

Spider weight dragging and lifting mechanics

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Abstract

Spiders can produce different types of silk for a variety of purposes, such as making webs for capturing prey, sheets for wrapping, anchorages for connecting threads to surfaces, nest-building, cocoons for protecting eggs, dragline for safe locomotion and ballooning. An additional mechanism, only recently video recorded and never discussed in the literature, is spider weight lifting. Of conceptual importance comparable to that of other key spider mechanisms such as ballooning, spider weight lifting –preceded by a dragging phase for vertical alignment of weight and anchorage– is studied here. It emerges as a smart technique, allowing a single spider to lift weights in principle of any entity just using a tiny pre-stress of the silk. Such a pre-stress already occurs naturally with the weight of the spider itself when it is suspended from a thread. Large deformations, high ultimate strain, nonlinear stiffening, re-tensioning of the silk fibers and extra height of the anchoring points are all characteristics of empirical spider silk and of this lifting technique. It will be demonstrated that they all help to increase the efficiency of the mechanism. Toy experiments inspired by the spider lifting are finally proposed.

Introduction

The aim of this work is to investigate an additional spider ability, only recently recorded and never discussed in the literature, this is the lifting weights. In the spider lifting mechanism the silk constitutive law, in particular the material stiffening and high ultimate strain, is key to the functionality of the technique. Also re-tensioning of the silk fibers and an extra height anchoring point are shown to increase the efficiency of the mechanism. The unique recorded video of a spider *Olios coenobitus* lifting the empty shell of a snail is available online (<https://www.youtube.com/watch?v=-n8nbL2ZBBU>): in the first phase dragging of the shell on the bottom surface is observed for vertically aligning it with the anchorage point, Figures 1; in the second phase, shell lifting takes place. Note that other spiders, such as *Phonognatha graefei*, are able to lift large leaves into their webs to build a retreat, but this happens in several days and not minutes as observed in this case and type of mechanism. We are investigating the ability of other types of spiders, even more efficient than *Olios coenobitus*, to make direct observations in the lab.

In the following, the mechanics of the spider's weight dragging and lifting is elucidated. Large deformations, high ultimate strain and nonlinear stiffening seem to be key for this mechanism and are all characteristics of the empirical silk.

In particular, the properties of spider silks and webs, ranging from the protein sequence (Lefevre et al. 2007) of the silk to the geometry of the web (Vollrath and Mohren 1985), have intrigued scientists as highly adapted materials and structures (Vollrath 2010, Vollrath and Knight 2001), with exemplary mechanical properties and robustness (Agnarsson et al. 2010; Du et al. 2006; Shao and Vollrath 2002; Omenetto and Kaplan 2010; Ko et al. 2002, Liu et al 2005, Swanson et al 2006). The spider (genome) is a prime example of Nature's evolutionary success. Its silk can surpass high energy-absorbing materials such as Kevlar in toughness, and can be comparable in strength to steel and in density to water thus providing an extremely light-weight alternative (Gosline et al. 1999; Vollrath 2010; Agnarsson et al. 2010; Swanson et al. 2009). In particular, major ampullate/dragline silk is super tough (i.e. more than Kevlar)

while entirely different silks from different glands (many of which predate dragline silk) are used for eggsacs (tubuliform), attachments (pyriform) and so on, and these have vastly different properties. Moreover, a combination of high tensile strength on par with steel of 1–2 GPa and extensibility up to 60% of maximum strain (Swanson et al. 2009) results in superior toughness, and exceeding performance when normalized by its density. Spiders utilize these unique material properties to construct structures which serve a variety of purposes. Indeed, beyond catching insects as prey, spider silk has evolved to fulfill many functions such as the construction of egg sacks and cocoons (Rammensee et al. 2008) or attachment disks (Sahni et al 2012), making it one of the most versatile known materials (Shao and Vollrath 2002; Vollrath et al. 1996) leading to interest in either natural (Lazaris A et al 2002) or artificial production processes (Lin et al 2015). Interest in understanding these materials and structures (Aoyanagi and Okumura 2010; Ko and Jovicic 2004; Alam et al. 2007) has led to recent studies at the molecular scale (Keten et al. 2010; Keten and Buehler 2010) of the silks, as well as to the mechanical characteristics of web-like structures (Aoyanagi and Okumura 2010; Ko and Jovicic 2004; Alam et al. 2007; Alam and Jenkins 2005). In particular, spider webs are fascinating examples of natural structural engineering essential for an animal's survival (Hansell 2005; Tarakanova and Buehler 2012). In parallel, spider architecture including the adhesion of anchorages (Varenberg et al. 2010, Pugno 2011) provides inspiration to structural engineers while matching the remarkable properties of silk fibers presents a challenge to materials scientists (Bosia et al. 2010; Pugno 2007). Structural detail can also change material properties and taking inspiration from spider web junctions it has been possible to produce the toughest fibers yet (1400J/g; spider silk around 200J/g, Kevlar about 100J/g) thanks to the insertion of loops and sliding knots for dissipating energy via friction (Pugno 2014, Berardo et al 2016, Pantano et al 2016, Bosia et al 2016).

However, from a mechanical perspective, it still remains relatively unknown how silk's distinct material behaviour influences the functionality of the structures. That being said, recent work suggests that the considering structure separately from materials is no longer sufficient – material properties govern the

structure and vice versa, creating heightened functionality through synergistic interactions (Agnarsson and Blackledge 2009; Sensenig et al. 2010; Opell and Bond 2001). For example, a spider may vary the properties of a piece of thread depending on its placement in the web (Boutry and Blackledge 2009). A complete understanding of the silk/structure synergy, therefore, requires the merging of studies on material and structural performance, as recently investigated for spider webs (Cranford et al. 2012) and anchorages (Pugno et al. 2013).

Universal constitutive law, large deformations and “natural” pre-stress

With this aim, let us consider the initial configuration as described in Figure 3 (top left panel), where thus the initial horizontal and vertical distances between centroid of the weight W and point of anchorage (origin of the reference system) are given by x_0, y_0 . We consider a nonlinear elastic constitutive law of the silk, stress σ vs strain ϵ , in the general form $\sigma = g(\epsilon)$. We consider large deformations of the silk and thus its strain is calculated as $\epsilon = \ln\left(\frac{l'}{l}\right)$, where l' is the final length and l is the initial one. Fibers with imposed pre-stress σ are inserted between weight and anchorage, resulting in the first phase of dragging (Figure 1 and 3 top right panel), terminating with the vertical alignment of the weight centroid and point of anchorage (Figure 3 bottom left panel), and in the second phase of lifting (Figure 2 and 3 bottom right panel) the weight. A plausible estimation of the pre-stress σ is its “natural” value due to the body weight w of the spider when suspended on the silk, i.e., $\sigma = \frac{w}{A}$, with A cross-sectional area of the silk fiber. This would be for example the pre-stress of the first silk fiber used for lifting if its deformed length, due to the spider’s weight, is exactly equal to the distance between weight and anchorage. Lower pre-stresses are obviously possible as are larger ones if muscular forces are activated; thus, in general, $\sigma = \beta \frac{w}{A}$, where $\beta > 0$ and “naturally” $\beta \cong 1$.

Dragging

As stated, in the first phase the weight is not lifted but dragged on the bottom surface towards the vertical alignment with the anchorage. Initially, n_0 silk fibers of length l_{00} and pre-stress σ_{00} are inserted between weight and anchorage (Figure 3 top right panel) causing the first movement of the weight. Note that $l_0 = l_{00}e^{\varepsilon_{00}} = l_{00}e^{g^{-1}(\sigma_{00})} = \frac{x_0}{\sin\vartheta_0} = \frac{y_0}{\cos\vartheta_0}$, being ϑ_0 the initial angle of the fiber with respect to the vertical direction, from which we could derive l_{00} . The number n_0 can be calculated imposing the horizontal equilibrium of the weight, i.e., $n_0\sigma_{00}\sin\vartheta_0 = (W/A - n_0\sigma_{00}\cos\vartheta_0)\mu_s$, where μ_s is the static friction coefficient between weight and substrate and as stated $\sigma_{00} = g\left(\ln\left(\frac{l_0}{l_{00}}\right)\right)$, $\sin\vartheta_0 = \frac{x_0}{l_0}$, $\cos\vartheta_0 = \frac{y_0}{l_0}$ and $l_0 = \sqrt{x_0^2 + y_0^2}$. This first step movement stops at a position x_1 that can be deduced, neglecting dynamic effects, by the same equilibrium considering the de-tensioning of the fibers during movement and the dynamic friction coefficient μ_d (between weight and substrate), i.e., $n_0\sigma_{01}\sin\vartheta_1 = (W/A - n_0\sigma_{01}\cos\vartheta_1)\mu_d$, where σ_{01} is the actual stress in the n_0 fibers at the end of step 1 and is given by $\sigma_{01} = g\left(\ln\left(\frac{l_1}{l_{00}}\right)\right)$ as well as $\sin\vartheta_1 = \frac{x_1}{l_1}$, $\cos\vartheta_1 = \frac{y_0}{l_1}$ and $l_1 = \sqrt{x_1^2 + y_0^2}$. After this first step, a second one can take place inserting new fibers of unstretched length l_{01} and in number n_1 that can be calculated from the new force equilibrium of the weight, i.e., $n_0\sigma_{01}\sin\vartheta_1 + n_1\sigma_{11}\sin\vartheta_1 = (W/A - n_0\sigma_{01}\cos\vartheta_1 - n_1\sigma_{11}\cos\vartheta_1)\mu_s$ with $\sigma_{11} = g\left(\ln\left(\frac{l_1}{l_{01}}\right)\right)$; it causes the movement of the weight up to a position x_2 , that again can be calculated, considering the dynamic friction coefficient and the de-tensioning of the fibers, from the following force equilibrium: $n_0\sigma_{02}\sin\vartheta_2 + n_1\sigma_{12}\sin\vartheta_2 = (W/A - n_0\sigma_{02}\cos\vartheta_2 -$

$n_1 \sigma_{12} \cos \vartheta_2) \mu_d$ with $\sigma_{02} = g\left(\ln\left(\frac{l_2}{l_{00}}\right)\right)$, $\sigma_{12} = g\left(\ln\left(\frac{l_2}{l_{01}}\right)\right)$, $\sin \vartheta_2 = \frac{x_2}{l_2}$, $\cos \vartheta_2 = \frac{y_0}{l_2}$ and $l_2 = \sqrt{x_2^2 + y_0^2}$. In general, at step j , we found the following dragging equations:

$$n_j = \frac{\mu_s W / A - \frac{x_j + \mu_s y_0}{\sqrt{x_j^2 + y_0^2}} \sum_{i=0}^{j-1} n_i g\left(\ln\left(\frac{\sqrt{x_j^2 + y_0^2}}{l_{0i}}\right)\right)}{g\left(\ln\left(\frac{\sqrt{x_j^2 + y_0^2}}{l_{0j}}\right)\right) \frac{x_j + \mu_s y_0}{\sqrt{x_j^2 + y_0^2}}} \quad (1a)$$

$$n_j g\left(\ln\left(\frac{\sqrt{x_{j+1}^2 + y_0^2}}{l_{0j}}\right)\right) \frac{x_{j+1} + \mu_d y_0}{\sqrt{x_{j+1}^2 + y_0^2}} + \frac{x_{j+1} + \mu_d y_0}{\sqrt{x_{j+1}^2 + y_0^2}} \sum_{i=0}^{j-1} n_i g\left(\ln\left(\frac{\sqrt{x_{j+1}^2 + y_0^2}}{l_{0i}}\right)\right) = \mu_d W / A \quad (1b)$$

Note that for the limiting case of anchorage on the surface ($y_0 = 0$) eqs. (1) simplify in:

$$n_j = \frac{\mu_s W / A - \sum_{i=0}^{j-1} n_i g\left(\ln\left(\frac{x_j}{l_{0i}}\right)\right)}{g\left(\ln\left(\frac{x_j}{l_{0j}}\right)\right)} \quad (2a)$$

$$n_j g\left(\ln\left(\frac{x_{j+1}}{l_{0j}}\right)\right) + \sum_{i=0}^{j-1} n_i g\left(\ln\left(\frac{x_{j+1}}{l_{0i}}\right)\right) = \mu_d W / A \quad (2b)$$

Different strategies are possible and can strongly affect the dragging and, as we will see, the lifting mechanism too. Let us focus on two strategies of “limiting” complexity. A simple strategy considers unstretched fiber lengths $l_{0i} = l_{00} = \text{const}$ at all the steps j (i) whereas a complex one (ii) considers the insertion of the new fibers n_j with a pre-stress $\sigma = g(\epsilon)$ and the simultaneous re-tensioning of the other $\sum_{i=0}^{j-1} n_i$ fibers at the same level of stress or strain, i.e., $l_{0i} = l_{00} = l_{j-1} e^{-\epsilon}$. Note that after this operation the stress in the fibers is not anymore σ due to de-tensioning, as imposed by the force equilibrium. Also note that fibers removal/cutting can also be considered by correspondingly reducing the numbers n_j .

For the simple or complex strategy, eqs. 1 become respectively:

$$N_j = \sum_{i=0}^j n_i = \frac{\mu_s W / A}{g \left(\ln \left(\frac{\sqrt{x_j^2 + y_0^2}}{l_{00}} \right) \right) \frac{x_j + \mu_s y_0}{\sqrt{x_j^2 + y_0^2}}} \quad (3a)$$

$$N_j g \left(\ln \left(\frac{\sqrt{x_{j+1}^2 + y_0^2}}{l_{00}} \right) \right) \frac{x_{j+1} + \mu_d y_0}{\sqrt{x_{j+1}^2 + y_0^2}} = \mu_d W / A \quad (3b)$$

or:

$$N_j = \sum_{i=0}^j n_i = \frac{\mu_s W / A}{g \left(\ln \left(\frac{\sqrt{x_j^2 + y_0^2}}{\sqrt{x_{j-1}^2 + y_0^2}} \right) + \varepsilon \right) \frac{x_j + \mu_s y_0}{\sqrt{x_j^2 + y_0^2}}} \quad (4a)$$

$$N_j g \left(\ln \left(\frac{\sqrt{x_{j+1}^2 + y_0^2}}{\sqrt{x_j^2 + y_0^2}} \right) + \varepsilon \right) \frac{x_{j+1} + \mu_d y_0}{\sqrt{x_{j+1}^2 + y_0^2}} = \mu_d W / A \quad (4b)$$

Note that from eq. (3b) we can deduce the minimal value $x_{j+1}^{min} = \sqrt{l_{00}^2 - y_0^2}$ achievable by the simple strategy (i) and thus for having $x_{j+1} = 0$ we must have $l_{00} \leq y_0$; however, an intermediate complexity strategy (iii) could be proposed as a series of cycles each of them following the simple strategy (i) with subsequent shorter lengths l_{00} , considered up to a value of $l_{00} = y_0$ for reaching the vertical alignment. The end of the first phase arises when $x_{j+1} = 0$, achievable only for $l_{00} \leq y_0$ in the first strategy (i) and without limitation in the second strategy (ii), after the insertion of:

$$N_I = \frac{W}{\sigma A} \quad (5)$$

total number of fibers, where $\sigma = g\left(\ln\left(\frac{y_0}{l_{00}}\right)\right)$ (i) or $\sigma = g\left(\ln\left(\frac{y_0}{\sqrt{x_{j-1}^2 + y_0^2}}\right) + \varepsilon\right) \cong g(\varepsilon)$ (ii)

respectively.

At the end of this first dragging phase the weight is vertically aligned with the anchorage and fully suspended by the stressed silk fibers and thus the second phase of lifting can start (Figure 3 and 3b bottom right panel). Let us assume the validity of eq. (5), thus all the fibers display the same stress at the end of the first phase; this hypothesis is not limiting the generality of the results and could be easily removed by following the presented rational.

Lifting

During the second phase, other new silk pre-stressed fibers, with different lengths and thus pre-stresses, are connected one by one between weight and anchorage. After the insertion of j fibers, the vertical force balance of the weight yields the following lifting equation:

$$\frac{W}{A} = N_I \sigma = N_I \sigma' + \sum_{i=1}^j \sigma_i = N_I g\left(\ln\left(\frac{y_I}{l_{00}}\right)\right) + \sum_{i=1}^j g\left(\ln\left(\frac{y_i}{l_{i0}}\right)\right) \quad (6)$$

where l_{i0} is the unstretched length of the i th fiber. Note that the stress of the “old” N_I fibers is not anymore the stress σ but is reduced to a value σ' by the de-tensioning imposed by the insertion of the new j fibers, each of them having a stress σ_i . The two previously considered strategies are also now considered as “limiting” cases, i.e., $l_{i0} = l_{00} = \text{const}$ (i) or $l_{i0} = l_{00} = y_{j-1} e^{-\varepsilon}$ (ii). For the two cases and remembering

that $l_{00} = y_0 e^{-\varepsilon} = y_0 e^{-g^{-1}(\sigma)}$, we obtain respectively $y_j = y_0 e^{g^{-1}\left(\frac{N_I}{j+N_I}\right) - g^{-1}(\sigma)}$ (i) or $y_j = y_{j-1} e^{g^{-1}\left(\frac{N_I}{j+N_I}\right) - g^{-1}(\sigma)}$ (ii) and thus in general:

$$y_j = y_0 e^{\left(g^{-1}\left(\frac{N_I}{j+N_I}\right) - g^{-1}(\sigma)\right)\eta j}, \quad N_I = \frac{W}{\beta w}, \sigma = \beta \frac{w}{A} \quad (7)$$

where for the first (i) strategy the “efficiency” $\eta = \frac{1}{j}$, whereas for the second (ii) one, $\eta = 1$; in general, for different strategies different efficiencies are expected as can be calculated with eq. (6).

The total number N_{II} of fibers inserted in the second phase for lifting the weight up to the desired height $H = y_0 - h$ can be calculated from $y_{j=N_{II}} = h$.

Efficiency

The efficiency η is more related to the lifting velocity than to the energetic gravitational efficiency η' of the entire process; the latter one can be calculated as:

$$\eta' = \frac{WH}{N_I wH + w \sum_{j=1}^{N_{II}} y_j} = \frac{\beta}{\frac{\sum_{j=1}^{N_{II}} y_j}{1 + \frac{N_{II} \langle y_j \rangle}{N_I H}}} = \frac{\beta}{1 + \frac{N_{II} \langle y_j \rangle}{N_I H}} \quad (8)$$

Note that the energy cost of the dragging phase alone basically (identically if $\beta = 1$) reaches the theoretical work to be done for lifting the weight to a height H and thus basically all the energy in the lifting phase is “lost”; accordingly, the energetic efficiency of the dragging+lifting mechanism is low.

Non linear stiffening (or softening)

To better elucidate the results let us assume the nonlinear constitutive law g in the form of $\sigma = g(\epsilon) = \sigma_u \left(\frac{\epsilon}{\epsilon_u}\right)^\alpha$, where the subscript u denotes ultimate values and α is the exponent describing the shape of the

constitutive law: linear elasticity is described by $\alpha=1$, where $\frac{\sigma_u}{\epsilon_u} = E$ is the silk Young's modulus; $\alpha>1$ describes stiffening behavior, as usually observed in biological materials, such as spider silk; $0\leq\alpha<1$ describes softening, as usually observed in engineering materials, such as steel. In such a case, eqs. (6)

and (7) become ($y_j = y_0 e^{-\left[1-\left(\frac{N_I}{j+N_I}\right)^{\frac{1}{\alpha}}\right]\epsilon}$ (i) or $y_j = y_{j-1} e^{-\left[1-\left(\frac{N_I}{j+N_I}\right)^{\frac{1}{\alpha}}\right]\epsilon}$ (ii) are derived for the two strategies respectively):

$$N_I \sigma = N_I \frac{\sigma_u}{\epsilon_u^\alpha} \ln^\alpha \left(\frac{y_j}{l_{00}} \right) + \frac{\sigma_u}{\epsilon_u^\alpha} \sum_{i=1}^j \ln^\alpha \left(\frac{l_j}{l_{i0}} \right) \quad (9a)$$

$$y_j = y_0 e^{-\left[1-\left(\frac{N_I}{n+N_I}\right)^{\frac{1}{\alpha}}\right]\epsilon \eta j}, \quad N_I = \frac{W}{\beta w}, \sigma = \beta \frac{w}{A}, \epsilon = \left(\frac{\sigma}{\sigma_u} \right)^{\frac{1}{\alpha}} \epsilon_u \quad (9b)$$

Eq. (9b) shows that placing the anchorage well above the height H to be reached by the weight (as it is seen in the real observation) is beneficial for reducing the related number of cycles N_{II} , even if the energetic cost could increase. For the first strategy (i) the minimal distance from the anchorage that can be reached is $h = y_\infty = y_0 e^{-\epsilon} = l_{00}$, however this strategy could be iterated n times –the strategy of middle complexity (iii)– to approach the anchoring point at a distance $h = y_\infty = y_0 e^{-n\epsilon}$ and thus $h = y_{n \rightarrow \infty} = 0$. For the second strategy (ii) $y_{j \rightarrow \infty} = y_0 e^{-j\epsilon}$ and again $h = y_\infty = 0$, so the situation after j cycles in strategy (ii) is similar to that of strategy (iii) for $n=j$ cycles of cycles and thus after j^2 cycles. Note that the jumps $\Delta y_j = y_{j-1} - y_j$ are decreasing with j and $\Delta y_\infty = 0$ (and that Δy_1 ($\alpha \rightarrow 1, \epsilon \rightarrow 0$) = $\frac{y_0 \epsilon}{N_I}$ for both the two strategies). Eq. (9b) also shows that large pre-stress (over ultimate stress ratio), nonlinear stiffening (as observed in spider silk) and ultimate strain (again as observed in spider silk) are all beneficial characteristics for the lifting mechanics.

Linearity

In the case of small deformations and linear constitutive law eqs. (9) become:

$$N_I \sigma = N_I E \frac{y_j - l_{00}}{l_{00}} + E \sum_{i=1}^j \left(\frac{y_j - l_{i0}}{l_{i0}} \right) \quad (10a)$$

$$y_j = \frac{(1+\varepsilon)N_I + j}{\frac{N_I}{l_{00}} + \sum_{i=1}^j \frac{1}{l_{i0}}} \quad (10b)$$

For $l_{i0} = \text{const}$, $y_j = \frac{(1+\varepsilon)N_I + j}{\frac{N_I}{l_{00}} + \frac{j}{l_{i0}}}$ and accordingly $y_\infty = l_{i0}$ and if, in addition, $l_{i0} = l_{00}$, i.e., the first strategy (i), $y_j = l_{00} \frac{(1+\varepsilon)N_I + j}{N_I + j}$ and thus $y_\infty = l_{00} = \frac{y_0}{1+\varepsilon}$; accordingly, for n iterations following the middle complexity strategy (iii) $y_\infty = \frac{y_0}{(1+\varepsilon)^n}$. For the second strategy (ii) $l_{i0} = l_{00} = \frac{y_{j-1}}{1+\varepsilon}$, thus $y_j = y_{j-1} \frac{(1+\varepsilon)N_I + j}{(N_I + j)(1+\varepsilon)}$ and $y_{j \rightarrow \infty} = \frac{y_{j-1}}{1+\varepsilon} = \frac{y_0}{(1+\varepsilon)^j}$. Thus in general for linearity (of the constitutive law and for small displacements) $y_{j \rightarrow \infty} = \frac{y_0}{(1+\varepsilon)^{nj}}$ describes a lifting strategy of a given efficiency.

Toy experiments

A simple toy experiment is proposed in Figure 4. Only the second phase, i.e. pure lifting, is considered. Elastic fibers are realized by a series and parallel of elastic bands and attached to a weight (candleholder). Adding/removing and/or disposing in series/parallel these elastic bands result in the weight lifting. Four different experiments with different number of series and parallel elastic bands are reported. Experiments are compared with the simplest linear predictions of eq. (10b) in Table 1, where the strain is computed from $\frac{y_0}{1+\varepsilon} = l_{00}$ with l_{00} considered for a series of elastic bands equal to their number multiplied by the

unstretched length of a single band; the latter is considered as the single free-parameter for all the comparison, taking into account a linearization around a non-zero finite strain.

Conclusions

In this paper we have elucidated for the first time, to the best of our knowledge, the mechanics of spider weight dragging and lifting. We cannot exclude that such phenomena have inspired ancient populations and has thus been applied for dragging and lifting weights before the advent of more advanced and energetically efficient technologies.

Research Ethics: this heading does not apply.

Animal ethics: this heading does not apply.

Permission to carry out fieldwork: this heading does not apply.

Data Availability: this heading does not apply (data concerning the toy experiments are reported in the Table 1).

Competing Interests: We have no competing interests.

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Figure 1. First phase of the spider weight lifting: n_0 silk fibers with given pre-stresses are attached to the shell; after these n_0 cycles the weight starts to move on the surface towards the projection point on it of the anchorage; additional n_1 fibers are then attached for realizing a second movement, and so on. Simultaneous operations, such as re-tensioning (or even cutting) of the pervious fibers, can be done. After a total number of fibers/cycles N_I , of the order of the ratio between the weight of the body to be lifted and the spider weight, the first phase of dragging is terminated: the shell is vertically aligned with the anchorage, touching lightly the substrate, being fully suspended by the silk stressed fibers. In the specific observation $N_I \cong 3$.



Figure 2. Second phase of the spider weight lifting: N_{II} new fibers with given pre-stresses are attached to the shell (at different positions on it, for better lifting weight stability) and simultaneous operations, such as re-tensioning (and even cutting) of the previous fibers, are done as suggested by the absence of floppy threads; after these N_{II} cycles, the shell is lifted from the bottom surface up to the desired height H (the shell is then used for spider protection, e.g. against desiccation). In the specific observation a $\Delta y \cong \text{shell}$ size is reached with about 10 cycles when approaching the final height H .

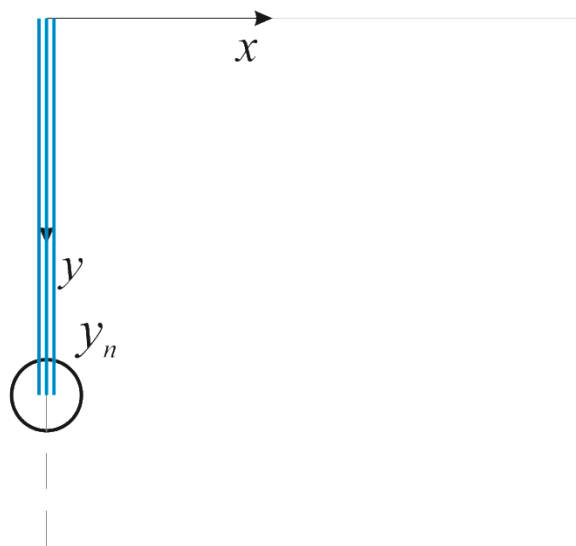
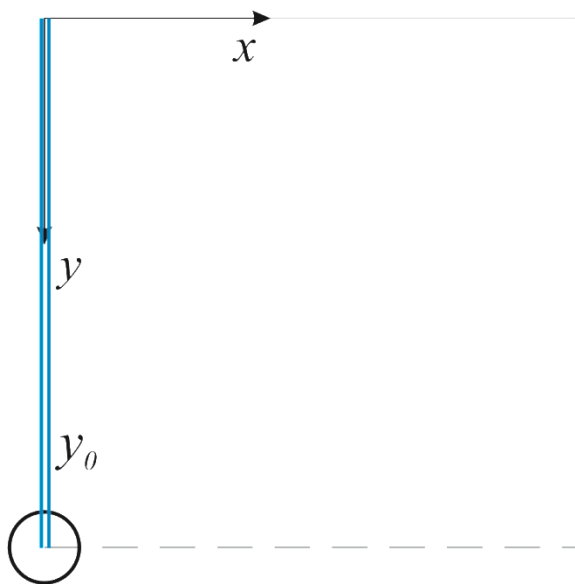
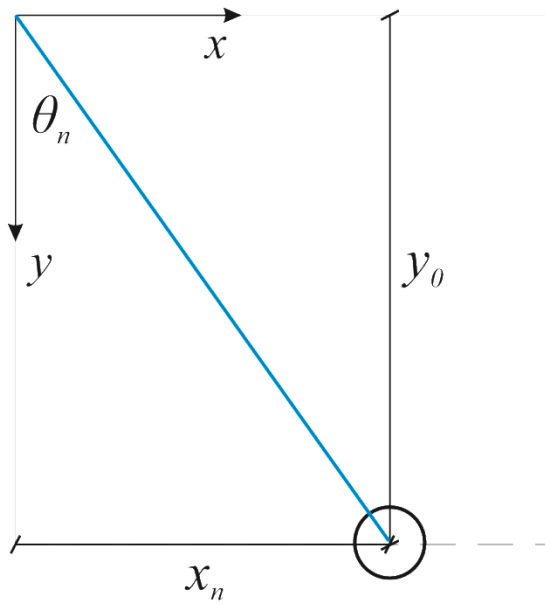
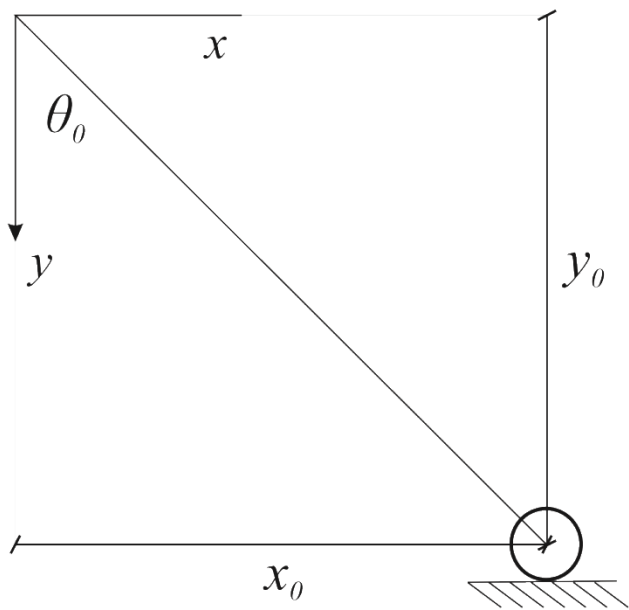


Figure 3. Spider dragging and lifting phases. Top left panel, initial condition: reference system with origin in the anchorage point and initial coordinates x_0, y_0 of the weight. Top right panel, dragging: pre-stressed silk fibers are attached to the weight and it starts to move horizontally towards the projection on the surface of the anchorage point, thus with coordinates $x_{j \rightarrow j_I} \rightarrow 0, y_0$. Bottom left panel, phase change: end of the first phase and beginning of the second one, at $x_{j=j_I} = 0, y_0$; the weight is vertically aligned with the anchorage and touches lightly the substrate, being fully suspended by the silk stressed fibers. Bottom right panel, lifting: the weight is lifted thanks to the insertion of other pre-stressed silk fibers with coordinates $x_j = 0, y_{j \rightarrow j_{II}} \rightarrow h$, where $h = y_0 - H$ and H is the desired lifting height.



Figure 4. Toy experiments inspired by the spider weight lifting. Elastic fibers are realized by a series of elastic bands and attached to a weight (candleholder). Four different experiments with different number of series and parallel elastic bands are reported. Adding/removing and/or disposing in series/parallel these elastic bands result in the weight lifting. Such experiments are compared with the simplest linear predictions of eq. (10b) in Table 1.

Number of elastic bands in series + in parallel	$y_0 - y_n^{(exp)}$	$y_0 - y_n^{(theo)}$
7	0.0	0.00
7+6	13.5	13.46
7+6+5	17.0	18.38
7+6+5+4	21.5	21.22
7+6+5+4+3	24.5	23.29
7+6+5+4+3+2	27.0	25.08
7	0.0	0.00
4	21.0	20.14
4+4	24.0	22.43
4+4+4	24.5	23.57
4+4+4+4	25.0	24.26
7	0.0	0.00
6+6	16.5	14.71
5+5+5	20.5	20.29
4+4+4+4	25.0	24.26
3+3+3+3+3	27.5	25.94
2+2+2+2+2+2	30.0	27.86
8	0	0
4+4	32.0	36.00
2+2+2+2	39.5	39.25

Table 1. Toy experimental results and comparison with linearized theory. Here $N_I=1$, $y_0 = 31\text{cm}$ for the 7 elastic bands (three experiments) or 41 cm for the 8 elastic bands (forth experiment), $l_{00} = k \times 1\text{cm}$ where k is the number of elastic band in a series and 1cm is the effective unstretched length of a single band, considered here as the free-parameter for taking into account a linearization around a non-zero finite strain (its apparent value is appears nearly doubled).