reference measurements were taken and updated for each  
320 spectral recording in order to convert the raw spectra into reflectance.

321



322 **Fig. 1.** Spectroscopic experiments in a range of water depths on (a) flume-1 with a sand bed and (b) flume-2 with a  
323 gravel bed composed of semi-natural material.

## 324 5-2- Radiative Transfer Simulations

325 Radiative transfer simulations have been used previously to examine the accuracy of OBRA by isolating  
326 the effects of substrate type and SSC in shallow rivers (Legleiter et al., 2009; Legleiter and Roberts,  
327 2009). We performed simulations using the Hydrolight radiative transfer model (Mobley and Sundman,  
328 2008) to examine the proposed MODPA by isolating the effect of IOPs by manipulating Chl-a, SSC, and  
329 CDOM. Long-term measurements of water quality parameters in Italian alpine rivers reported by the  
330 Trento Environment Protection Provincial Agency (Giardino et al., 2007) were used to define the range of  
331 IOPs used in the simulations. The relatively wide range of IOPs assumed for radiative transfer  
332 simulations permitted the evaluation of bathymetric models not only in normal conditions of the Sarca  
333 River but also in extreme conditions of IOPs (relatively turbid waters). This broader range of IOPs and

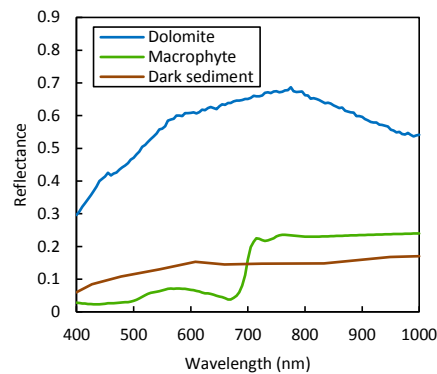
334 water depth for the simulated data can thus be used to assess the feasibility of extending our approach to  
 335 other rivers with similar optical properties.

336 The effect of each IOP was isolated by considering constant values for the other IOPs (Table 2). Note that  
 337 dolomite, which is dominant bottom type in the Sarca River study region, was considered for these  
 338 simulations and the water depth varied from 2 cm to 2 m in 2 cm increments. For each experiment, 300  
 339 spectral reflectances were simulated for which half of the data, selected at random, were used for  
 340 calibration of the models and the remaining data reserved for validation. The CDOM absorption at 440  
 341 nm,  $a_{\text{CDOM}}(440)$ , was chosen to quantify the influence of this constituent on this IOP (Kirk, 1996).

342 **Table 2.** The range of IOPs considered for Hydrolight simulations. The effect of variations in each of IOPs was  
 343 isolated by considering constant values for other IOPs.

Isolated IOP (variable)	Other IOPs (constant)
Chl-a = [1, 3, 5] mg/m <sup>3</sup>	SSC= 3 g/m <sup>3</sup> , $a_{\text{CDOM}}(440)= 0.22 \text{ m}^{-1}$
SSC= [0, 3, 6] g/m <sup>3</sup>	Chl-a= 3 mg/m <sup>3</sup> , $a_{\text{CDOM}}(440)= 0.22 \text{ m}^{-1}$
$a_{\text{CDOM}}(440)= [0.07, 0.22, 0.36] \text{ m}^{-1}$	Chl-a= 3 mg/m <sup>3</sup> , SSC= 3 g/m <sup>3</sup>

344  
 345 In addition, an optically-complex condition was also considered to explore the effectiveness of  
 346 bathymetry models by treating all of the IOPs and also the bed type as variable parameters. Three  
 347 different bottom types (dark sediment, macrophyte, and dolomite) were considered in the same range of  
 348 IOPs and water depths of previous simulations, resulting in 8100 individual spectra. Spectral reflectances  
 349 of the three bottom types are shown in Fig. 2 which are characteristics of both bright and dark substrates.



350  
 351 **Fig. 2.** Spectral reflectances of bottom types used in radiative transfer simulations.

### 352 **5-3- WV-2 Image and In-Situ Measurements**

353 An 8-band WV-2 image and its spectral convolution with GeoEye's band passes (Table 1), were used to  
354 map the bathymetry of the Sarca River. The Sarca is a mountain-piedmont gravel-bed river flowing from  
355 the Adamello glaciers down to Lake Garda in northeast Italy. It is a shallow (depth <1 m), narrow (mean  
356 width < 30 m), and clearly flowing stream which is regulated by an upstream dam that maintains a very  
357 consistent water level with a minimal sediment load during a long period of several years. A WV-2 image  
358 was used for which both TOA and AComp (Pacifci et al., 2014) reflectances were available. AComp  
359 provides an estimate of aerosol optical depth and water vapor independently in each pixel and applies the  
360 atmospheric correction by accounting for adjacency effects (Pacifci, 2016; DigitalGlobe, 2016). In  
361 addition, we spectrally convolved the WV-2 image with the spectral response function of the GeoEye  
362 sensor to gain more insight into the effectiveness of the additional spectral bands of the WV-2 imagery  
363 over traditional 4-band (RGB-NIR) HRSI like GeoEye for mapping river bathymetry.

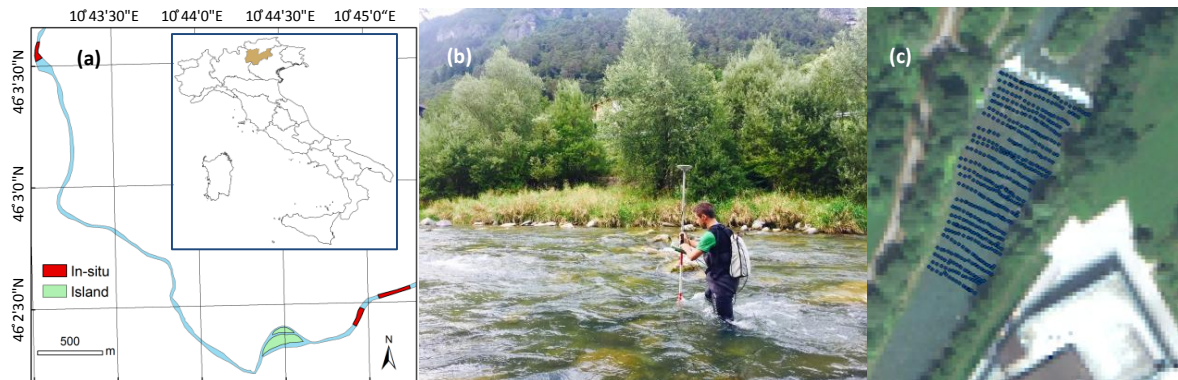
364 The field survey was carried out in three reaches along the river to gather depth samples as representative  
365 as possible for different environmental conditions (depth, bottom type, etc.). The in-situ depths were  
366 recorded with precise coordinates using RTK GPS along cross-sections with about one to two meter  
367 distances (Fig. 3). An ordinary block kriging was used to interpolate the measured depths at the pixel  
368 scale to enable a pixel-to-pixel comparison of in-situ depths with the image-derived estimates (Legleiter  
369 and Overstreet, 2012).

370

371

372





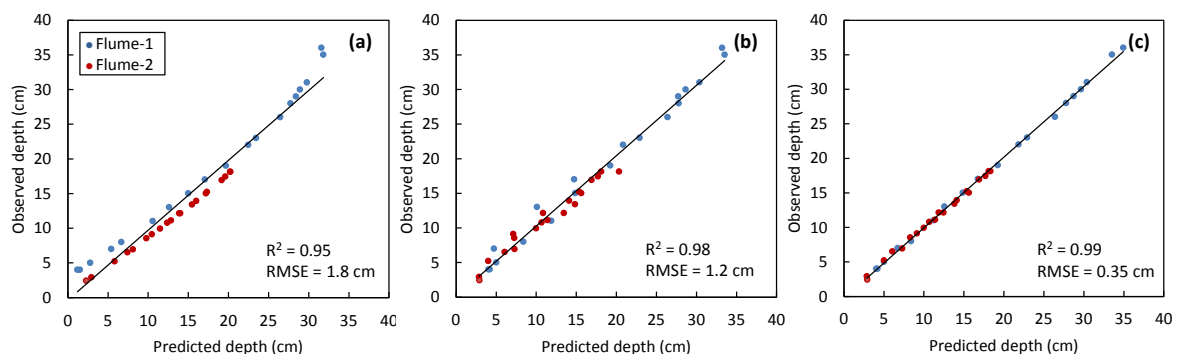
373  
 374 **Fig. 3.** In-situ measurements of water depths in (a) three reaches of the Sarca River, using (b) a RTK GPS (c) at  
 375 dense points along cross-sections. The location of river is highlighted in northeast Italy.

## 376 6- Results

377 The bathymetry models were applied to spectroscopic data collected in the laboratory, synthetic data from  
 378 radiative transfer modeling, and HRSI. Findings are presented and discussed in the following subsections.

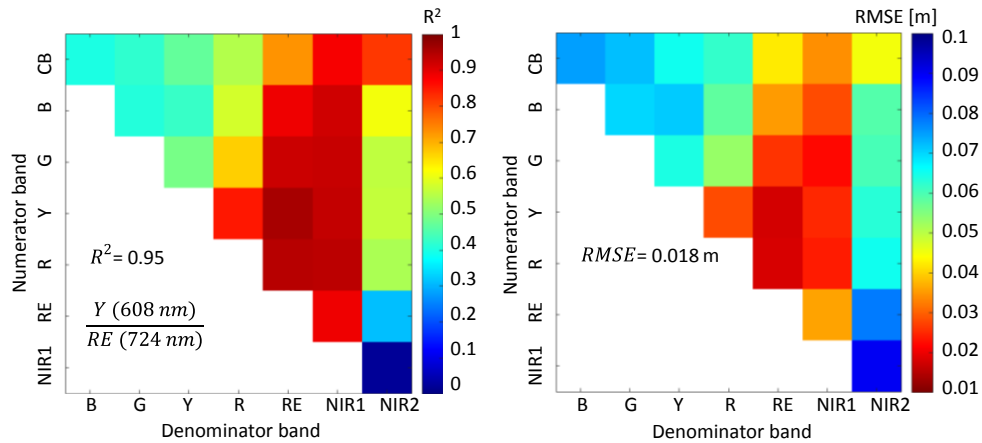
### 379 6-1- Laboratory Experiments

380 The parameters of the bathymetric models were estimated using half of the observations over both flumes,  
 381 selected at random, to gain insight into the robustness of the models with respect to substrate variations  
 382 between the flumes. Fig. 4 represents the predicted vs. observed depths using WV-2 spectra for validation  
 383 samples. For brevity, the match-ups between predicted and observed depths for the simple Lyzenga model  
 384 that provided the lowest accuracies are dropped from all figures but the accuracy statistics are provided on  
 385 bar charts.



386  
 387 **Fig. 4.** Validation of depths derived from (a) OBRA, (b) multiple Lyzenga and (c) MODPA based on PLS  
 388 regression using laboratory spectra convolved to WV-2 bands.

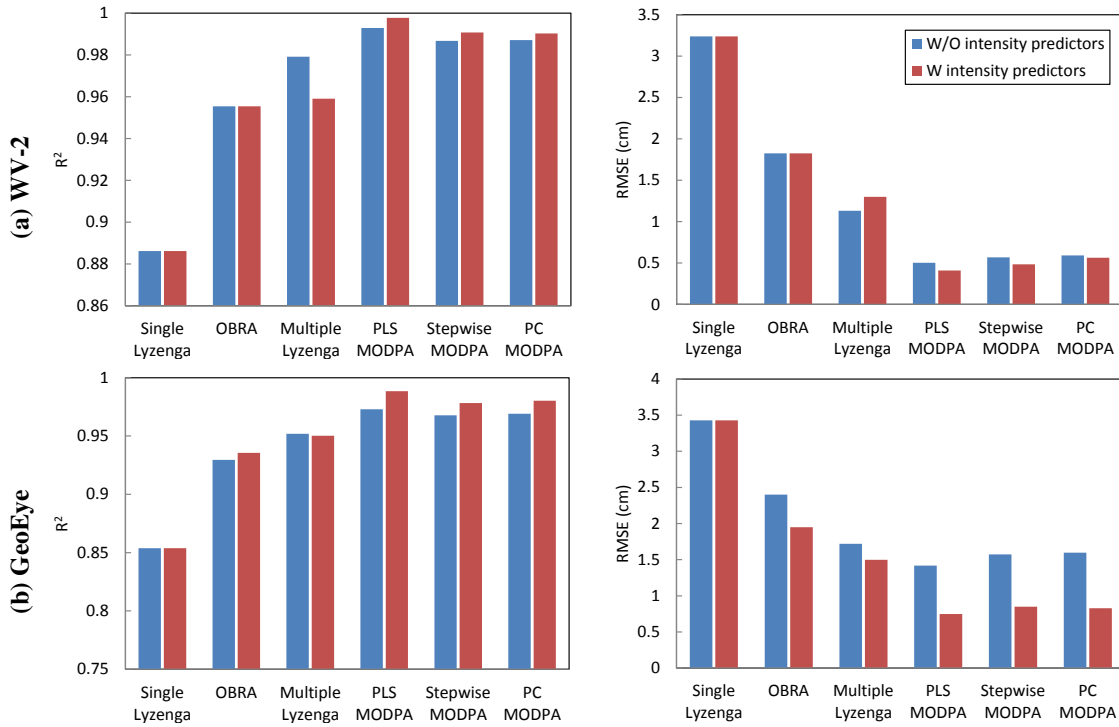
389 The OBRA matrices illustrated in Fig. 5 show the  $R^2$  and RMSE of the ratio model for all possible  
 390 combinations of spectral bands; the highest regression  $R^2$  occurred for the ratio between the yellow and  
 391 the red-edge bands (Y/RE).



392  
 393 **Fig. 5.** OBRA of laboratory WV-2 spectra representing  $R^2$  and RMSE of the ratio bathymetry model for all the  
 394 possible combination of spectral bands.

395 As evident in Fig. 4, the retrievals from OBRA were sensitive to the substrate types of the two flumes.  
 396 The relatively bright substrate in flume-1 has been confused with shallower depths while the darker  
 397 bottom-type of the flume-2 led to overestimation of depths. The multiple Lyzenga model and MODPA  
 398 were both robust with respect to substrate variability. However, the residuals from MODPA were about  
 399 four times smaller than those of multiple Lyzenga (0.35 cm vs. 1.2 cm RMSEs).

400 The accuracy statistics of bathymetry models with and without intensity predictors are compared for the  
 401 laboratory spectra convolved to both WV-2 and GeoEye bands in Fig. 6. The three different regression  
 402 approaches (i.e., PLS, stepwise and PC) provided high accuracies for the proposed MODPA. However,  
 403 MODPA based on PLS regression was slightly more accurate than the other two forms of regression. The  
 404 optimal model, PLS-based MODPA, was composed of one Lyzenga predictor derived from the RE band  
 405 and three ratio predictors derived from G/NIR1, Y/RE and R/RE ratios for the laboratory WV-2 spectra.  
 406 The extra predictors improved the accuracies of bathymetry retrievals. The improvements were more  
 407 pronounced for the spectra convolved to a lower number of bands (i.e., 4-band GeoEye), and we inferred  
 408 that the enhanced spectral resolution of WV-2 led to more accurate depth retrievals than GeoEye.



409 **Fig. 6.** Accuracy statistics ( $R^2$  and RMSE) of bathymetry models with (W) and without (W/O) intensity predictors  
 410 applied to laboratory spectra convolved to match (a) WV-2 and (b) GeoEye bands.

## 411 6-2- Synthetic Data Analysis

### 412 6-2-1- Isolating the Effect of IOPS

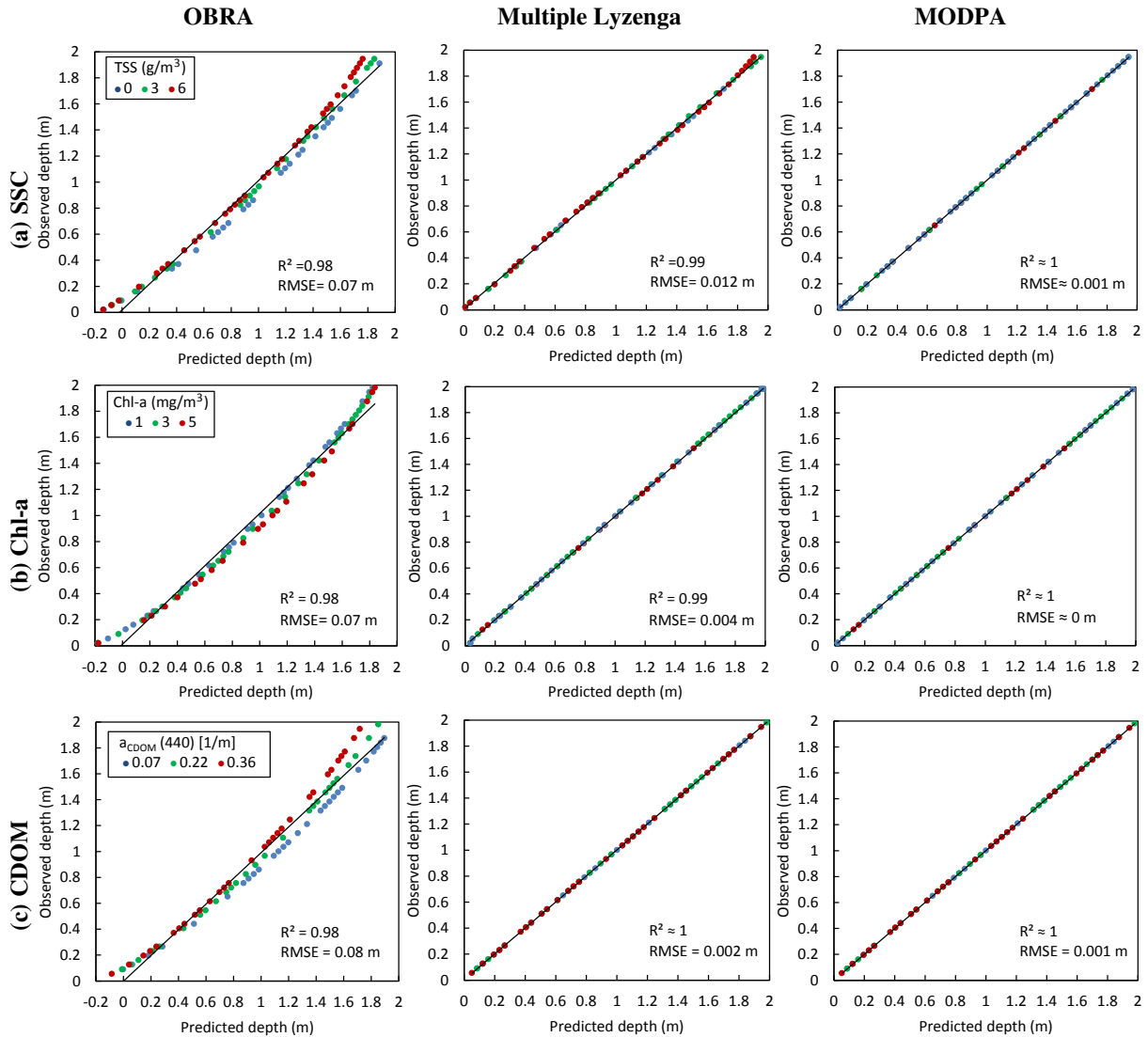
413 Fig. 7 illustrates the results of isolating the effect of variations in IOPs for waters with up to 2 m depth.  
 414 The OBRA-based retrievals were sensitive to changes in concentrations of each IOP. According to  
 415 Legleiter et al. (2009), the exponential relation between radiance and depth is subject to failure as depth  
 416 increases. This is because IOPs, particularly as influenced by SSC, imply greater scattering in a thicker  
 417 water column. As evident in Fig. 7, mismatches between the OBRA retrievals and known depths are more  
 418 pronounced for the higher depths, particularly with high SSC. The multiple Lyzenga model and MODPA  
 419 showed very good performance, but the residuals were smaller for the proposed MODPA.

420

421

422

423

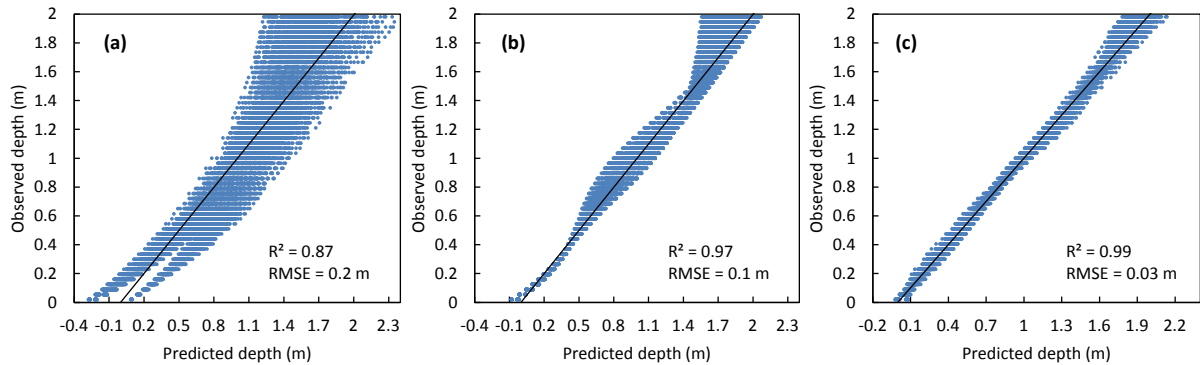


424 **Fig. 7.** Match-up validation of different bathymetry models by isolating the effect of IOPs including (a) SSC, (b)  
 425 Chl-a, and (c) CDOM.

### 426 6-2-2- Optically-Complex Shallow Waters

427 In this testing strategy, we have assumed shallow waters with variable bottom-types and IOPs (see  
 428 Section 5-2). MODPA led to the highest correlation with known depths ( $R^2 = 0.98$  and RMSE= 6 cm  
 429 without considering intensity predictors). Including the intensity predictors further enhanced depth  
 430 retrieval using MODPA (RMSE= 3 cm). This demonstrated the effectiveness of intensity predictors for  
 431 improving the robustness of bathymetry models in optically-complex waters. The match-up validations

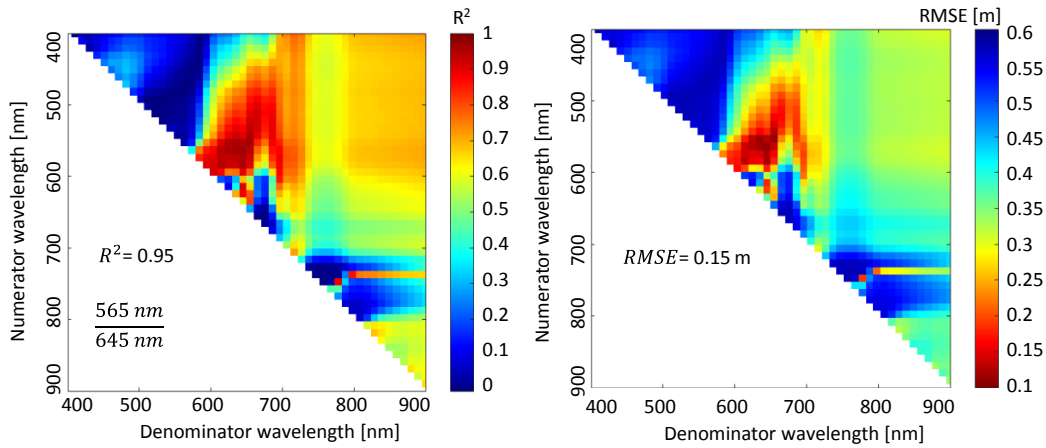
432 indicated significant improvement (i.e., 7 cm better RMSE) of depth retrieval using MODPA compared to  
433 the multiple Lyzenga model (Fig. 8).



434  
435 **Fig. 8.** Match-up validation of depth retrieval based on (a) OBRA, (b) Multiple Lyzenga and (c) MODPA with

436 intensity predictors for the optically complex spectra with variable IOPs and bottom types.

437 We performed further analysis to understand if hyperspectral data could improve the performance of  
438 OBRA in the optically-complex testing scenario. Radiative transfer simulations with a spectral resolution  
439 of 10 nm were used to perform OBRA in the spectral range of 400 nm to 900 nm. As evident in Fig. 9,  
440 depth retrieval for the optimal pair of ratio bands has been improved compared to that of 8-band WV-2  
441 data, but required very high spectral resolution (i.e., 50 bands in the range of 400 nm to 900 nm).  
442 However, the results are not comparable with MODPA (RMSE of 3 cm for MODPA vs. 15 cm for OBRA  
443 using hyperspectral data). This indicates that utilizing multiple predictors derived from a relatively low  
444 spectral resolution data (8-band WV-2) through MODPA is much more effective than when using a single  
445 predictor model like OBRA, even with high spectral resolution. Note that the wavelength position rather  
446 than the spectral resolution of hyperspectral data can also influence the performance of OBRA (Legleiter  
447 et al., 2009).



448

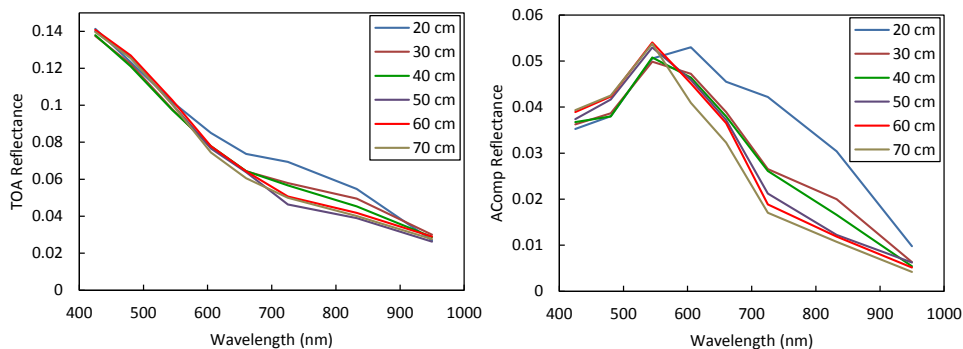
449 **Fig. 9.** OBRA of simulated spectra with 10 nm spectral resolution for the optically-complex testing scenario.

450 **6-3- WV-2 Image Analysis**

451 Atmospheric effects can make a significant contribution to the TOA radiance at short wavelengths  
 452 (mainly visible bands) due to the low reflectivity of water bodies (Gordon, 1990; Pahlevan et al., 2017).

453 Fig. 10 compares the AComp reflectances (i.e., surface reflectances) with TOA reflectances for WV-2  
 454 image pixels from a range of water depths along the Sarca River. The image-derived reflectances were  
 455 averaged for all pixels with a given depth known from the field survey. As evident in Fig. 10, atmospheric  
 456 effects were significant at short wavelengths dominated by Rayleigh scattering (Gordon 1990; Pahlevan  
 457 et al., 2017). AComp and TOA reflectances of the WV-2 image were then supplied to the bathymetry  
 458 models to investigate robustness of the models with respect to atmospheric effects.

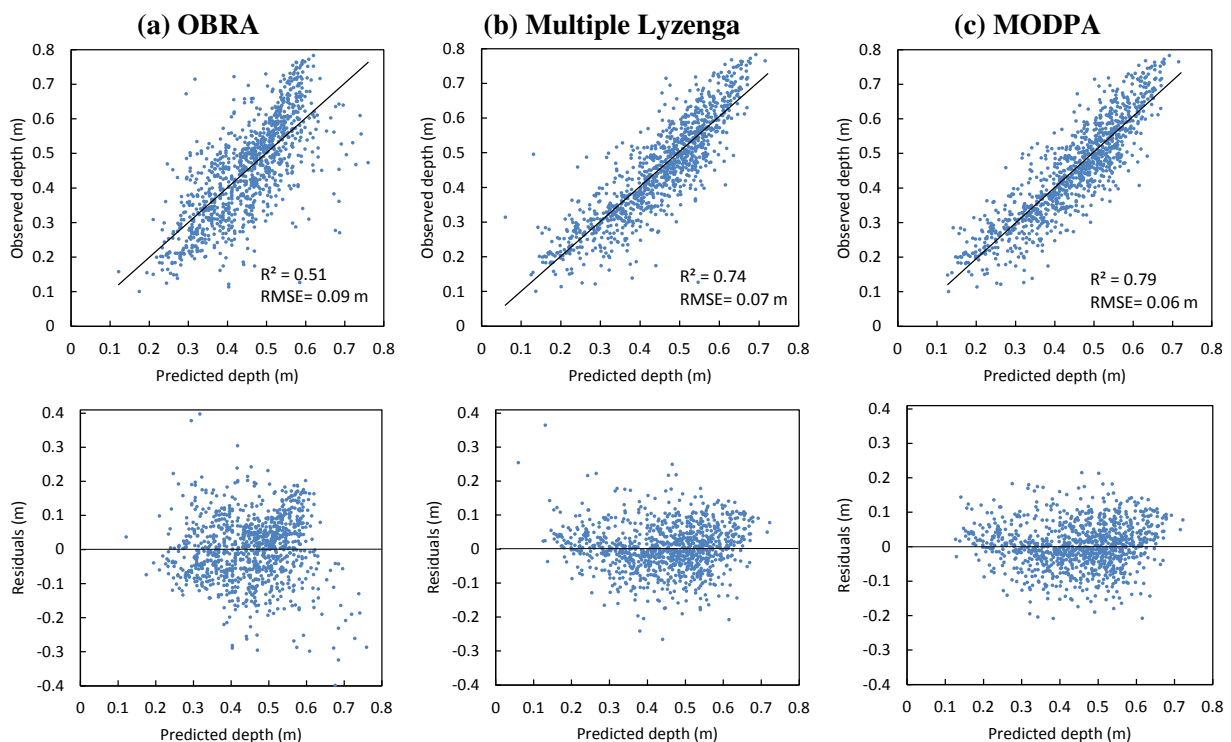
459



460

461 **Fig. 10.** Comparison of TOA and AComp reflectances of WV-2 image in a range of water depths along the Sarca  
 462 River.

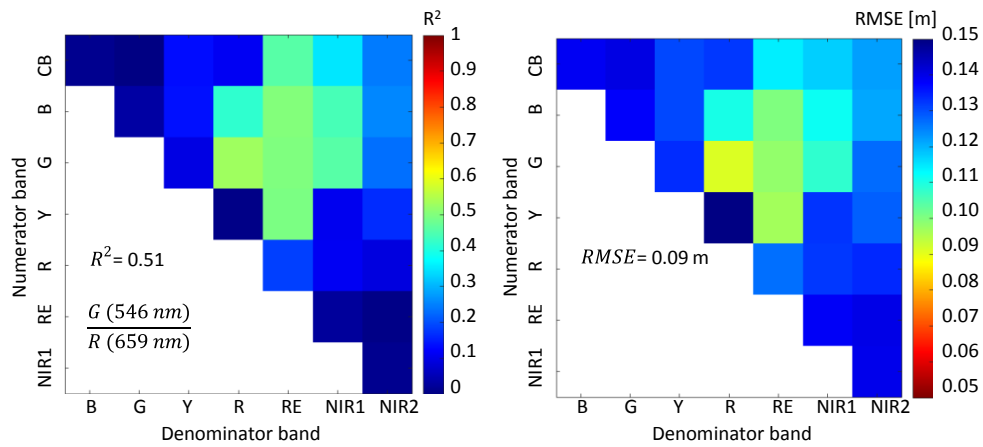
463 As first validation approach, one half of the data was reserved for calibration of models and the remaining  
 464 half for accuracy assessment. Note that substrate compositions such as algae cover and also water column  
 465 constituents can vary over distances of less than a meter in small rivers such as our case study (Fonstad  
 466 and Marcus, 2005), which can significantly complicate the depth retrieval. Fig. 11 illustrates the  
 467 validation of bathymetry models based on TOA reflectances from the WV-2 image; MODPA provided  
 468 the highest accuracy. The residual plots indicate absolute errors of up to 0.4 m for OBRA and multiple  
 469 Lyzenga methods, whereas MODPA provided depth estimates with residuals smaller than 0.2 m.



470 **Fig. 11.** Validation of depth retrieval from TOA reflectances of WV-2 image based on (a) OBRA, (b) Multiple  
 471 Lyzenga and (c) MODPA using PLS regression.

472 Fig. 12 shows the OBRA matrix obtained from TOA reflectances of WV-2 image for which G/R ratio  
 473 yielded the highest observed vs. predicted  $R^2$  (0.51) with an RMSE of 9 cm. The matrix indicates that  
 474 band ratios with a B or G numerator and a RE or NIR1 denominator as well as Y/RE ratio also provided  
 475 comparable results with the optimal band ratio (i.e., G/R). This demonstrates the potential of long  
 476 wavelengths across the near-infrared spectrum in retrieving the bathymetry in shallow and clear waters as

477 long as the water column depth is not too great and the IOPs do not dictate complete absorption or  
 478 scattering of the signal.



479 **Fig. 12.** OBRA using TOA reflectances of WV-2 image representing  $R^2$  and RMSE of the ratio model for all the  
 480 possible combination of spectral bands.  
 481

482 Fig. 13 shows the retrieved bathymetry maps from TOA reflectances compared to in-situ depths along  
 483 three reaches of the Sarca River.

484

485

486

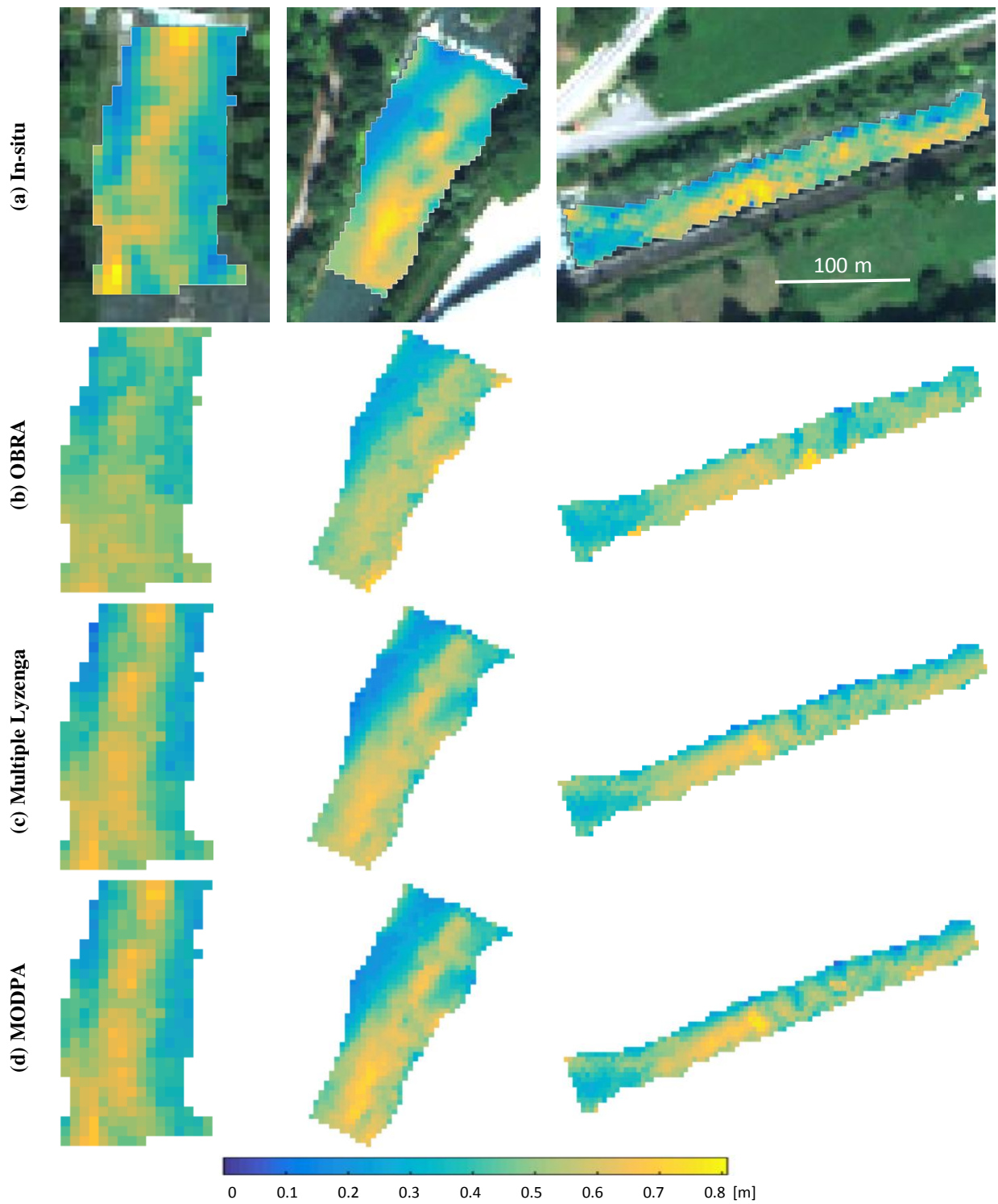
487

488

489

490





491

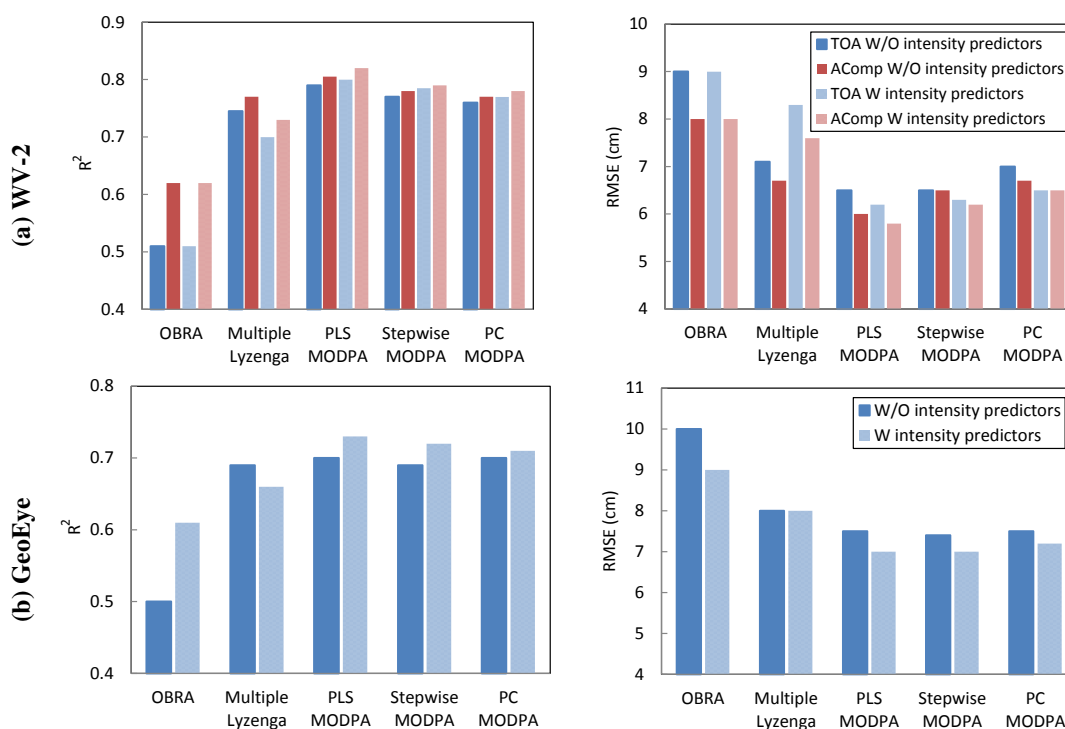
492

**Fig. 13.** Comparison of (a) in-situ depths with bathymetry maps derived from (b) OBRA, (c) Multiple Lyzenga

493

model and (d) MODPA.

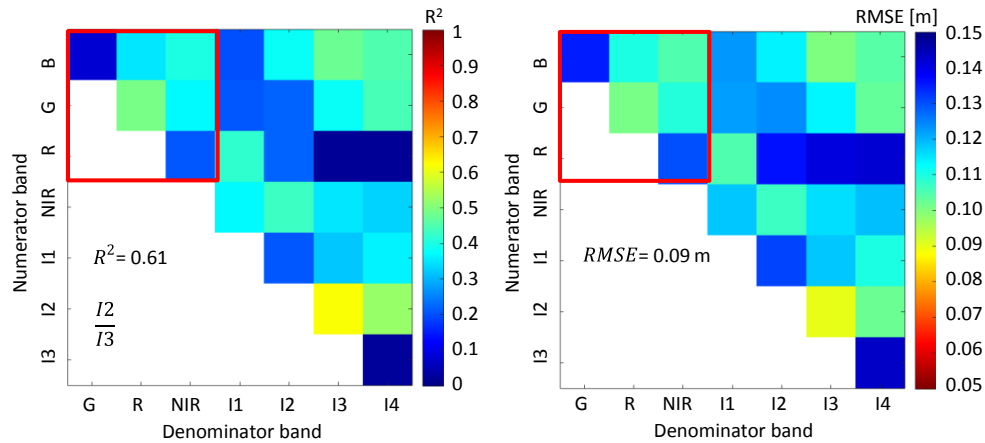
494 The accuracy statistics of bathymetry models with and without intensity predictors are compared for the  
 495 WV-2 image and its convolution to GeoEye bands in Fig. 14. In addition, AComp reflectances were  
 496 examined relative to the TOA reflectances using the WV-2 image. In general, the AComp reflectances  
 497 yielded higher accuracies than TOA reflectances. However, the accuracy enhancement was more  
 498 pronounced for OBRA, whereas MODPA was less affected by atmospheric effects. Again, the three  
 499 approaches for selection of optimal predictors provided comparable results, but the PLS regression was  
 500 slightly more accurate than the others. This model was composed of three Lyzenga predictors derived  
 501 from CB, G and RE bands and two ratio predictors derived from G/R and G/NIR1 using the WV-2 image.



502 **Fig. 14.** Accuracy statistics ( $R^2$  and RMSE) of bathymetry models with (W) and without (W/O) intensity predictors  
 503 applied on (a) WV-2 and (b) GeoEye images. The comparison also performed for the TOA and AComp reflectances  
 504 of the WV-2 image.

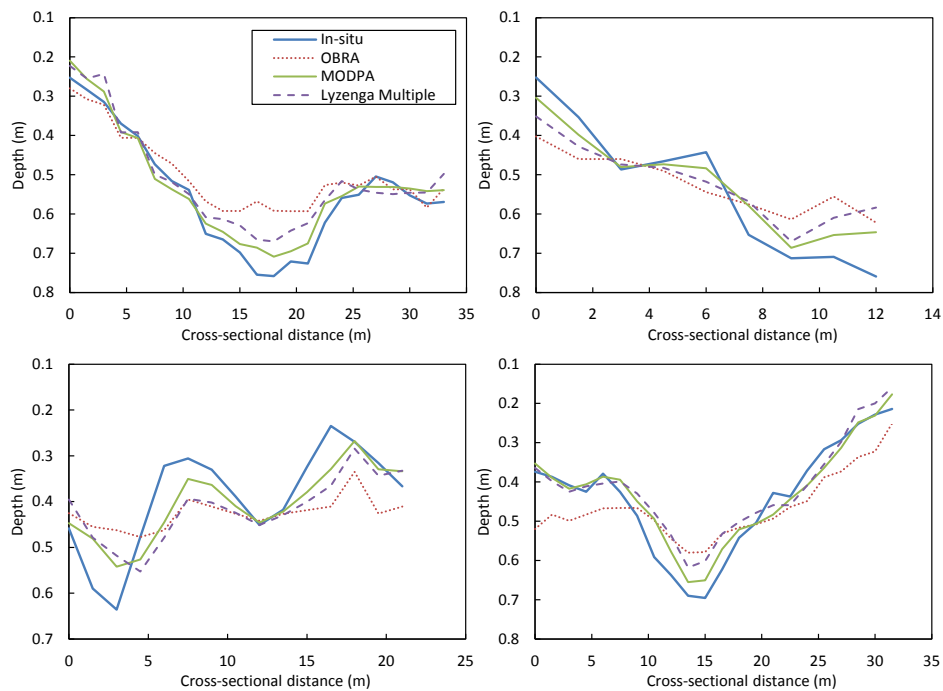
505 As can be inferred from Fig. 14, the intensity predictors in general led to an increase of  $R^2$  for all the  
 506 models except for the Lyzenga's multiple regression model. This is mainly because making use of all the  
 507 Lyzenga predictors derived from original bands and intensity components induces the overfitting problem  
 508 as well as degradation of predictive power due to the presence of irrelevant predictors. As an interesting

509 point, intensity predictors for the GeoEye image remarkably increased the accuracy of OBRA (about 0.1  
 510 enhancement of  $R^2$ ). This is shown in Fig. 15 where the optimal ratio model has been derived from  
 511 intensity (I) bands.



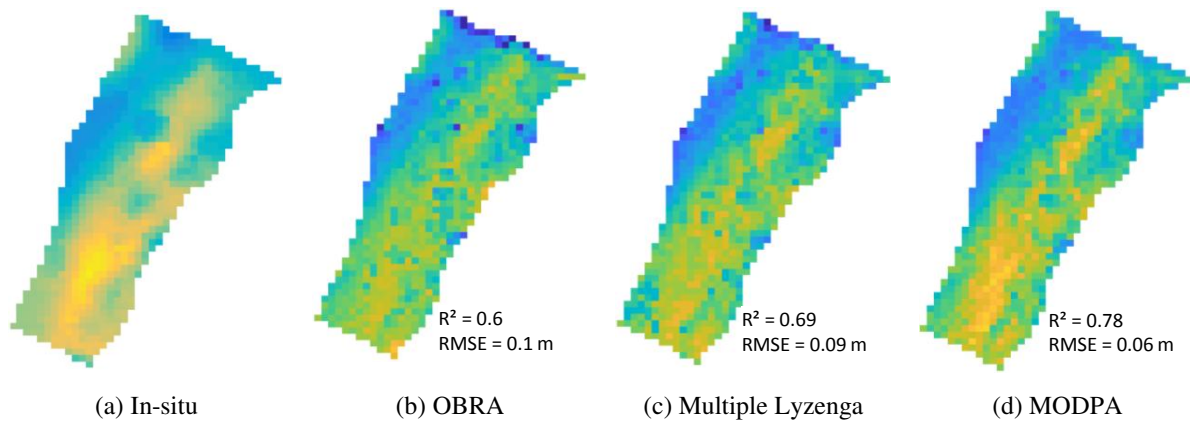
512  
 513 **Fig. 15.** OBRA of GeoEye image where the OBRA matrix derived from the original image bands (RGB color space)  
 514 is highlighted with a red box. The optimal band ratio model was derived from intensity (I) predictors.

515 Fig. 16 compares the bathymetry retrieved from the WV-2 image with in-situ observations along a few  
 516 randomly selected cross-sections.



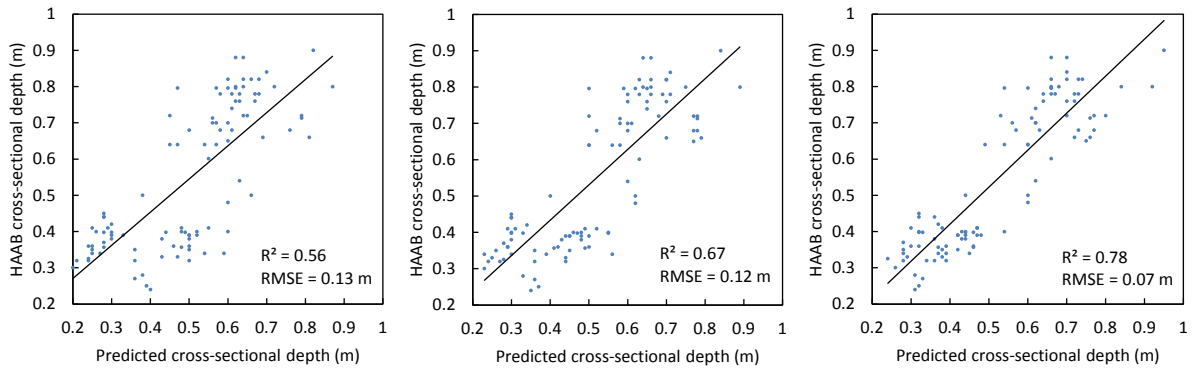
517  
 518  
 519 **Fig. 16.** Comparison of in-situ depths along cross-sections of the Sarca River with bathymetry retrieval from  
 520 different models considering intensity predictors using WV-2 image.

521 We performed an additional analysis to investigate the performance of bathymetry models with spatially  
 522 distant samples for calibration and validation. In this context, the two distal in-situ reaches were used for  
 523 calibration and the middle one for validation. Fig. 17 shows the depth maps and the accuracy statistics  
 524 derived from bathymetric models for the middle reach of the Sarca River. The results demonstrated the  
 525 increased validity and robustness of MODPA compared to other methods.



526 **Fig. 17.** Depth maps estimated for the middle reach of the Sarca River by calibrating the bathymetry models with  
 527 two distal in-situ reaches.

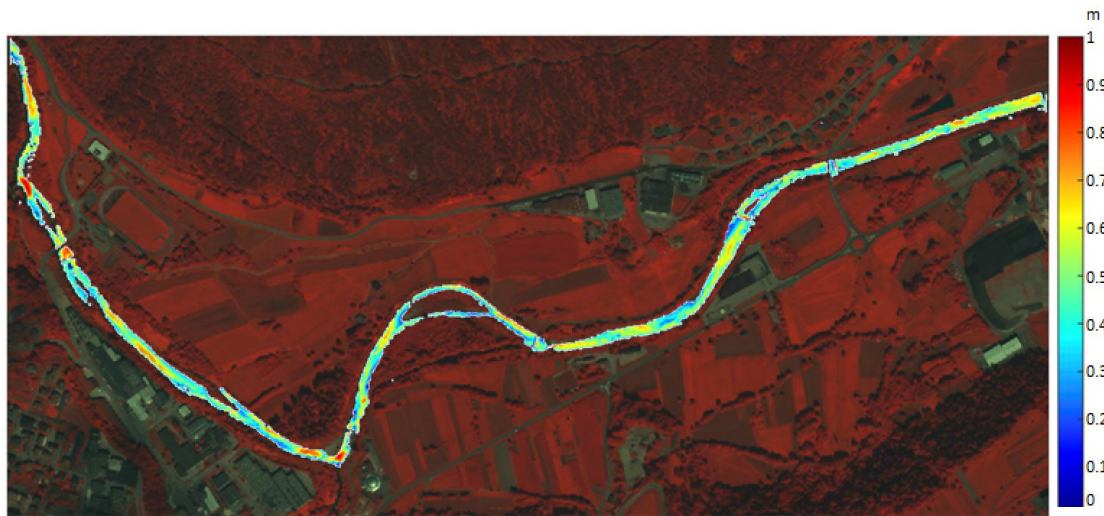
528 In addition, we estimated mean and maximum depths for 50 cross-sections regularly spaced along a 3 km  
 529 reach of the Sarca River to perform HAAB (Eqs. 10 and 11). In this regard, the discharge of the river was  
 530 available from gage records ( $Q = 4.6 \text{ m}^3/\text{s}$ ). Regional slopes of the channel were estimated from an  
 531 available LiDAR-derived digital surface model ( $0.01 < S < 0.003$ ) and cross-sectional widths ( $W$ ) were  
 532 measured on the image. The depth estimates based on HAAB allowed us to perform an independent  
 533 analysis on the efficacy of bathymetry models in reaches where no in-situ measurement was available.  
 534 The proposed MODPA resulted in a more accurate depth estimates compared to OBRA and multiple  
 535 Lyzenga models. MODPA-based depth estimates indicate enhancement of  $R^2$  on the order of 0.22 and  
 536 0.11 with RMSE improvement of 0.06 m and 0.05 m compared to OBRA and multiple Lyzenga models,  
 537 respectively (Fig. 18).



538

539 **Fig. 18.** Mean and maximum cross-sectional depths from HAAB compared with depth retrievals from WV-2 image  
 540 based on (a) OBRA, (b) Multiple Lyzenga and (c) MODPA using PLS regression.

541 The bathymetric map derived from the WV-2 image for a 5 km-long reach using the proposed MODPA  
 542 based on PLS regression is shown in Fig. 19. In addition to the quantitative assessment performed on  
 543 independent check points described above, visual inspection also supports the realism of the map, with  
 544 the pool-to-pool spacing across the reach corresponding to the theoretically established 5-7 channel  
 545 widths (Montgomery et al., 1995).



546

547 **Fig. 19.** Bathymetry map derived from the proposed MODPA based on PLS regression using WV-2 image.

## 548 7- Discussion

549 Lyzenga's single predictor demonstrated to be very sensitive to variations in substrate type and IOPs.  
 550 Although this predictor individually failed in providing depth information, it might have potential for  
 551 classifying riverbed compositions. The OBRA also failed to provide satisfactory, robust depth retrieval

552 with respect to substrate and IOPs variability. Despite identification of the optimal pair of bands for the  
553 ratio model, OBRA is a single predictor model and most likely neglects other explanatory variables even  
554 when using very high spectral resolution data. Multiple Lyzenga predictors enhanced the robustness of  
555 the model with respect to optically complicating factors in riverine environments. However, this model  
556 does not account for any process to select optimal predictors and might lead to overfitting problems that  
557 could degrade prediction accuracies due to the risk of correlated and redundant predictors. This problem  
558 would become even more significant when using high-dimensional (hyperspectral) imagery and also  
559 when considering additional candidate predictors such as intensity components used in this study. The  
560 performance of the multiple Lyzenga model on WV-2 data was degraded by including the intensity  
561 predictors. This finding highlights the significance of using MODPA to identify optimal predictors,  
562 among all the candidate predictors, including the intensity components. Moreover, intensity predictors  
563 were most significant when there were more complexities in the data (Fig. 8). This is reasonable as the  
564 main rationale for adding new predictors is to deal with complex data and enhance robustness with  
565 respect to all undesirable variations. As OBRA and proposed MODPA identify the optimal predictor/s,  
566 they yielded improved results when using intensity predictors. More specifically, the single predictor of  
567 OBRA for the GeoEye image was a combination of intensity predictors. This result shows the  
568 effectiveness of extra predictors such as intensity components for bathymetry mapping from imagery with  
569 low spectral resolution. The results of bathymetry models applied to simulated spectra further suggested  
570 the robustness of MODPA with respect to changes in IOPs (as influenced by SSC, Chl-a and CDOM) and  
571 also in optically-complex rivers where all the IOPs as well the bottom types were variable. The intensity  
572 predictors improved the results of MODPA in the testing scenario associated with the simulated optically-  
573 complex rivers (3 cm improvement of RMSE for depths up to 2 m). Moreover, the range of predicted  
574 depths for MODPA was more in agreement with the known depths whereas other methods were hindered  
575 by estimation of some negative depths in the optically-complex testing scenario (see Fig. 8).

576 The enhanced spectral resolution of WV-2 showed benefits for mapping the bathymetry of shallow rivers.  
577 For instance, the long-wavelength bands including RE and NIR1 proved to be useful as Lyzenga  
578 predictors or as the denominator of ratio-based predictors. This is mainly because light in shallow and  
579 clear rivers is not fully attenuated even for long/highly-absorbing wavelengths. On the other hand, short-  
580 wavelength bands (e.g. B, CB, G and Y) performed as appropriate numerator bands for ratio predictors. In  
581 summary, the WV-2 sensor provided a wealth of options for selecting either Lyzenga or ratio predictors  
582 and led to higher accuracies than when using 4-band GeoEye data (e.g., improvements of  $R^2$  and RMSE  
583 respectively on the order of 9% and 1 cm using TOA reflectances without intensity predictors).  
584 Comparing the TOA and AComp reflectances over a range of field-measured depths showed reasonable  
585 correction of atmospheric effects (e.g., appropriate removal of Rayleigh scattering over short  
586 wavelengths). AComp reflectances yielded higher accuracies than TOA data, with a more pronounced  
587 difference for OBRA (improvements of  $R^2$  and RMSE on the order of 11% and 1 cm, respectively).  
588 However, multiple-predictor models, particularly MODPA, showed robust bathymetry retrievals with  
589 respect to atmospheric effects. MODPA provided promising results and improvements for bathymetry  
590 retrieval in the Sarca River based on a WV-2 image. The best result was derived from MODPA based on  
591 PLS regression using AComp reflectances where  $R^2$  and RMSE were estimated as 0.82 and 5.8 cm,  
592 respectively. Although the three investigated regression methods provided very comparable results, the  
593 PLS-based regression showed slightly more accurate results. The imaged-derived bathymetry of the Sarca  
594 River validated based on two different sampling strategies for calibration of the models and also by  
595 comparing with the cross-sectional depth estimates from basic models of river hydraulics (i.e., HAAB).

## 596 **8- Conclusions and Future Work**

597 The thinner and less complex water columns of shallow and clearly flowing rivers permit the bottom  
598 component of radiance to dominate the signal reaching the sensor. Although this radiance component is  
599 desired for bathymetry retrieval, it is affected not only by water depth but also by substrate  
600 type/composition and indirectly by water column properties (IOPs). Moreover, other factors such as

601 highly variable roughness of the water surface, variable IOPs, and atmospheric effects can complicate  
602 depth retrieval in riverine environments. Therefore, development of methods robust to all these variations  
603 is essential in order to retrieve consistent bathymetric data over large spatial and temporal extents using  
604 optical imagery. This research introduced MODPA to take advantage of both Lyzenga and ratio  
605 predictors and also to integrate extra predictors obtained from the intensity component of the HSI color  
606 space. In this regard, all the possible Lyzenga and ratio predictors derived from the original image as well  
607 as the intensity components were considered as candidate predictors. A set of optimal predictors were  
608 then selected based on one of PLS, PC or stepwise regressions.

609 The proposed MODPA outperformed widely-used OBRA and multiple Lyzenga methods through three  
610 independent analyses using laboratory spectra, radiative transfer model simulations, and satellite data.  
611 The significance of MODPA was demonstrated in optically-complex waters by providing robust retrievals  
612 with respect to variations in substrate type, IOPs, water surface roughness, and atmospheric effects.  
613 Additional predictors (e.g. spectral water indices) could be included in the MODPA particularly for low  
614 spectral resolution imagery or for studies on optically-complex waters, which will be the subject of future  
615 investigations. The radiative transfer simulations were representative of a wide range of IOPs in the study  
616 region, including turbid waters. However, more research should be dedicated to study turbid rivers to  
617 further explore the potential of MODPA. The first tests on DigitalGlobe AComp indicated the  
618 effectiveness of this product for mapping the bathymetry of shallow and clearly flowing rivers. However,  
619 more studies should be dedicated to comprehensively analyze the quality of AComp product for remote  
620 sensing of inland waters.

621 Note that the key for empirical depth retrieval methods is to have a sufficient number of samples available  
622 for calibration to allow the regression model to capture the variability and complexity of the data. In the  
623 cases with limited number of in-situ samples, cross-validation approaches (Martens and Dardenne, 1998)  
624 and also the hydraulic-based approach considered in this study (i.e., HAAB) would be beneficial to



625 perform the calibration and validation of bathymetric models. Moreover, HAAB allows to examine the  
626 reliability of depth retrievals in the reaches without available in-situ depths.

627 This research demonstrated the effectiveness of spectroscopic experiments in an indoor environment of a  
628 hydraulic laboratory to study the bathymetry of very shallow waters considering variable bottom types.  
629 Experiments of this kind can be extended to study other attributes of fluvial systems such as flow velocity  
630 and water quality indicators. The proposed MODPA was demonstrated to be an efficient technique for  
631 mapping river bathymetry. However, application of this technique is restricted neither to riverine  
632 environments nor to a specific optical sensor. MODPA has the potential for application to any  
633 multi/hyper-spectral image over optically shallow inland or coastal waters. The sensor and platform type  
634 can be defined based on requirements of the case study, such as the spatial resolution. Further assessment  
635 of MODPA using freely-available Sentinel-3, Sentinel-2, and Landsat-8 imagery would be interesting in  
636 various coastal/inland applications.

### 637 **Acknowledgments**

638 This work was carried out within the SMART Joint Doctorate (Science for the Management of Rivers  
639 and their Tidal systems) funded with the support of the Erasmus Mundus programme of the European  
640 Union. The authors acknowledge the imagery grant awarded by DigitalGlobe Foundation for providing  
641 the WV-2 imagery. We acknowledge the Alexander Goetz instrument support program of ASD Inc. for  
642 awarding us a short-term usage of HandHeld2 spectroradiometer. The authors are grateful to Prof. Aronne  
643 Armanini, Prof. Maurizio Righetti and Prof. Guido Zolezzi for giving access to the hydraulic laboratory at  
644 the University of Trento and their supports during the experiments. We would like to greatly appreciate  
645 Dr. Nima Pahlevan at NASA Goddard Space Flight Center (GSFC) for providing the Hydrolight  
646 simulations. We also highly appreciate constructive comments from Dr. Patrice Carbonneau and two  
647 other anonymous reviewers, which improved the manuscript.

648

649 **References**

- 650 Abdi, H., 2003. Partial Least Square Regression (PLS Regression). In Encyclopedia of Social Science Research  
651 Methods; SAGE: Thousand Oaks, CA, USA, pp. 792–795.
- 652 Bramante, J.F., Raju, D.K., and Sin, T.M., 2013. Multispectral derivation of bathymetry in Singapore's shallow,  
653 turbid waters, *International Journal of Remote Sensing*, 34:6, 2070-2088.
- 654 Brando , V.E., Anstee, J.M., Wettle, M., Dekker, A.G., Phinn, S.R., Roelfsem, C., 2009. A physics based retrieval  
655 and quality assessment of bathymetry from suboptimal hyperspectral data. *Remote Sensing of Environment*,  
656 113, 755–770.
- 657 Bryant, R.G., Gilvear, D.J., 1999. Quantifying geomorphic and riparian land cover changes either side of a large  
658 flood event using airborne remote sensing: River Tay, Scotland. *Geomorphology*, 29 (3/4): 307–321.
- 659 Carbonneau, P., Fonstad, M.A., Marcus, W.A., Dugdale, S.J., 2012. Making riverscapes real. *Geomorphology*, 137  
660 (1), 74–86.
- 661 Carbonneau, P.E., Lane, S.N., Bergeron, N., 2006. Feature based image processing methods applied to bathymetric  
662 measurements from airborne remote sensing in fluvial environments. *Earth Surface Processes and  
663 Landforms*, 31, 1413–1423.
- 664 Carbonneau, P.E., Lane, S.N., Bergeron, N.E., 2004. Catchment-scale mapping of surface grain size in gravel bed  
665 rivers using airborne digital imagery, *Water Resources Research*, 40 (7).
- 666 Carper, W.J., T. M. Lillesand, and R. W. Kiefer, 1990. The Use of Intensity-Hue-Saturation Transformations for  
667 Merging SPOT Panchromatic and Multispectral Image Data, *Photogrammetric Engineering & Remote  
668 Sensing*, 56(4):459-467.
- 669 Dekker, A.G., Phinn, S.R., Anstee, J., Bissett, P., Brando, V.E., Casey, B., Fearn, P., Hedley, J., Klonowski, W.,  
670 Lee, Z.P., Lynch, M., Lyons, M., Mobley, C., Roelfsema, C., 2011. Intercomparison of shallow water  
671 bathymetry, hydro-optics, and benthos mapping techniques in Australian and Caribbean coastal environments.  
672 *Limnol. Oceanogr. Methods*, 9, 396–425.
- 673 Dierssen, HM, Zimmerman, RC, Leathers, RA, Downes, TV, Davis, CO. 2003. Ocean color remote sensing of  
674 seagrass and bathymetry in the Bahamas Banks by high-resolution airborne imagery. *Limnology and  
675 Oceanography*, 48: 444–455.
- 676 Dietrich, J.T., 2017. Bathymetric Structure-from-Motion: extracting shallow stream bathymetry from multi-view  
677 stereo photogrammetry. *Earth Surface Processes and Landforms*, 42: 355–364.
- 678 DigitalGlobe, 2013. spectral Response for DigitalGlobe Earth Imaging Instruments. Available at: [https://dg-cms-  
679 uploads-production.s3.amazonaws.com/uploads/document/file/105/DigitalGlobe\\_Spectral\\_Response\\_1.pdf](https://dg-cms-uploads-production.s3.amazonaws.com/uploads/document/file/105/DigitalGlobe_Spectral_Response_1.pdf),  
680 Last access on 14/6/2018.
- 681 DigitalGlobe, 2016. DigitalGlobe Atmospheric Compensation. Available online: [http://digitalglobe-  
682 marketing.s3.amazonaws.com/files/documents/AComp\\_WP\\_ACOMP.pdf](http://digitalglobe-marketing.s3.amazonaws.com/files/documents/AComp_WP_ACOMP.pdf) (accessed on 14 June 2018).

683 Durand, M., Gleason, C. J., Garambois, P. A., Bjerklie, D., Smith, L. C., Roux, H., Rodriguez, E., Bates,  
684 P.D., Pavelsky, T.M., Monnier, J., Chen, X., Di Baldassarre, G., Fiset, J.M., Flipo, N., Frasson, R.P.d.M., Fulton,  
685 J., Goutal, N., Hossain, F., Humphries, E., Minear, J.T., Mukolwe, M.M., Neal, J.C., Ricci, S., Sanders, B.F.,  
686 Schumann, G., Schubert, J. E., and Vilmin, L., 2016, An intercomparison of remote sensing river discharge  
687 estimation algorithms from measurements of river height, width, and slope, *Water Resources Research*, 52,  
688 4527–4549.

689 Flener, C., 2013. Estimating deep water radiance in shallow water: adapting optical bathymetry modeling to shallow  
690 river environments. *Boreal Environment Research*. 18: 488–502.

691 Flener, C., Lotsari, E., Alho, P., Käyhkö, J., 2012. Comparison of empirical and theoretical remote sensing based  
692 bathymetry models in river environments. *River Research and Applications*, 28 (1), 118-133.

693 Flener, C., Vaaja, M., Jaakkola, A., Krooks, A., Kaartinen, H., Kukko, A., Kasvi, E., Hyypä, H., Hyypä, J., and  
694 Alho, P., 2013, Seamless Mapping of River Channels at High Resolution Using Mobile LiDAR and UAV-  
695 Photography. *Remote Sensing*, 5, 6382-6407.

696 Fonstad, M. A., and Marcus, W. A., 2005. Remote sensing of stream depths with hydraulically assisted bathymetry  
697 (HAB) models. *Geomorphology*, 72, pp. 320–339.

698 Fryer, J.G., 1983. A simple system for photogrammetric mapping in shallow water, *Photogrammetric Record*,  
699 11(62):203-208.

700 Giardino, C., Brando, V.E., Dekker, A.G., Strömbeck, N., Candiani, G., 2007. Assessment of water quality in Lake  
701 Garda (Italy) using Hyperion. *Remote Sensing of Environment*, 109 (2), pp. 183-195.

702 Gitelson, A.A. and Kondratyev, K.Y., 1991, Optical models of mesotrophic and eutrophic water bodies.  
703 *International Journal of Remote Sensing*, 12, pp. 373–385.

704 Gordon, H.R., 1990. Radiometric considerations for ocean color remote sensors. *Applied Optics*. 29, 3228–3236.

705 Haaland, D.M., and Thomas, E.V., 1988. Partial Least-Squares methods for spectral analyses. 1. Relation to other  
706 quantitative calibration methods and the extraction of qualitative information. *Analytical Chemistry*;60:1193–  
707 202.

708 Haenlein, M., Kaplan, A.M., 2004. A beginner's guide to partial least squares analysis. *Underst. Stat*, 3, 283–297.

709 Howley, T., Madden, M.G., O'Connell, M.L., Ryder, A.G., 2006. The effect of principal component analysis on  
710 machine learning accuracy with high-dimensional spectral data. *Knowledge-Based Systems*, 19(5), 363-370.

711 Hugue, F., Lapointe, M., Eaton, B.C., Lepoutre, A., 2016. Satellite-based remote sensing of running water habitats  
712 at large riverscape scales: Tools to analyze habitat heterogeneity for river ecosystem management.  
713 *Geomorphology*, 253, 353–369.

714 Jawak, S.D., and Luis, A.J., 2016. High-resolution multispectral satellite imagery for extracting bathymetric  
715 information of Antarctic shallow lakes ", *Proc. SPIE 9878, Remote Sensing of the Oceans and Inland Waters:  
716 Techniques, Applications, and Challenges*, 987819: doi:10.1117/12.2222769.

717 Jordan, D.C., Fonstad, M.A. 2005. Two-dimensional mapping of river bathymetry and power using aerial  
718 photography and GIS on the Brazos River, Texas. *Geocarto* 20(3): 1–8.

719 Kay, S., Hedley, J.D., and Lavender, S., 2009, Sun Glint Correction of High and Low Spatial Resolution Images of  
720 Aquatic Scenes: a Review of Methods for Visible and Near-Infrared Wavelengths, *Remote Sensing*, 1, 697-  
721 730.

722 Kinzel, P.J., Legleiter, C.J., and Nelson, J.M. 2013. Mapping river bathymetry with a small footprint green LiDAR:  
723 Applications and challenges. *Journal of the American Water Resources Association*, 49(1): 183-204.

724 Kirk, J.T.O., 1996. *Light & Photosynthesis in Aquatic Ecosystems*, 2nd ed.; Cambridge University Press: Cambridge,  
725 UK.

726 Lane, S.N., Widdison, P.E., Thomas, R.E., Ashworth, P.J., Best, J.L., Lunt, I.A., Sambrook Smith, G.H., Simpson,  
727 C.J., 2010. Quantification of braided river channel change using archival digital image analysis, *Earth Surface*  
728 *Processes and Landform*, 35(8), pp. 971–985.

729 Lee, Z.P., Carder, K.L., Mobley, C.D., Steward, R.G., Patch, J.S., 1998, Hyperspectral remote sensing for shallow  
730 waters, 1. A semi-analytical model. *Applied Optics*, 37, 6329–6338.

731 Lee, Z.P., Carder, K.L., Mobley, C.D., Steward, R.G., Patch, J.S., 1999. Hyperspectral remote sensing for shallow  
732 waters, 2. Deriving bottom depths and water properties by optimization. *Applied Optics*, 38, 3831–3843.

733 Legleiter, C.J., 2013. Mapping river depth from publicly available aerial images. *River Research and Applications*,  
734 29(6): 760-780.

735 Legleiter, C.J., and Overstreet, B.T. 2012. Mapping gravel-bed river bathymetry from space. *Journal of Geophysical*  
736 *Research - Earth Surface*, 117(F04024): doi: 10.1029/2012jf002539.

737 Legleiter, C.J., and Overstreet, B.T. 2014. Retrieving river attributes from remotely sensed data: An experimental  
738 evaluation based on field spectroscopy at the Outdoor Stream Lab. *River Research and Applications*, 30(6):  
739 671-684.

740 Legleiter, C.J., and Roberts, D.A., 2009. A forward image model for passive optical remote sensing of river  
741 bathymetry. *Remote Sensing of Environment*, 113 (5): 1025-1045.

742 Legleiter, C.J., Mobley, C.D., and Overstreet, B.T., 2017. A framework for modeling connections between  
743 hydraulics, water surface roughness, and surface reflectance in open channel flows. *Journal of Geophysical*  
744 *Research - Earth Surface*, 122(9): 1715-1741.

745 Legleiter, C.J., Overstreet, B.T., Glennie, C., Zhigang, P., Fernandez-Diaz, J., and Singhanian, A. 2016. Evaluating  
746 the capabilities of the CASI hyperspectral imaging system and Aquarius bathymetric LiDAR for measuring  
747 channel morphology in two distinct river environments. *Earth Surface Processes and Landforms*, 41(3): 344-  
748 363.

749 Legleiter, C.J., Roberts, D.A., and Lawrence, R.L. 2009. Spectrally based remote sensing of river bathymetry. *Earth*  
750 *Surface Processes & Landforms*, 34(8): 1039-1059.

751 Legleiter, C.J., Roberts, D.A., Marcus, W.A., Fonstad, M.A., 2004. Passive optical remote sensing of river channel  
752 morphology and in-stream habitat: Physical basis and feasibility. *Remote Sensing of Environment*, 93, 493-510.

753 Legleiter, C.J., Stegman, T.K., and Overstreet, B.T. 2016. Spectrally based mapping of riverbed composition.  
754 *Geomorphology*, 264: 61-79.

755 Lesser, M.P., Mobley, C.D., 2007. Bathymetry, water optical properties, and benthic classification of coral reefs  
756 using hyperspectral remote sensing imagery. *Coral Reefs*, 26, 819–829.

757 Li, X., Zhang, Y., Bao, Y., Luo, J., Jin, X., Xu, X., Song, X., and Yang G., 2014. Exploring the Best Hyperspectral  
758 Features for LAI Estimation Using Partial Least Squares Regression. *Remote Sensing*, 6, pp. 6221-6241.

759 Louchard, E.M., Reid, R.P., Stephens, F.C., Davis, C.O., Leathers, R.A., Valerie, D.T., 2003. Optical remote  
760 sensing of benthic habitats and bathymetry in coastal environments at Lee Stocking Island, Bahamas: A  
761 comparative spectral classification approach. *Limnology and Oceanography*, 48 (2003), pp. 511–521.

762 Lyzenga, D.R., 1978. Passive remote sensing techniques for mapping water depth and bottom features. *Applied*  
763 *Optics*, 17, 379–383.

764 Lyzenga, D.R., 1981, Remote sensing of bottom reflectance and water attenuation parameters in shallow water using  
765 aircraft and Landsat data, *International Journal of Remote Sensing*, 2:1, 71-82.

766 Lyzenga, D.R., 1985. Shallow-Water Bathymetry Using Combined Lidar and Passive Multispectral Scanner Data.  
767 *International Journal of Remote Sensing*, 6, 115-125.

768 Lyzenga, D.R., Malinas, N.P. and Tanis, F.J., 2006. Multispectral bathymetry using a simple physically based  
769 algorithm, *IEEE Transactions on Geoscience and Remote Sensing*, 44(8), 2251-2259.

770 Marcus, W. A., and Fonstad, M.A., 2008. Optical remote mapping of rivers at sub-meter resolutions and watershed  
771 extents, *Earth Surface Processes & Landforms*, 33(1), 4–24.

772 Marcus, W. A., and Fonstad, M.A., 2010. Remote sensing of rivers: The emergence of a subdiscipline in the river  
773 sciences, *Earth Surface Processes & Landforms*, 35(15), 1867–1872.

774 Markovitch, S., and Rosenstein, D., 2002, Feature Generation Using General Constructor Functions, *Machine*  
775 *Learning*, 49, 59–98.

776 Martens, H.A., Dardenne, P., 1998. Validation and verification of regression in small data sets, *Chemometrics and*  
777 *Intelligent Laboratory Systems*, 44, pp. 99–121.

778 MATLAB, 2018, MATLAB User's Guide. The Math Works, Inc., Natick, MA.

779 Mobley, C.D., 1994. Light and water: Radiative transfer in natural waters. Academic: San Diego, USA.

780 Mobley, C.D., and Sundman, L.K., 2008. Hydrolight 5, Ecolight5 User Guide, Sequoia Scientific, Inc., Bellevue.

781 Montgomery, D.R., Buffington, J.M., Smith, R.D., Schmidt, K.M., and Pess, G., 1995. Pool spacing in forest  
782 channels. *Water Resources Research*, 31(4), 1097-1105.

783 Mouw, C.B., Greb, S., Aurin, D.A., DiGiacomo, P.M., Lee, Z., Twardowski, M., Binding, C., Hu, C., Ma, R.,  
784 Moore, T., Moses, W., Craig, S.E., 2015. Aquatic color radiometry remote sensing of coastal and inland

785 waters: challenges and recommendations for future satellite missions. *Remote Sens. Environ.* 160, 15–30,  
786 <http://dx.doi.org/10.1016/j.rse.2015.02.001>.

787 Mumby, P. J., and Edwards, A. J., 2000. Water column correction approaches. In E. P. Green, P. J. Mumby, A. J.  
788 Edwards, & C. D. Clark (Eds.), *Remote sensing handbook for tropical coastal management*. Paris: Unesco.  
789 316 pp.

790 Niroumand-Jadidi, M. and Vitti, A., 2016, Optimal Band Ratio Analysis of WorldView-3 Imagery for Bathymetry  
791 of Shallow Rivers (case Study: Sarca River, Italy), *ISPRS - International Archives of the Photogrammetry,*  
792 *Remote Sensing and Spatial Information Sciences*, Volume XLI-B8, 2016, pp. 361-364.

793 Niroumand-Jadidi, M. and Vitti, A., 2017b. Grain Size Mapping in Shallow Rivers Using Spectral Information: A  
794 Lab Spectroradiometry Perspective, *Proc. SPIE 10422, Remote Sensing of the Ocean, Sea Ice, Coastal*  
795 *Waters, and Large Water Regions 2017*, 104220B.

796 Niroumand-Jadidi, M., and Vitti, A., 2017a. Reconstruction of river boundaries at sub-pixel resolution: Estimation  
797 and spatial allocation of water fractions. *ISPRS International Journal of Geo-Information*, 6, 383.

798 Overstreet, B.T., and Legleiter, C.J. 2017. Removing sun glint from optical remote sensing images of shallow rivers.  
799 *Earth Surf Processes & Landforms*, 42(2): 318-333.

800 Pacifici, F., 2016. Atmospheric Compensation in Satellite Imagery. US Patent 9396528B2.

801 Pacifici, F., Longbotham, N., and Emery, W. J., 2014. The Importance of Physical Quantities for the Analysis of  
802 Multitemporal and Multiangular Optical Very High Spatial Resolution Images, *IEEE Transactions on*  
803 *Geoscience and Remote Sensing*, 52(10),6241-6256.

804 Pahlevan, N., Roger, J.-C., Ahmad, Z., 2017. Revisiting short-wave-infrared (SWIR) bands for atmospheric  
805 correction in coastal waters. *Optics Express*, 25 (2017), pp. 6015-6035.

806 Philpot, W. D. 1989. Bathymetric mapping with passive multispectral imagery. *Applied Optics*, 28: 1569–1578.

807 Qian, Y., Ye, M., and Zhou, J., 2012, Hyperspectral Image Classification Based on Structured Sparse Logistic  
808 Regression and Three-Dimensional Wavelet Texture Features, *IEEE Transactions on Geoscience and Remote*  
809 *Sensing*, VOL. 51, NO. 4, 2276-2291.

810 Reunanen, J., 2003. Overfitting in Making Comparisons Between Variable Selection Methods. *Journal of Machine*  
811 *Learning Research*, 3, 1371-1382.

812 Shintani C., and Fonstad, M.A., 2017. Comparing remote-sensing techniques collecting bathymetric data from a  
813 gravel-bed river, *International Journal of Remote Sensing*, DOI: 10.1080/01431161.2017.1280636.

814 Stumpf, R. P., Holderied, K., and Sinclair, M., 2003. Determination of water depth with high-resolution satellite  
815 imagery over variable bottom types. *Limnology and Oceanography*, 48, pp. 547–556.

816 Walther, S.C., Marcus, W.A., Fonstad, M.A., 2011. Evaluation of high resolution, true colour, aerial imagery for  
817 mapping bathymetry in a clear water river without ground-based depth measurements. *International Journal*  
818 *of Remote Sensing*, 32 (15), pp. 4343–4363.

- 819 Westaway, R.M., Lane, S.N., and Hicks, D.M., 2001. Airborne remote sensing of clear water, shallow, gravel-bed  
820 rivers using digital photogrammetry and image analysis. *Photogrammetric Engineering and Remote Sensing*,  
821 67: pp. 1271–1281.
- 822 Winterbottom, S. J., and Gilvear, D. J., 1997. Quantification of channel bed morphology in gravel-bed rivers using  
823 airborne multispectral imagery and aerial photography, *Regulated Rivers: Research & Management*, 13(6),  
824 489–499.
- 825 Wold, S., Sjostrom, M., and Eriksson, L., 2001. PLS-regression: a basic tool of chemometrics, *Chemometrics and*  
826 *Intelligent Laboratory Systems*, 58(2), 109–130.
- 827 Woodget, A.S., Carbonneau, P.E., Visser, F., and Maddock, I.P., 2015. Quantifying submerged fluvial topography  
828 using hyperspatial resolution UAS imagery and structure from motion photogrammetry. *Earth Surface*  
829 *Processes and Landforms*, 40: 47–64.